



3D Modelling of Flow Dynamics in Packed Beds of Low Aspect Ratio

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Aims To investigate 3D fluid flow heterogeneity in packed beds of low aspect ratios and to compare the results with those from with 2D modelling

Abstract Computer fluid dynamics (CFD) was used to investigate non-uniform structure flow distributions in packed bed reactors of low aspect ratios. Detailed knowledge of flow dynamics in terms of local structure of the packed bed, pressure drops and interstitial flow distributions was examined. The discrete element method was used to generate various packing configurations. The porosity profiles from the CFD simulation results were in a good agreement with the semi-analytical models, especially, in the vicinity of the wall. Similar oscillation trends with damping profiles towards the centre of the packed beds were observed. The discrepancies in regions towards the centre would be caused by the loose structure of the generated packing. The simulation results were validated by pressure drop measurements. Both experimental and simulation results fitted well Reichelt and Zhavoronkov models at high Reynolds numbers and these results clearly demonstrated that the generated packing exhibited pressure drops which were close to relevant models at low aspect ratios allowing further investigations of mass transfer and chemical reactions. Flow heterogeneity was investigated by radial distribution of the velocity. At high aspect ratios of packed bed, the velocity profile had a thin peak near the wall and a dumped profile towards the centre.

Packing generation by the Discrete Element Method

The overall setting parameters

- Wall parameters:
 - Normal stiffness coefficient, $kn = 1 \times 10^{13}$
 - Tangential stiffness coefficient, $ks = 1 \times 10^{13}$
 - Friction coefficient, $kfric = 0.2$;
- Particle parameters:
 - Normal stiffness coefficient, $kn = 2.5 \times 10^8$
 - Tangential stiffness coefficient, $ks = 2.5 \times 10^8$
 - Friction coefficient, $kfric = 0.2$
 - Density = 3.900

Update particle + wall positions and set of contacts

Law of Motion (applied to each particle) → resultant force + moment

Force-Displacement Law (applied to each contact) → relative motion + constitutive law

contact forces

Analysis of porosity profiles of the randomly generated packings

Domain index was allocated integer numbers of "zero" for the between particle domains and "unity" for all solid phase domains

The volumetric 3D data were reduced to 2D data by averaging along the angular coordinate: $\epsilon(r, z) = \frac{1}{2\pi} \int_0^{2\pi} \epsilon(r, \theta, z) d\theta$

The 2D surface data for each slice were reduced into 1D by averaging along the length (axial coordinate) of the packed bed: $\epsilon(r) = \frac{1}{L} \int_0^L \epsilon(r, z) dz$

Full packed bed radial porosity profiles along with literature models

Radial porosity profiles along with bed length (angular averaged)

Aspect ratio (AR) : 1.5 Aspect ratio (AR) : 3.0 Aspect ratio (AR) : 4.0

Results

Pressure drops by simulation and established models (Carman, Ergun, Zhavoronkov and Reichelt)

Velocity/pressure drops profiles

(a) 3D modelling (b) 2D structure based (c) 2D empirical based

(a) AR2 (b) AR3 (d) AR6 (f) AR9

Momentum balance

2D modeling (two missing data : porosity and/or porosity)

$$\rho_p u \cdot \nabla u = -\epsilon \nabla P + \mu \nabla \cdot \nabla u - \frac{2}{3} q u \cdot \nabla u + \epsilon F$$

$$\nabla \cdot (\rho_g u) = 0$$

$$F = -\frac{\mu u}{K} - \beta \rho u^2$$

$$K = \frac{\epsilon^3 dp^2}{A(1-\epsilon)^2}, \quad \beta = \frac{B(1-\epsilon)}{\epsilon^3 dp}$$

where $A = 150, B = 1.75$

$u|_{r=0} = u_0, \nabla u|_{r=1} = 0$
 $\nabla u|_{r=0} = 0$

1. Porosity by empirical models

$$\epsilon_c(r) = 1 - \pi [R_c^2 - a(r_c - r_{se})^2]$$

$$R_{se} = R_c^2 - \frac{a^2}{2}$$

with $a = 0.045 - 0.55e^{-0.1/d_p}$
 $r_c = \frac{(R_c r^2 - R_c^2) + R_c^2}{4a}$, $r_{se} = |r_c + R_c|$
 $r_c = br^2 + r' + R_c^2$, with $b = 0.037 - 2.0e^{-0.1/d_p}$

