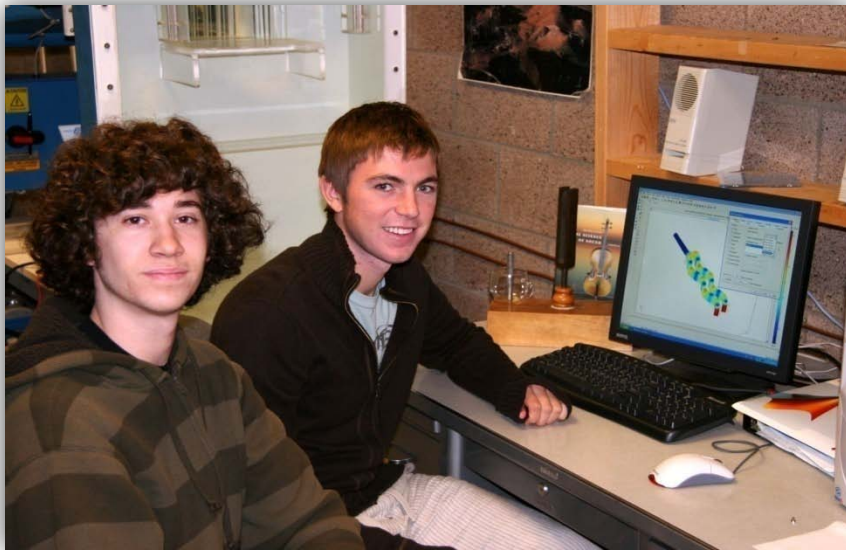


Resonating with Students in the Undergraduate Physics Laboratory: *Comprehending Acoustic Vibrations*



Keith Stein
Bethel University
St. Paul, Minnesota

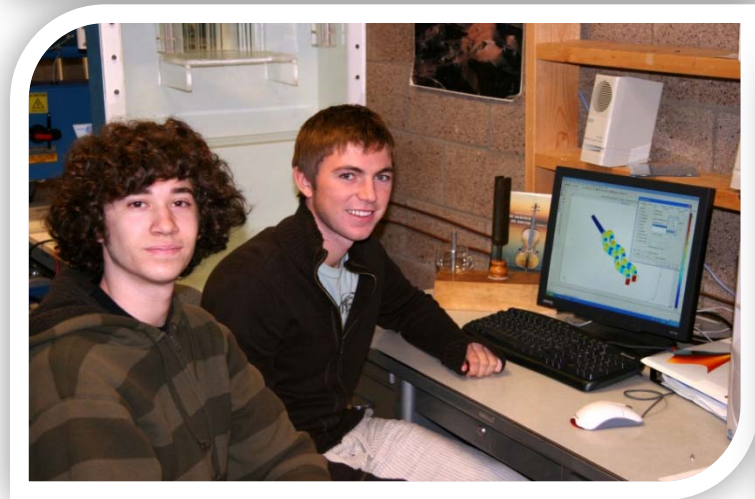
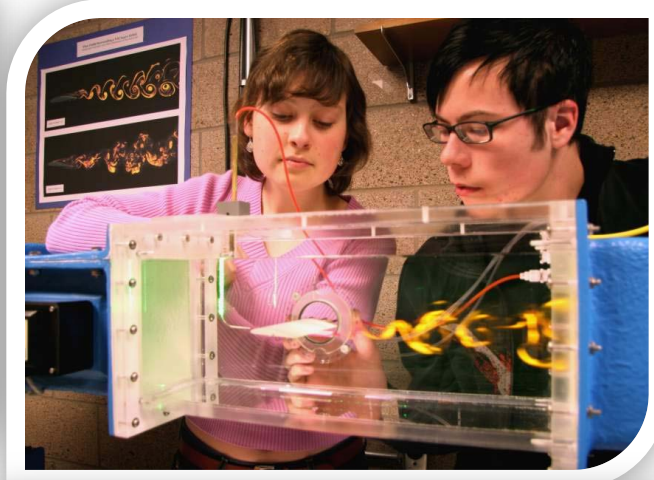


