

# Stress analysis of flexible glass in a large deformation test setup

W. Langgemach

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Flexible glass with thicknesses below 100  $\mu\text{m}$  has outstanding properties:

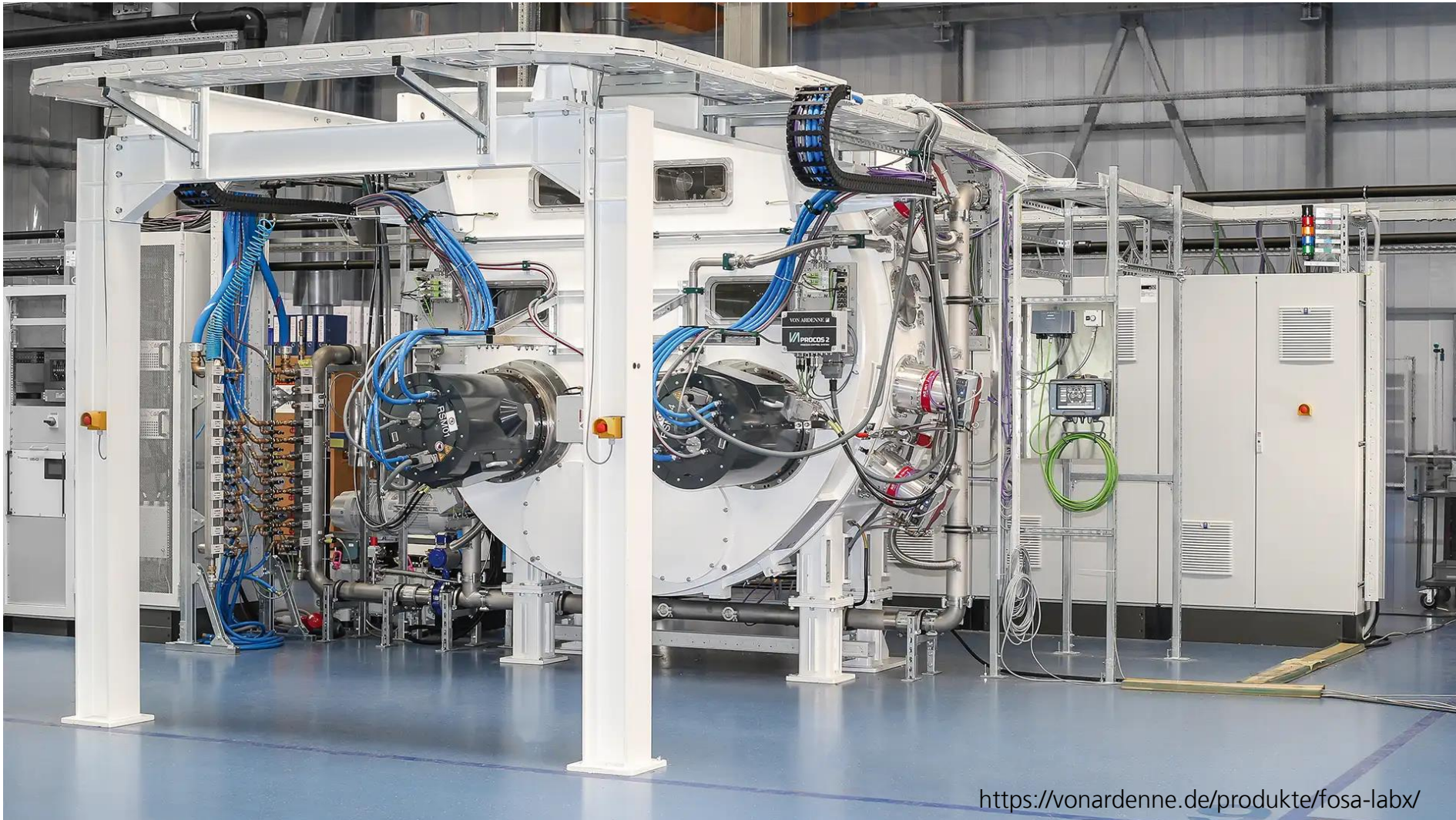
- Low surface roughness
- Outstanding barrier properties
- ...

... it is, however, still brittle.