2. Porosity by angular (perimeter) averaging from 3D structures

3D modeling (no missing data but time computer power consuming)

$$\rho_p u \cdot \nabla u = -\nabla P + \mu \nabla \cdot \nabla u - \frac{2}{3} \mu \nabla \cdot \nabla u$$

$$\nabla \cdot (\rho_g u) = 0$$

$$u|_{r=0} = u_0, P|_{r=1} = P_0$$

Modelling of momentum, heat and mass balances in packed bed reactor (Pt/Alumina catalyst deactivation in CO oxidation)

Two-dimensional Modelling

Momentum balance in a homogenous porous medium

$$\rho_p u \cdot \nabla u = -\epsilon \nabla P + \mu \nabla \cdot \nabla u - \frac{2}{3} q u \cdot \nabla u + \epsilon F$$

$$\nabla \cdot (\rho_g u) = 0$$

$$F = -\frac{\mu u}{K} - \beta \rho u^2$$

$$K = \frac{\epsilon^3 dp^2}{A(1-\epsilon)^2}, \quad \beta = \frac{B(1-\epsilon)}{\epsilon^3 dp}$$

where $A = 150, B = 1.75$
 $u|_{r=0} = u_0, \nabla u|_{r=1} = 0$
 $\nabla u|_{r=0} = 0$

Deactivation model

$$\frac{dc}{dt} = A_0 e^{-E_a/RT} c_{CO}$$

Heat balance (both gas and solid phases)

$$\epsilon \rho_g c_p u \cdot \nabla T + (1-\epsilon) \rho_s c_p \frac{\partial T}{\partial t} + \epsilon \rho_g c_p u \cdot \nabla T = \nabla \cdot (k \nabla T) + Q$$

$$\rho_s c_p \frac{\partial T}{\partial t} = \nabla \cdot (k_s \nabla T) + Q$$

$$k = \Delta T_{cr}$$

Mass balance (both gas and solid phases)

$$\frac{\partial c}{\partial t} + \nabla \cdot (-D_s \nabla c) + u \cdot \nabla c = 0$$

$$\frac{\partial c_s}{\partial t} + \nabla \cdot (-D_s \nabla c_s) = R$$

$$\nabla c|_{r=0} = 0$$

$$R = a A e^{E_a/RT} c_{CO}$$

Three-dimensional Modelling

1. Momentum balance

$$\rho_p u \cdot \nabla u = -\epsilon \nabla P + \mu \nabla \cdot \nabla u - \frac{2}{3} q u \cdot \nabla u + \epsilon F$$

$$\nabla \cdot (\rho_g u) = 0$$

$$u|_{r=0} = u_0, P|_{r=1} = P_0$$

2. Mass balance

2.1. in the gaseous phase

$$\frac{\partial c}{\partial t} + \nabla \cdot (-D_s \nabla c) + u \cdot \nabla c = 0$$

2.2. in the catalytic phase

$$\frac{\partial c_s}{\partial t} + \nabla \cdot (-D_s \nabla c_s) = R$$

3. Heat balance in the gas phase

3.1. Heat balance in the gas phase

$$\epsilon \rho_g c_p u \cdot \nabla T + \rho_g c_p u \cdot \nabla T = \nabla \cdot (k \nabla T) + Q$$

3.2. in the catalytic phase

$$\rho_s c_p \frac{\partial T}{\partial t} = \nabla \cdot (k_s \nabla T) + Q$$

4. Deactivation rate

$$\frac{dc}{dt} = A_0 e^{E_a/RT} c_{CO}$$

Local deactivation results

Activity coefficient profiles

Activity Coefficient

z/L

2D modelling (empirical models of porosity and diffusion)

2D modelling (structure based porosity and diffusion)

3D modelling

YD=13 YD=15 YD=17

dimensionless activation energy of deactivation

Conclusions

- This work used the 3D CFD modelling to investigate non uniform (local) deactivation in packed bed reactors of low AR under dynamic operations.
- The modelling was justified by pressure drops tests and *in situ* sampling by moving capillary and mass spectrometry
- Good agreements in terms of pressure drops and porosity profiles with established models
- 2D modelling based on averaged distribution structures of 3D modelling is promising approach to substitute large computation consuming 3D modelling.

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