

# Eddy Currents

Induced eddy currents and associated thermal loads are of interest in many high power AC applications. This example is of general nature and illustrates some of the involved physics as well as suitable modeling techniques in the AC/DC Module.

# Model Definition

A metallic plate is placed near a 50 Hz AC conductor. The resulting eddy current distribution in the plate depends on the conductivity and permeability of the plate. In the discussion, four different materials are considered: copper, aluminum, stainless steel, and magnetic iron. The step-by-step instructions focus on copper and iron. The geometry consists of a single wire and a plate with dimensions as shown in Figure 1.

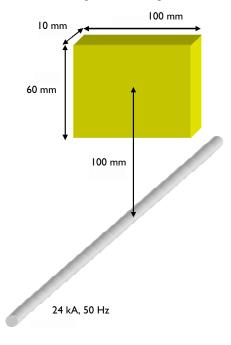


Figure 1: The model geometry.

Because one cannot afford meshing an infinite volume, it is necessary to specify a finite volume to mesh and solve for. In this case, it makes sense to enclose the wire and the plate in a cylinder with the wire on the cylinder axis. This is a good choice when used with the default boundary condition, Magnetic Insulation, which forces the field to be tangential

to the exterior boundaries. For the cylindrical shape of the domain, that is a reasonable approximation to reality. The conductor is modeled as a line current with 0° phase and an effective (RMS) value of 24 kA.

The magnetic vector potential is calculated from

$$(j\omega\sigma - \omega^2\varepsilon)\mathbf{A} + \nabla \times \left(\frac{1}{\mu}\nabla \times \mathbf{A}\right) = \mathbf{0}$$

where  $\sigma$  is the conductivity,  $\epsilon$  the permittivity, and  $\mu$  the permeability. An important parameter in eddy current modeling is the skin depth,  $\delta$ .

$$\delta = \sqrt{\frac{2}{\omega\mu\sigma}}$$

The following table lists the skin depth for the different materials at a frequency of 50 Hz.

MATERIAL	DEL DEDMEADULEY	COMPLICATIVITY	CKINI DERTII
MATERIAL	REL. PERMEABILITY	CONDUCTIVITY	SKIN DEPTH
Copper	1	5.998·10 <sup>7</sup> S/m	9 mm
Aluminum	1	3.774·10 <sup>7</sup> S/m	I2 mm
Stainless steel	1	1.137·10 <sup>6</sup> S/m	67 mm
Iron	4000	1.12·10 <sup>7</sup> S/m	0.34 mm

In order for the model to produce accurate results, the mesh needs to resolve the evanescent fields in the metal. In practice, this means you need to resolve the skin depth with at least more than 1 element, preferably closer to 2, or even more. This application uses a maximum element size of 5 mm for the copper plate.

When the skin depth is small in comparison to the size of the conducting objects, it can be practically impossible to resolve it. This often happens at high frequencies, in large structures, or with highly conductive and permeable materials. These cases require a different technique: Exclude the interior of the conducting objects from the model. Instead, represent them with an impedance boundary condition. This condition essentially sets the skin depth to zero, making all induced currents flow on the surface of the conductors. Mathematically, the relation between the magnetic and electric fields at the boundary reads:

$$\mathbf{n} \times \mathbf{H} + \sqrt{\frac{\epsilon - j\sigma/\omega}{\mu}} \mathbf{n} \times (\mathbf{E} \times \mathbf{n}) = \mathbf{0}$$

The dissipated power density,  $P_d$  (SI unit: W/m<sup>2</sup>) can be calculated from

$$P_{\rm d} = \frac{1}{2} (\mathbf{J}_S \cdot \mathbf{E^*})$$

where  $\mathbf{J}_{S}$  is the induced surface current density, and the asterisk (\*) denotes the complex conjugate.

This model has the interior of the plate included in the model for copper, and uses the impedance boundary condition for magnetic iron.

# Results and Discussion

In Figure 2, the induced eddy current distribution for a plate made of copper is shown as streamlines, whereas the distribution of the ohmic losses is shown as a slice plot.

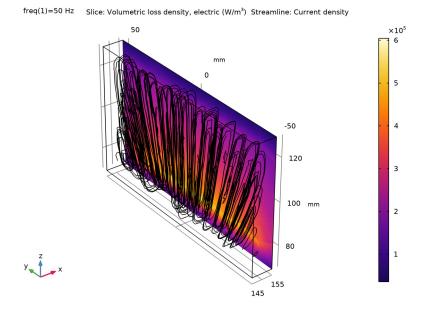


Figure 2: Induced eddy current distribution and losses in the copper plate.