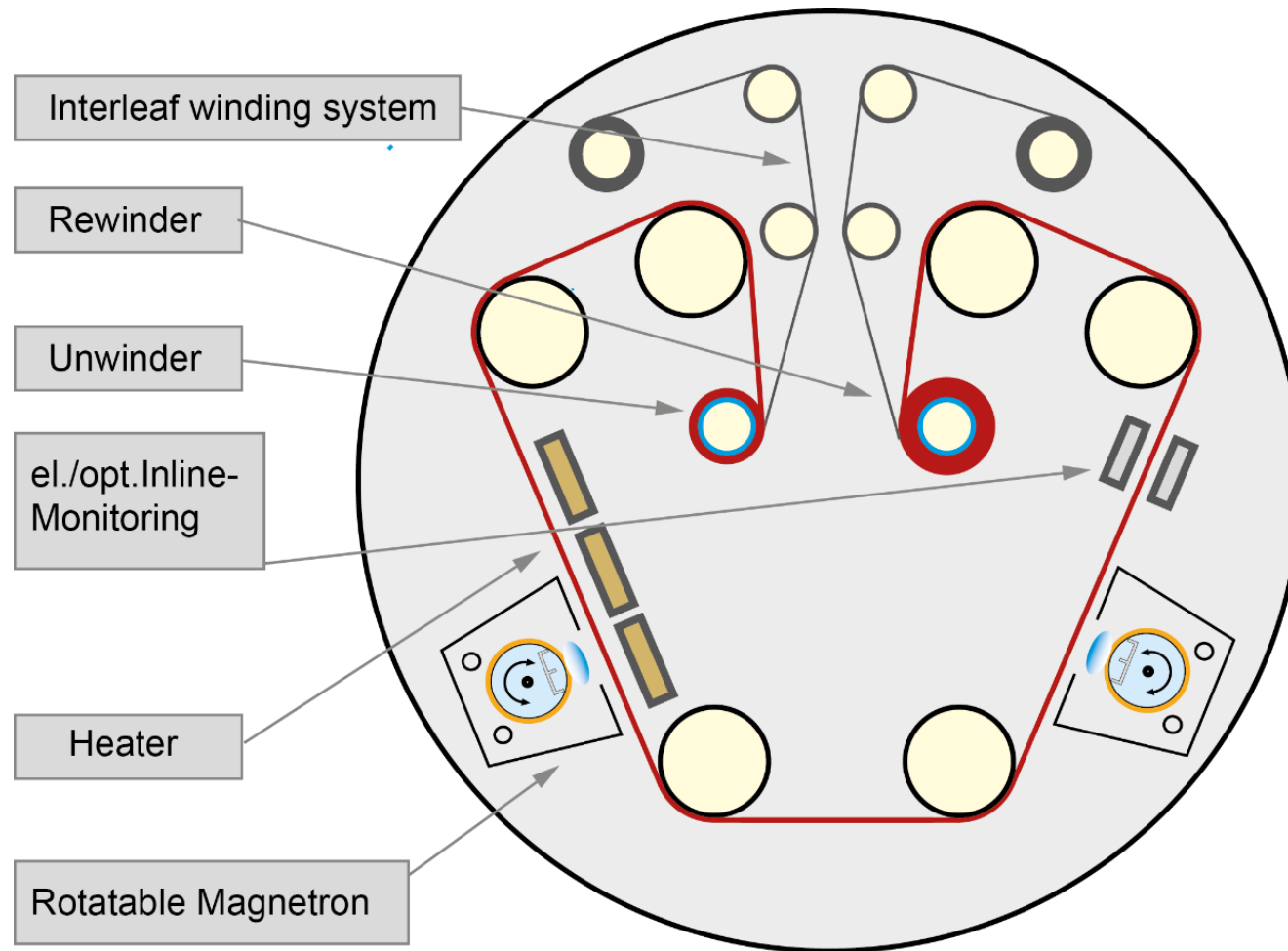




# Fosa LabX – Roll-to-roll pilot coating machine for flexible glass



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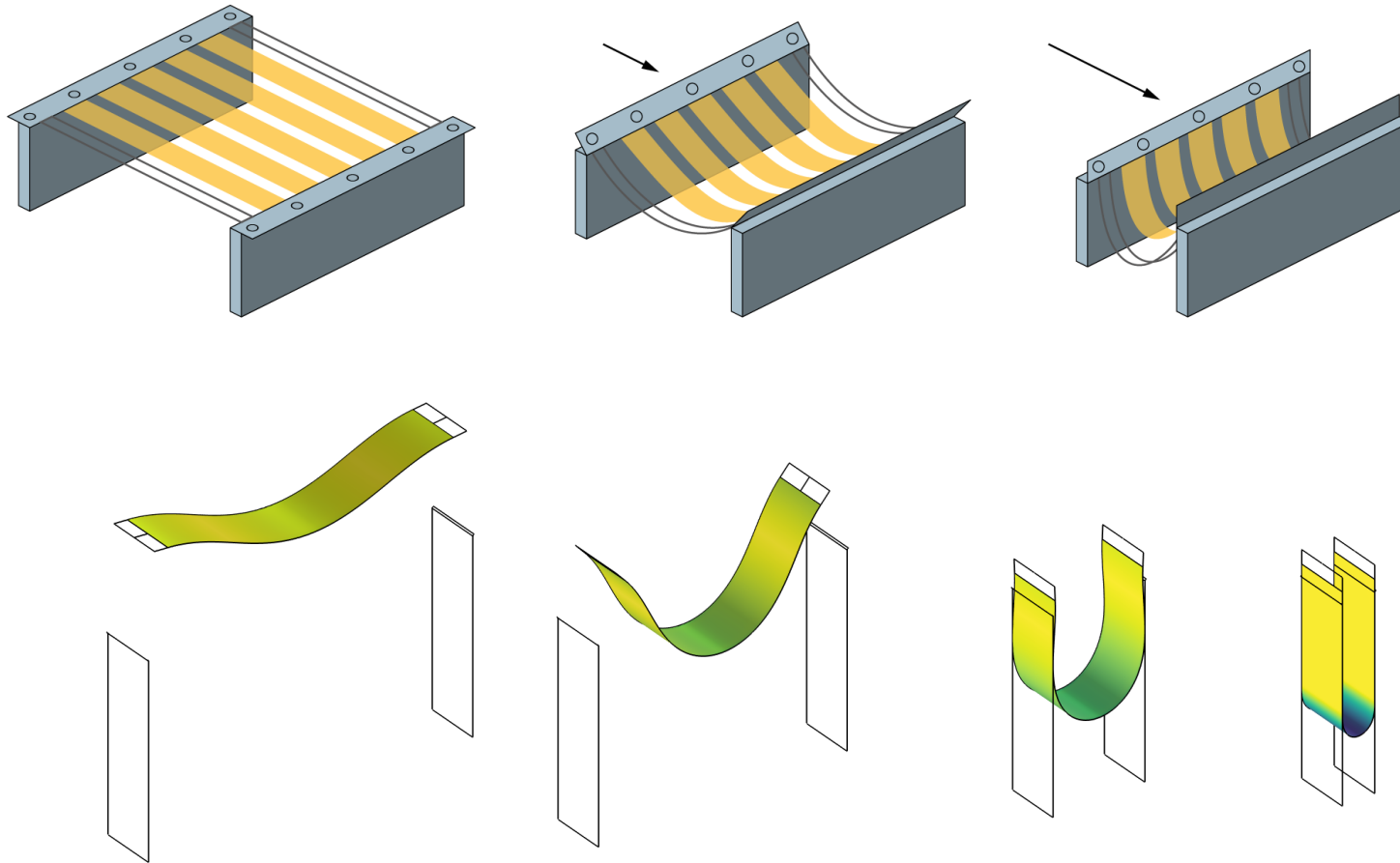