A total dissipated power of 6 W was obtained from integration through the plate. If you repeat the simulation for different materials, the application shows that lowering the conductivity decreases the dissipated power. However, for high permeability materials like soft iron, the dissipated power is higher than in copper (27 W) despite a much lower conductivity.

Application Library path: ACDC Module/Introductory Electromagnetics/ eddy\_currents

# Modeling Instructions

From the File menu, choose New.

#### NEW

In the New window, click Model Wizard.

## MODEL WIZARD

- I In the Model Wizard window, click **3D**.
- 2 In the Select Physics tree, select AC/DC > Electromagnetic Fields > Magnetic Fields (mf).
- 3 Click Add.
- 4 Click Study.
- 5 In the Select Study tree, select General Studies > Frequency Domain.
- 6 Click M Done.

## **GEOMETRY I**

- I In the Model Builder window, under Component I (compl) click Geometry I.
- 2 In the Settings window for Geometry, locate the Units section.
- 3 From the Length unit list, choose mm.

Cylinder I (cyl1)

- I In the Geometry toolbar, click ( Cylinder.
- 2 In the Settings window for Cylinder, locate the Size and Shape section.
- 3 In the Radius text field, type 250.
- 4 In the Height text field, type 300.
- 5 Locate the Axis section. From the Axis type list, choose Cartesian.
- 6 In the x text field, type 1.
- 7 In the z text field, type 0.

Line Segment I (Is I)

I In the Geometry toolbar, click  $\bigcirc$  More Primitives and choose Line Segment.

- 2 In the Settings window for Line Segment, locate the Starting Point section.
- **3** From the **Specify** list, choose **Coordinates**.
- 4 Locate the **Endpoint** section. From the **Specify** list, choose **Coordinates**.
- 5 In the x text field, type 300.
- 6 Click Build All Objects.

# Block I (blk I)

- I In the Geometry toolbar, click Block.
- 2 In the Settings window for Block, locate the Size and Shape section.
- 3 In the Width text field, type 10.
- 4 In the **Depth** text field, type 100.
- 5 In the Height text field, type 60.
- 6 Locate the Position section. In the x text field, type 145.
- 7 In the y text field, type -50.
- 8 In the z text field, type 70.
- 9 Click Build All Objects.
- **10** Click the **Transparency** button in the **Graphics** toolbar.

The model geometry is now complete. Prepare your simulation by defining selections.

# DEFINITIONS

# Plate

- I In the **Definitions** toolbar, click 🔓 **Explicit**.
- 2 In the Settings window for Explicit, type Plate in the Label text field.
- 3 Select Domain 2 only.

#### Plate Boundaries

- I In the **Definitions** toolbar, click **\( \frac{1}{3} \) Explicit**.
- 2 In the Settings window for Explicit, type Plate Boundaries in the Label text field.
- **3** Select Domain 2 only.
- 4 Locate the Output Entities section. From the Output entities list, choose Adjacent boundaries.

# ADD MATERIAL

I In the Materials toolbar, click **‡** Add Material to open the Add Material window.

- 2 Go to the Add Material window.
- 3 In the tree, select Built-in > Copper.
- **4** Click the **Add to Component** button in the window toolbar.
- 5 In the Materials toolbar, click **4** Add Material to close the Add Material window.

#### MATERIALS

Copper (mat1)

- I In the Settings window for Material, locate the Geometric Entity Selection section.
- 2 From the Selection list, choose Plate.

# MAGNETIC FIELDS (MF)

Ambère's Law in Solids I

- I In the Physics toolbar, click Domains and choose Ampère's Law in Solids.
- 2 In the Settings window for Ampère's Law in Solids, locate the Domain Selection section.
- 3 From the Selection list, choose Plate.
- 4 In the list, select 2.

Edge Current I

- I In the Physics toolbar, click **Edges** and choose **Edge Current**.
- **2** Select Edge 6 only.
- 3 In the Settings window for Edge Current, locate the Edge Current section.
- **4** In the  $I_0$  text field, type sqrt(2)\*24[kA], resulting in an RMS current of 24 kA.