Newly developed fatigue test setup using a U-Shape Folding Tester by Bayflex solutions (endurance test machine).  
→ Customized for flexible glass testing with 3D printed specimen holders



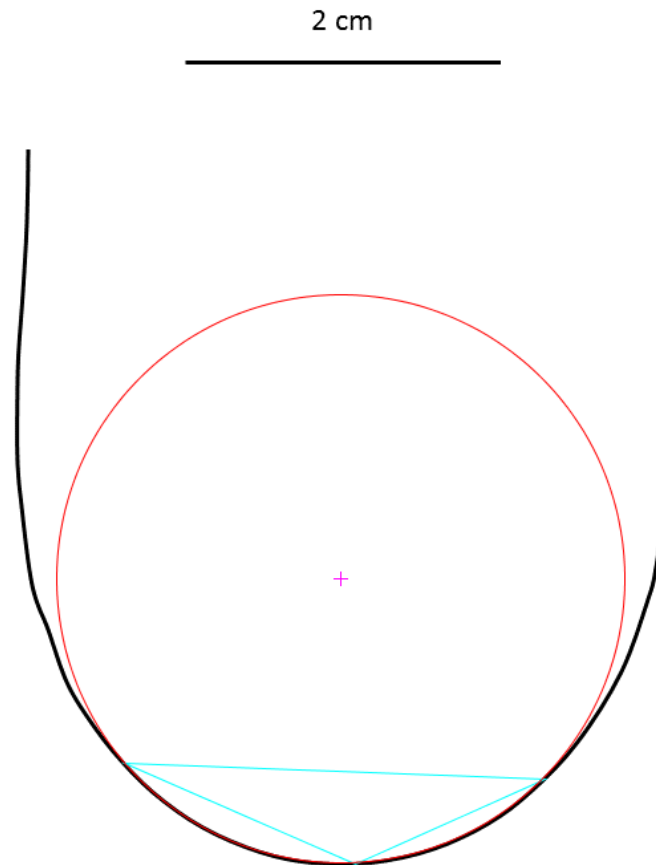
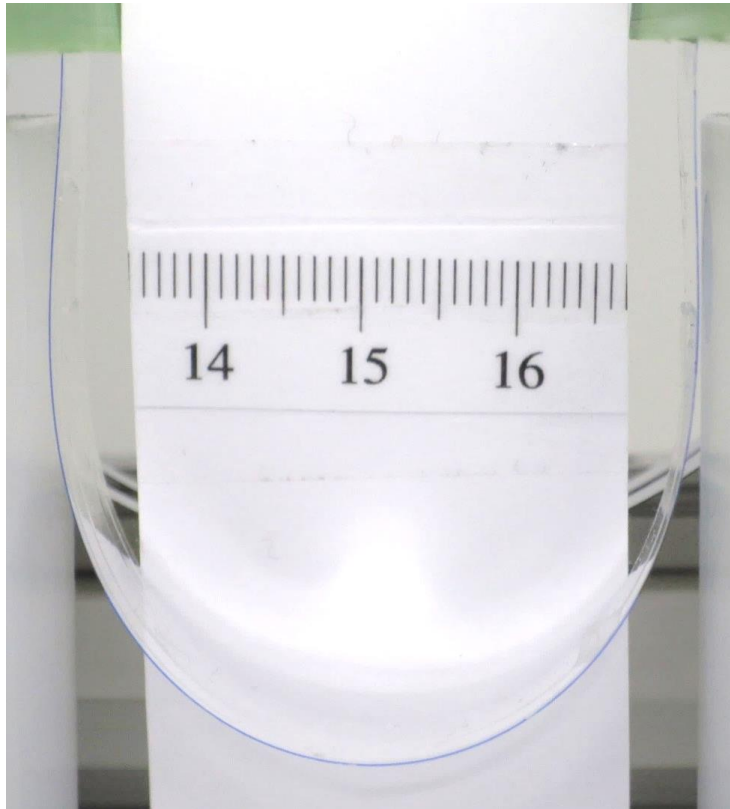
# U-Shape folding test using an endurance testing machine



## Two phases of deformation:

1. Horizontal state into drop-like form
2. U-Shape deformation with wall contact

# Estimation of the bending radius from frontal photographs



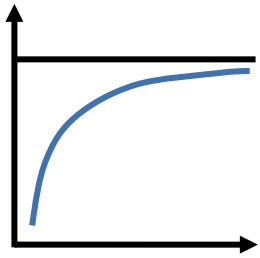
Assuming pure bending:

$$\sigma_{max} = \frac{E \cdot t}{2R}$$

- $\sigma_{max}$  ... Maximum stress
- $E$  ... Young's modulus
- $t$  ... Glass thickness
- $R$  ... bending radius

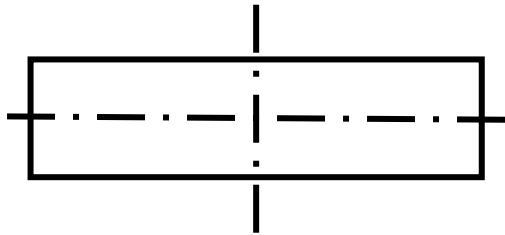
# COMSOL Simulation of sample deformation

Structural mechanics module



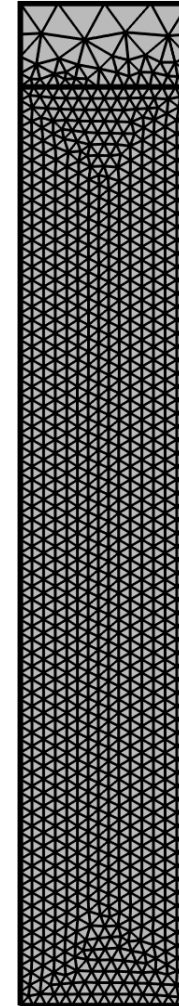
## Stationary non-linear study

- Large geometric deformation
- Contact
- Evaluation of first principal stress



## Simulation details

- Quarter of the sample
- Shell structure
- Triangular mesh elements

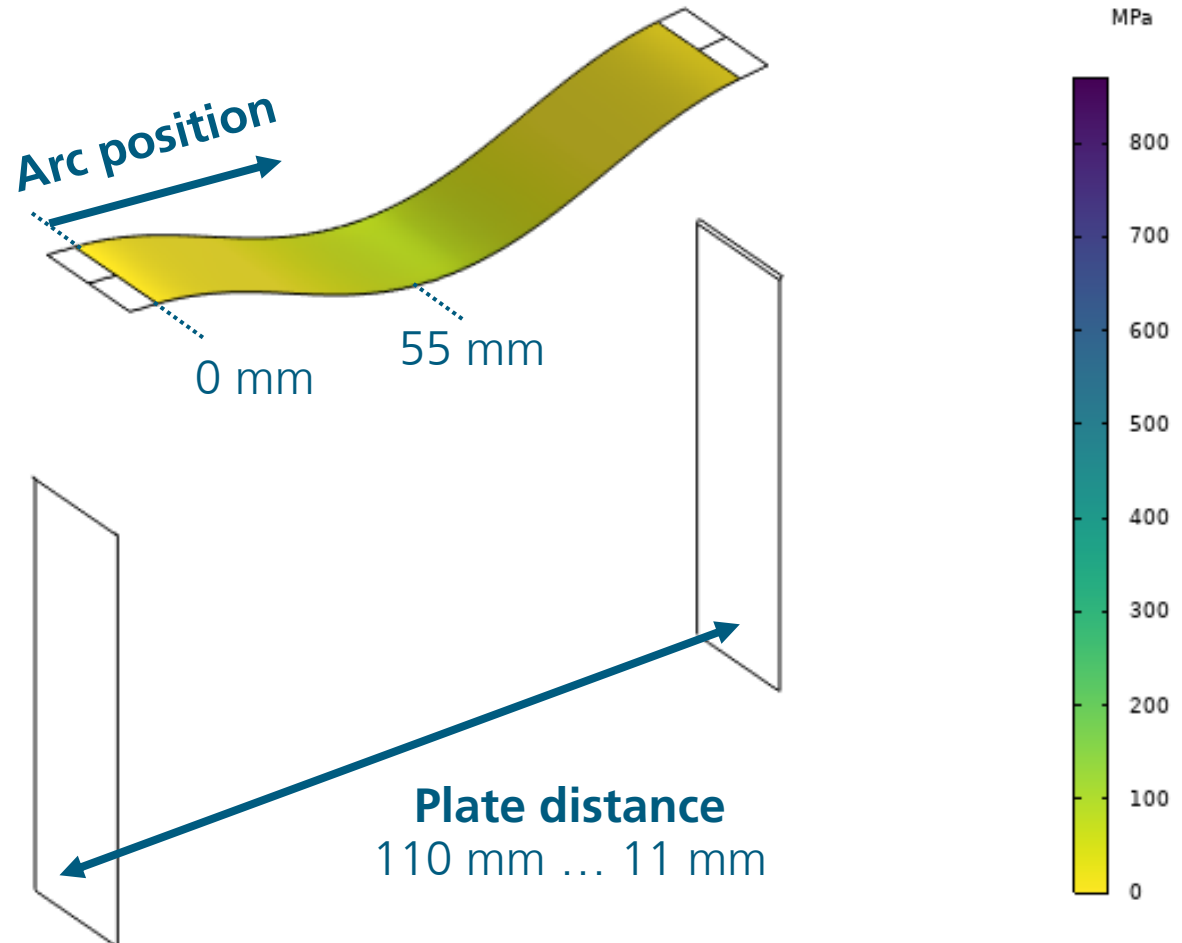