## MESH I

To resolve the skin depth while maintaining a good mesh economy, mesh the copper plate finer than the rest of the geometry. Note that you need to add the finer mesh first in the sequence; otherwise you would get a coarse mesh on the common domain boundaries that would constrain the mesh inside the copper plate domain.

Free Tetrahedral I

- I In the Mesh toolbar, click A Free Tetrahedral.
- 2 In the Settings window for Free Tetrahedral, locate the Domain Selection section.
- 3 From the Geometric entity level list, choose Domain.
- 4 From the Selection list, choose Plate.
- 5 Click to expand the Scale Geometry section. In the y-direction scale text field, type 0.4.

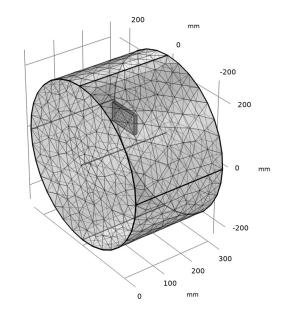
6 In the z-direction scale text field, type 0.4.

# Size 1

- I Right-click Free Tetrahedral I and choose Size.
- 2 In the Settings window for Size, locate the Element Size section.
- **3** Click the **Custom** button.
- 4 Locate the Element Size Parameters section.
- **5** Select the **Maximum element size** checkbox. In the associated text field, type **5**.

## Free Tetrahedral 2

- I In the Mesh toolbar, click A Free Tetrahedral.
- 2 In the Model Builder window, right-click Mesh I and choose Build All.





### STUDY I

# Step 1: Frequency Domain

- I In the Model Builder window, under Study I click Step I: Frequency Domain.
- 2 In the Settings window for Frequency Domain, locate the Study Settings section.
- 3 In the Frequencies text field, type 50.
- 4 In the Study toolbar, click **Compute**.

#### RESULTS

# Magnetic Flux Density (mf)

The default plot shows the magnetic flux density norm in three cross sections. The following instructions show you how to visualize the eddy currents and the resistive heating in the copper plate.

# Study I/Solution I (2) (soll)

- I In the Model Builder window, expand the Results > Datasets node.
- 2 Right-click Results > Datasets > Study I/Solution I (soll) and choose Duplicate.

# Selection

- I In the Results toolbar, click has a Attributes and choose Selection.
- 2 In the Settings window for Selection, locate the Geometric Entity Selection section.
- 3 From the Geometric entity level list, choose Domain.
- 4 From the Selection list, choose Plate. Switch from transparency to wireframe rendering.
- **5** Click the **Transparency** button in the **Graphics** toolbar.
- 6 Click the Wireframe Rendering button in the Graphics toolbar.

# Eddy Currents and Heating

- I In the Results toolbar, click **3D Plot Group**.
- 2 In the Settings window for 3D Plot Group, type Eddy Currents and Heating in the Label text field.
- 3 Locate the Data section. From the Dataset list, choose Study I/Solution I (2) (soll).

# Slice 1

- I Right-click Eddy Currents and Heating and choose Slice.
- 2 In the Settings window for Slice, click Replace Expression in the upper-right corner of the Expression section. From the menu, choose Component I (compl) > Magnetic Fields > Heating and losses > mf.Qrh - Volumetric loss density, electric - W/m3.
- 3 Locate the Plane Data section. From the Entry method list, choose Coordinates.
- 4 In the x-coordinates text field, type 154.9.
- 5 Locate the Coloring and Style section. From the Color table list, choose HeatCamera.
- **6** In the **Eddy Currents and Heating** toolbar, click  **Plot**.

#### Streamline 1

- I In the Model Builder window, right-click Eddy Currents and Heating and choose Streamline.
- 2 In the Settings window for Streamline, click Replace Expression in the upper-right corner of the Expression section. From the menu, choose Component I (compl) > Magnetic Fields > Currents and charge > mf.]x,mf.]y,mf.]z - Current density.
- 3 Locate the Streamline Positioning section. From the Positioning list, choose Uniform density.
- 4 In the Separating distance text field, type 0.06.
- 5 Locate the Coloring and Style section. Find the Point style subsection. From the Color list, choose Black.

Zoom in to get a better view of the results.

# Eddy Currents and Heating

- I In the Model Builder window, click Eddy Currents and Heating.
- 2 In the Eddy Currents and Heating toolbar, click Plot.

As a final step, integrate the resistive heating in the copper to compute the total heating power.