# Clarification of terms

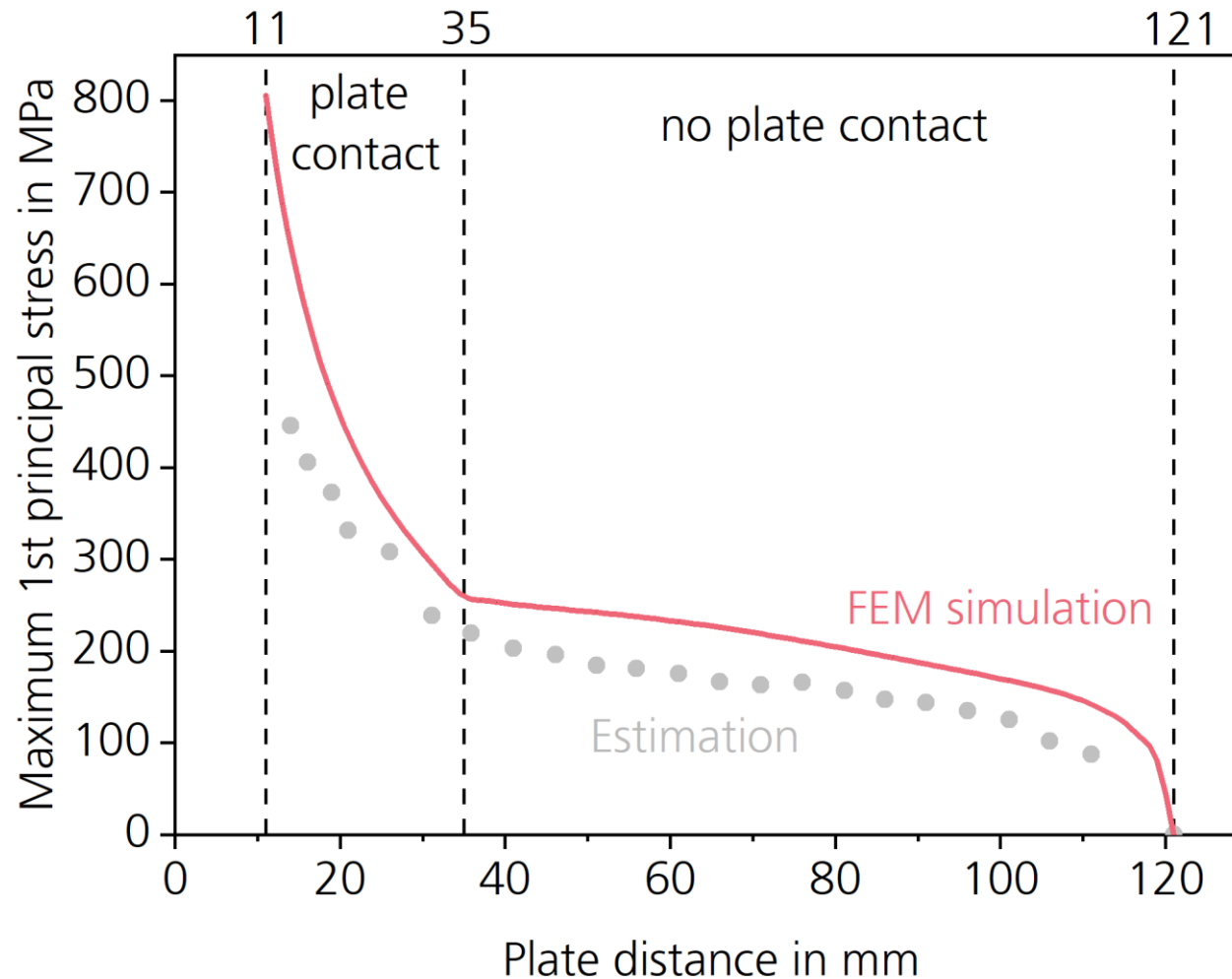
**Sample dimensions**  
20 x 120 x 0.1 mm<sup>3</sup>

**Deformed part**  
20 x 110 x 0.1 mm<sup>3</sup>



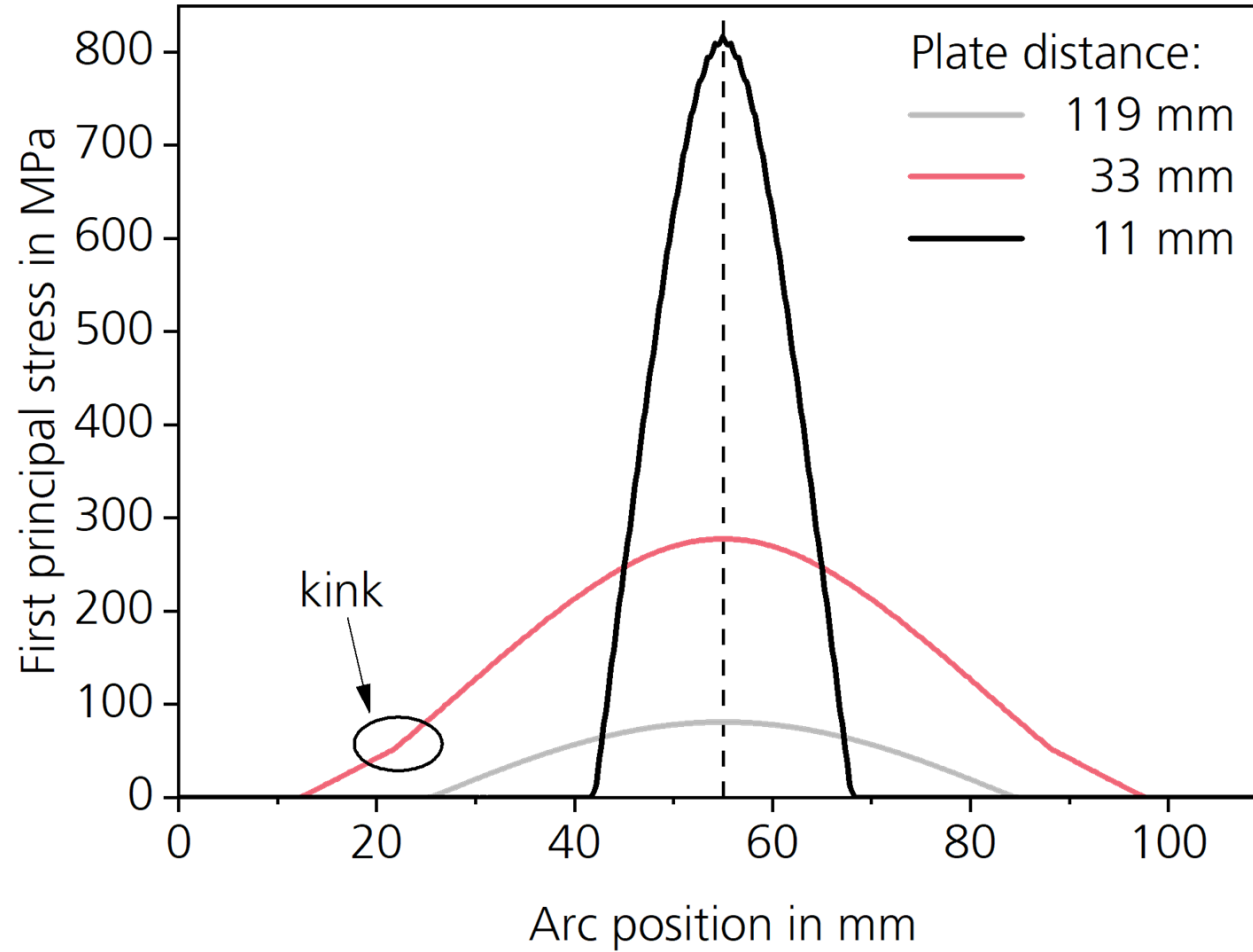
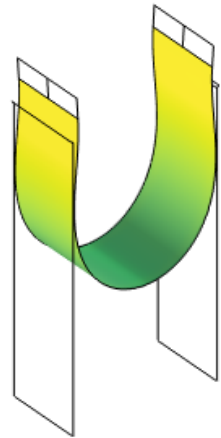
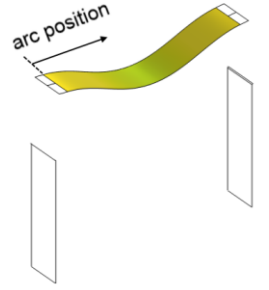
# The maximum stress curve is non-linear and consists of two ranges

First principal stress



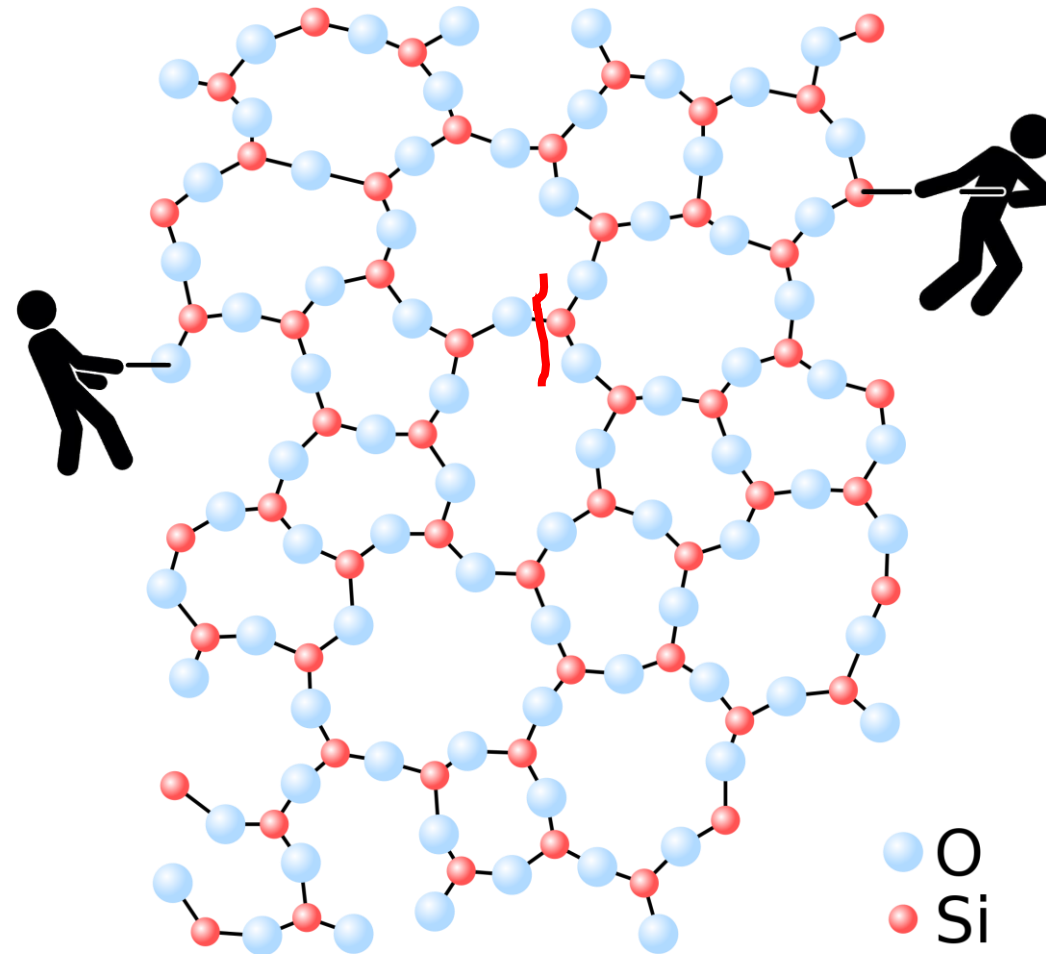
# Analysis of the stress distribution in the sample

## First principal stress





# When glass breaks, atomic bonds are broken up



Glass network: Jdrewitt, Public domain, via Wikimedia Commons

# All you need to know about glass strength (today)



1. Failure at the weakest link
2. Glass strength is statistically distributed, following the Weibull distribution
3. Compressive strength is 10x higher than the tensile strength