## Volume Integration 1

- I In the Results toolbar, click  $\frac{8.85}{6.12}$  More Derived Values and choose Integration > Volume Integration.
- 2 In the Settings window for Volume Integration, locate the Selection section.
- 3 From the Selection list, choose Plate.
- 4 Click Replace Expression in the upper-right corner of the Expressions section. From the menu, choose Component I (compl) > Magnetic Fields > Heating and losses > mf.Qrh -Volumetric loss density, electric - W/m3.
- 5 Click **= Evaluate**.

The result should be close to 6 W.

If you would like to repeat the analysis for aluminum or some other material with a skin depth of the order of 1 cm or greater, just change the material in the plate and run the simulation again. In the remaining part of this tutorial, the Impedance Boundary Condition will be used to compute the results for magnetic iron, which has a skin depth far less than the thickness of the plate.

# MAGNETIC FIELDS (MF)

- I In the Model Builder window, under Component I (compl) click Magnetic Fields (mf).
- 2 In the Settings window for Magnetic Fields, locate the Domain Selection section.
- 3 From the Selection list, choose Manual.
- 4 Select Domain 1 only.

Removing the plate means no equations will be solved inside it. Add an **Impedance Boundary Condition** to switch to a surface representation instead.

Impedance Boundary Condition I

- I In the Physics toolbar, click **Boundaries** and choose Impedance Boundary Condition.
- 2 In the Settings window for Impedance Boundary Condition, locate the Boundary Selection section.
- 3 From the Selection list, choose Plate Boundaries.

## ADD MATERIAL

- I In the Home toolbar, click **Add Material** to open the Add Material window.
- 2 Go to the Add Material window.
- 3 In the tree, select Built-in > Iron.
- **4** Click the **Add to Component** button in the window toolbar.
- 5 In the Home toolbar, click 👯 Add Material to close the Add Material window.

# MATERIALS

Iron (mat2)

- I In the Settings window for Material, locate the Geometric Entity Selection section.
- 2 From the Geometric entity level list, choose Boundary.
- 3 From the Selection list, choose Plate Boundaries.

# STUDY I

In order to keep the results for copper, disable **Solver I** before computing the study. This way, COMSOL Multiphysics will generate a second solver branch.

Solution I (soll)

- I In the Model Builder window, expand the Study I > Solver Configurations node.
- 2 Right-click Solution I (soll) and choose Disable.
- 3 In the Model Builder window, click Study 1.

- 4 In the Settings window for Study, locate the Study Settings section.
- 5 Clear the Generate default plots checkbox.
- 6 In the Study toolbar, click **Compute**.

#### RESULTS

Study 1/Solution 2 (sol2)

In the Model Builder window, under Results > Datasets click Study I/Solution 2 (sol2).

## Selection

- I In the Results toolbar, click has a Attributes and choose Selection.
- 2 In the Settings window for Selection, locate the Geometric Entity Selection section.
- 3 From the Geometric entity level list, choose Boundary.
- 4 From the Selection list, choose Plate Boundaries.

The resistive heating variable is now available on the surface of the plate. You can add a surface plot for the surface resistive heating.

Surface Loss Density, Electric

- I In the Results toolbar, click **3D Plot Group**.
- 2 In the Settings window for 3D Plot Group, type Surface Loss Density, Electric in the Label text field.
- 3 Locate the Data section. From the Dataset list, choose Study I/Solution 2 (sol2).

## Surface I

- I Right-click Surface Loss Density, Electric and choose Surface.
- 2 In the Settings window for Surface, click Replace Expression in the upper-right corner of the Expression section. From the menu, choose Component I (compl) > Magnetic Fields > Heating and losses > mf.Qsrh - Surface loss density, electric - W/m<sup>2</sup>.
- 3 Locate the Coloring and Style section. From the Color table list, choose HeatCamera.

Surface Integration 2

- I In the Results toolbar, click  $\frac{8.85}{6.12}$  More Derived Values and choose Integration > Surface Integration.
- 2 In the Settings window for Surface Integration, locate the Data section.
- 3 From the Dataset list, choose Study I/Solution 2 (sol2).
- 4 Locate the Selection section. From the Selection list, choose Plate Boundaries.

- **5** Click **Replace Expression** in the upper-right corner of the **Expressions** section. From the menu, choose Component I (compl) > Magnetic Fields > Heating and losses > mf.Qsrh -Surface loss density, electric - W/m<sup>2</sup>.
- 6 Click **= Evaluate**.

The result should be close to 27 W.