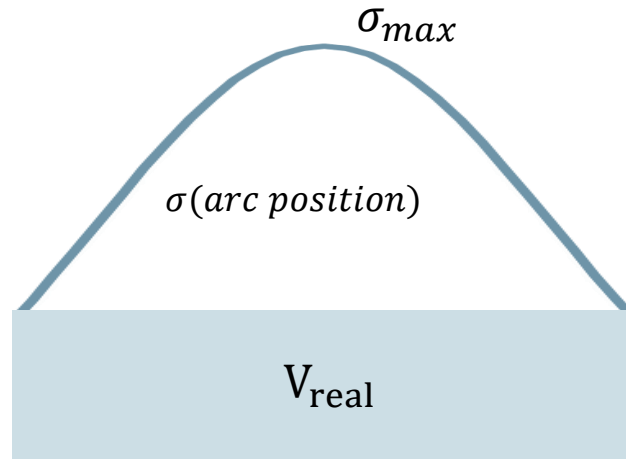
[Icons](#) by Vecteezy

# Effective length of the sample

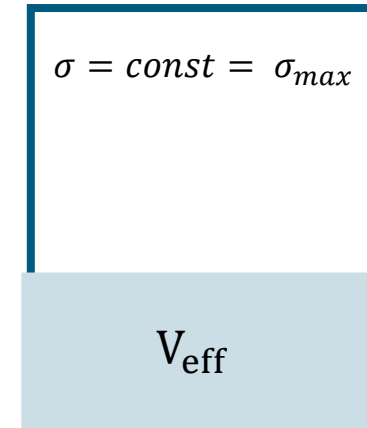
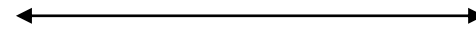
Fracture mechanics for professionals ☺

Weibull:

$$F(\sigma) = 1 - e^{-\left(\frac{\sigma}{\sigma_{crit}}\right)^m}$$

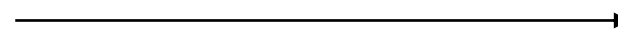


Equal failure probability



$$V_{eff} = \int_{\sigma > 0} \left( \frac{\sigma(\vec{r})}{\sigma_r} \right)^m dV$$

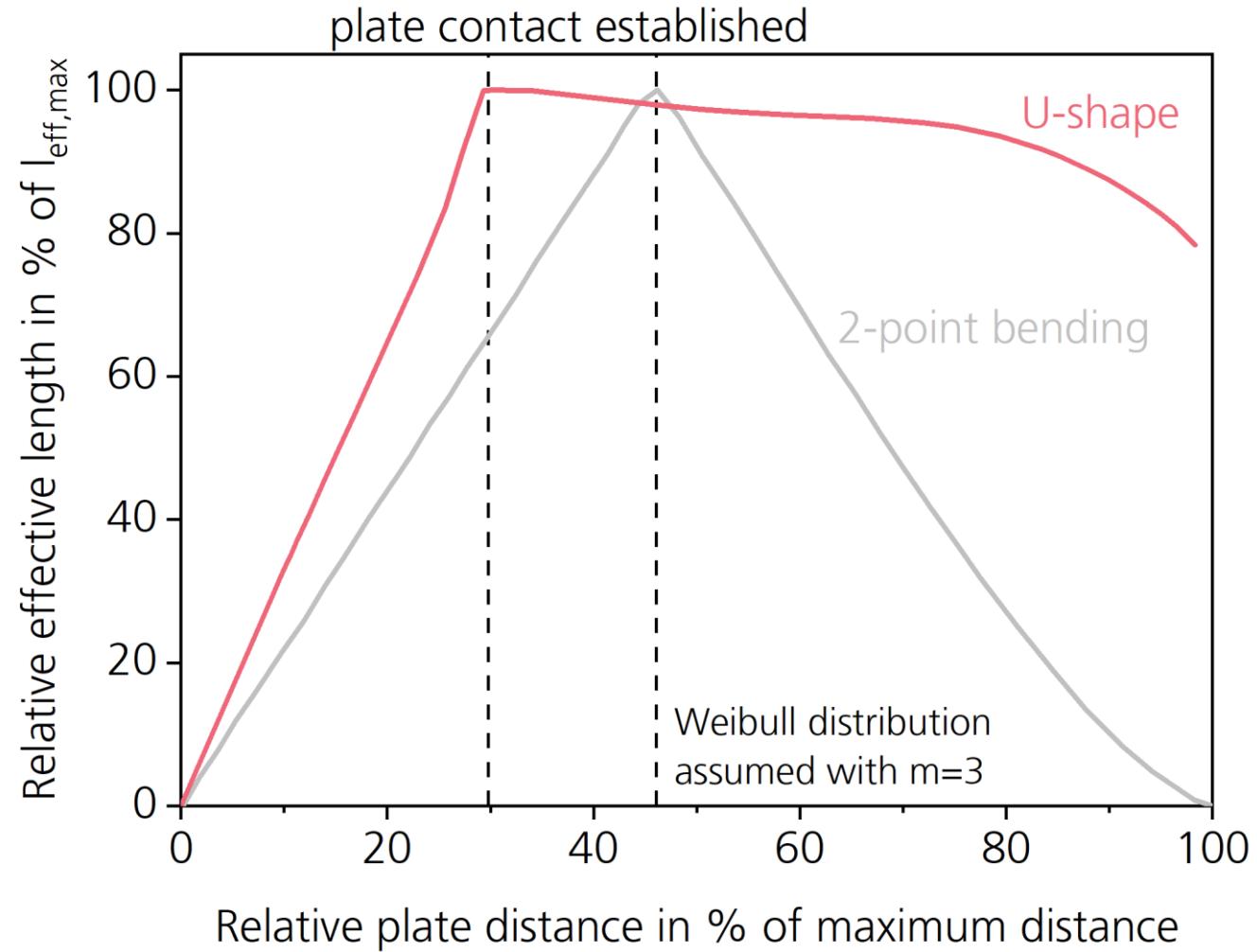
constant cross-section



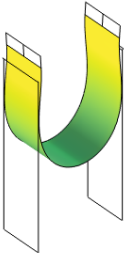
$$l_{eff} = \int_{\sigma > 0} \left( \frac{\sigma(l)}{\sigma_{max}} \right)^m dl$$



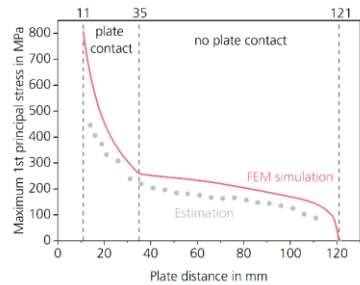
# Effective length



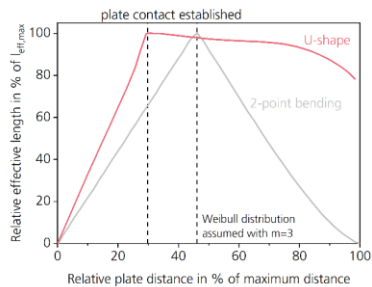
# Summary



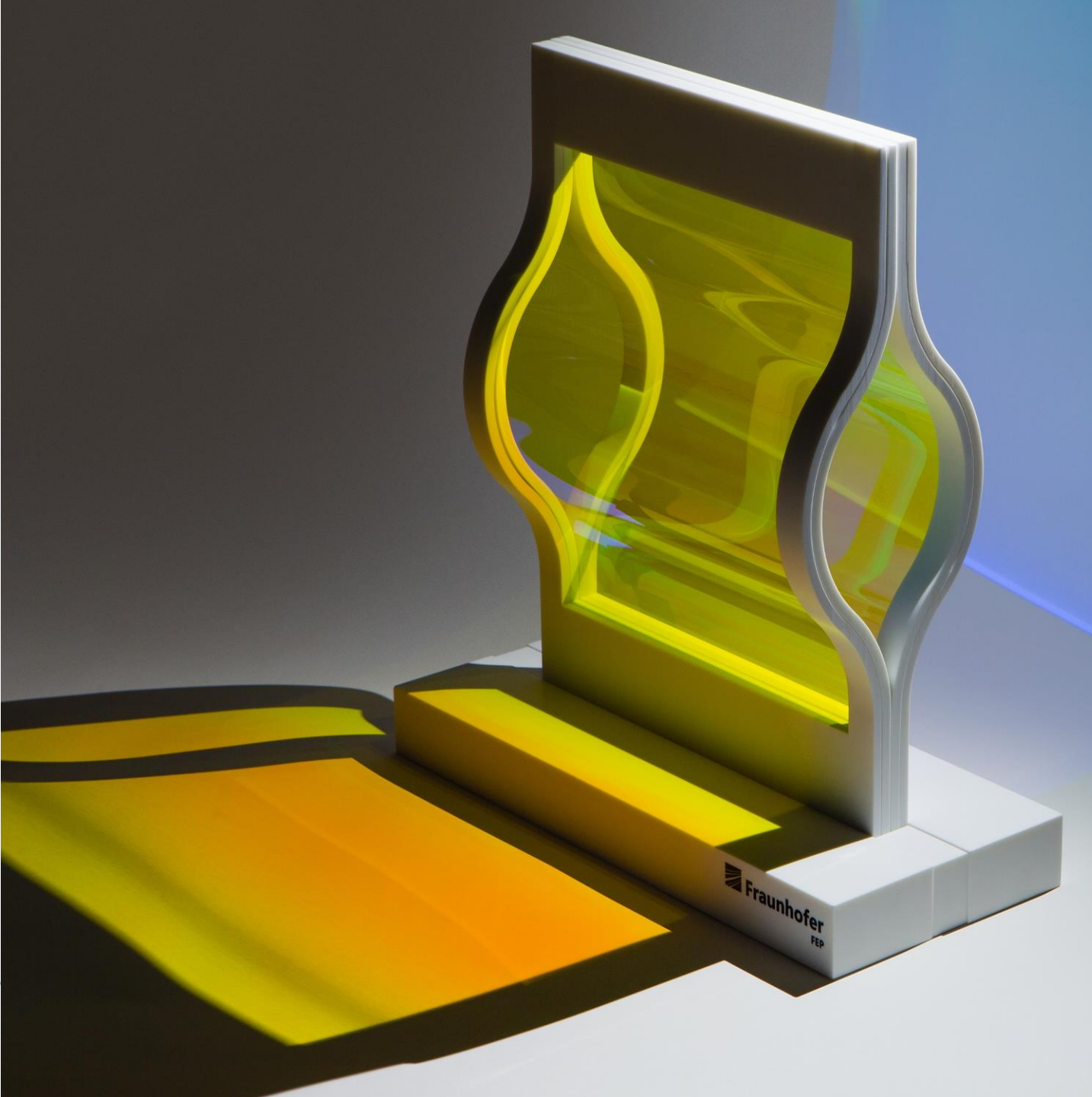
Successful non-linear simulation of the large-deformation test setup including mechanical contact



Maximum stress was underestimated when pure bending was assumed



Effective length of the new setup is advantageous compared to other existing setups



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Wiebke Langgemach

Fraunhofer FEP, Dresden

[wiebke.langgemach@fep.fraunhofer.de](mailto:wiebke.langgemach@fep.fraunhofer.de)