Outline

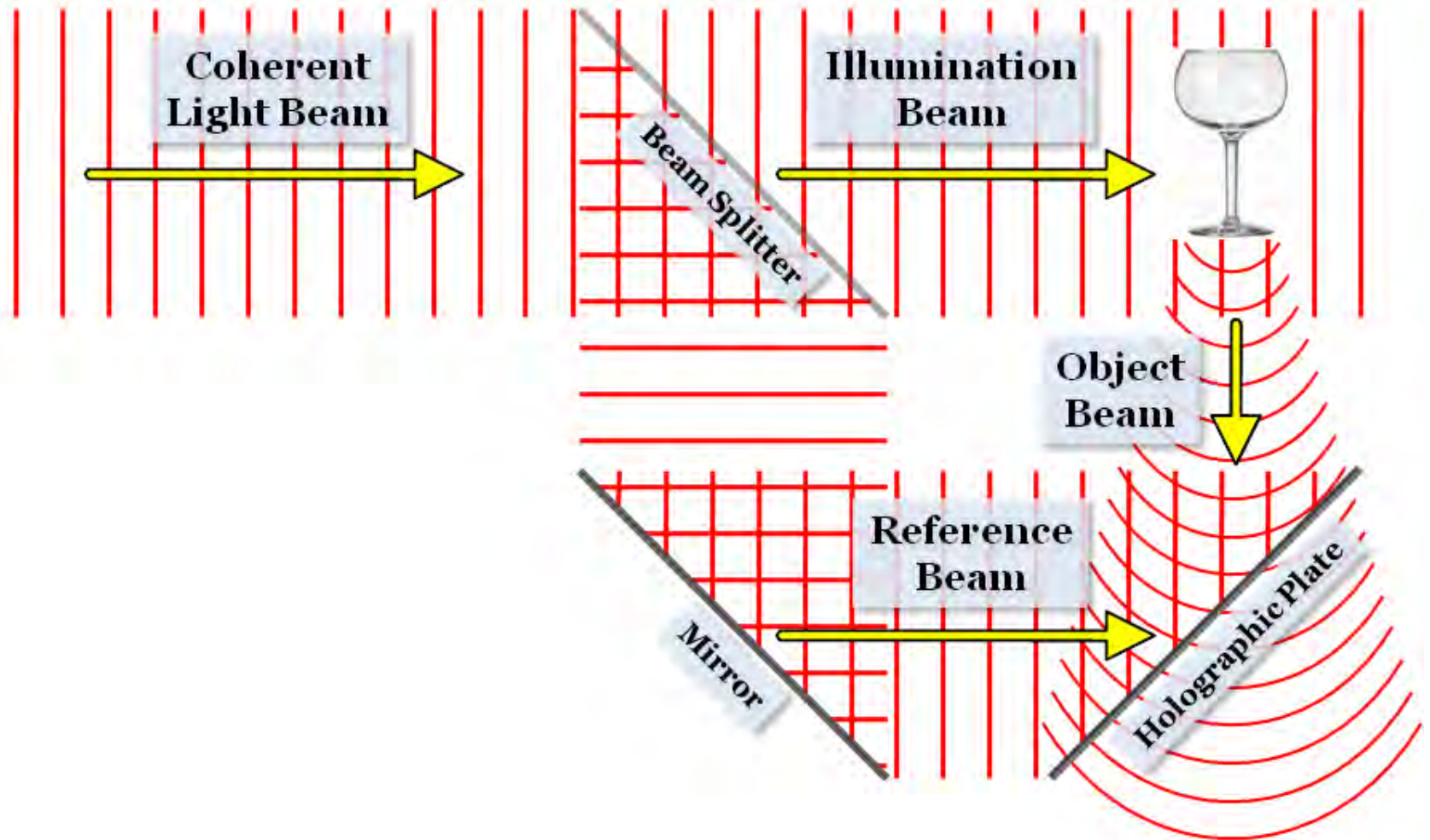
- **Introduction: The Advanced Lab Concept**
- **Approach**
 - **Optical Diagnostics: Stroboscopic Holography**
 - **Computational Modeling: COMSOL Eigenfrequency Analysis**
- **Examples**
 - **Vibrational Modes of a Handbell**
 - **Vibrational Modes of a Coffee Cup**
 - **Vibrational Modes of a Tuning Fork**
- **Concluding Remarks**

Introduction:

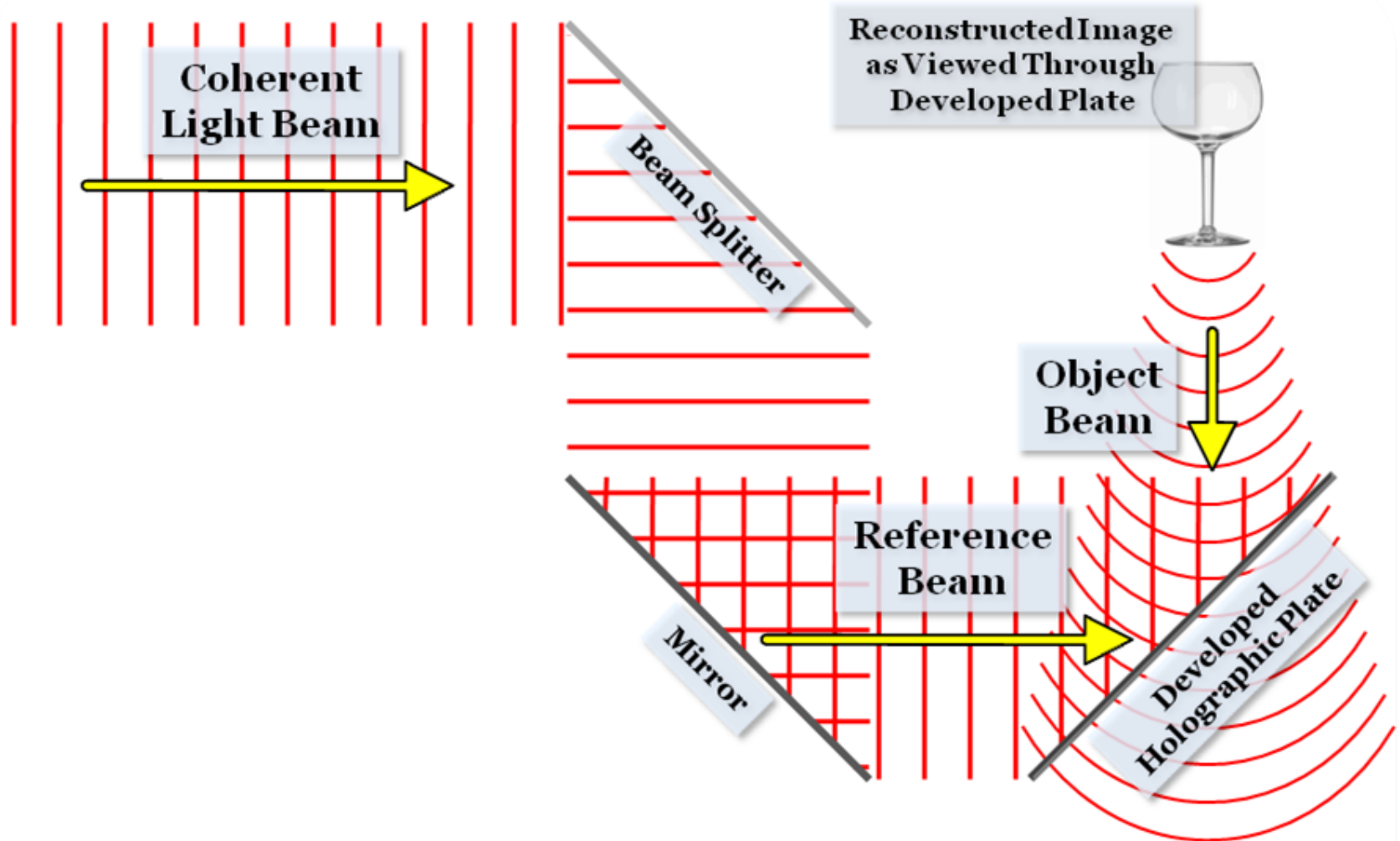
The Advanced Lab Concept



Optical Diagnostics Approach: *Real-time Stroboscopic Holography*

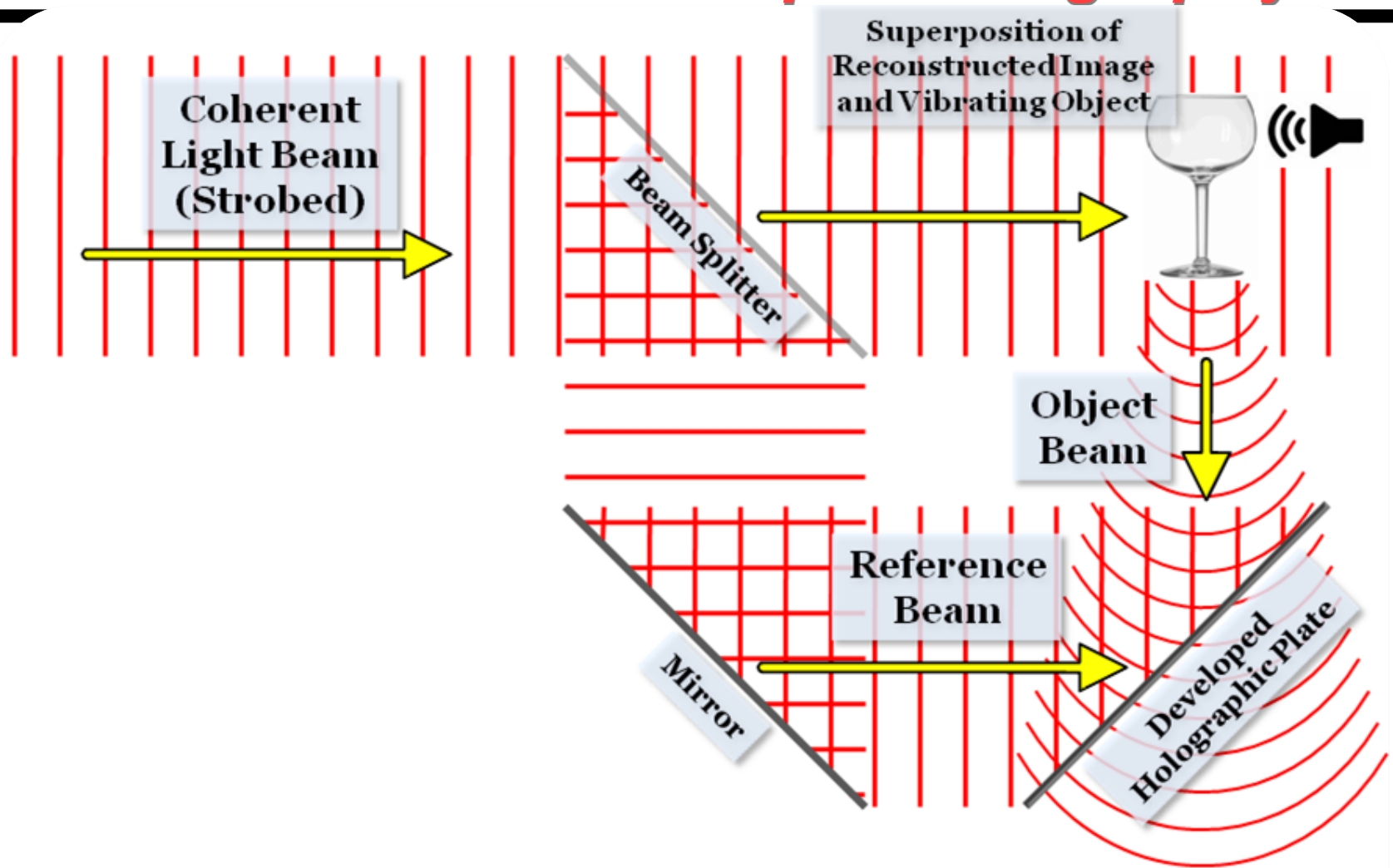


Optical Diagnostics Approach: *Real-time Stroboscopic Holography*



Viewing of Reference Hologram

Optical Diagnostics Approach: *Real-time Stroboscopic Holography*



Stroboscopic Viewing

Computational Approach:

COMSOL Eigenfrequency Analysis

➤ Eigenvalue Analyses

- Linear Elasticity
- Undamped vibrations
- Three objects
 - Handbell
 - Coffee Cup
 - Tuning Fork

$$\rho \frac{\partial^2 \bar{\mathbf{u}}}{\partial t^2} - \nabla \cdot \bar{\boldsymbol{\sigma}} = \bar{\mathbf{F}}$$

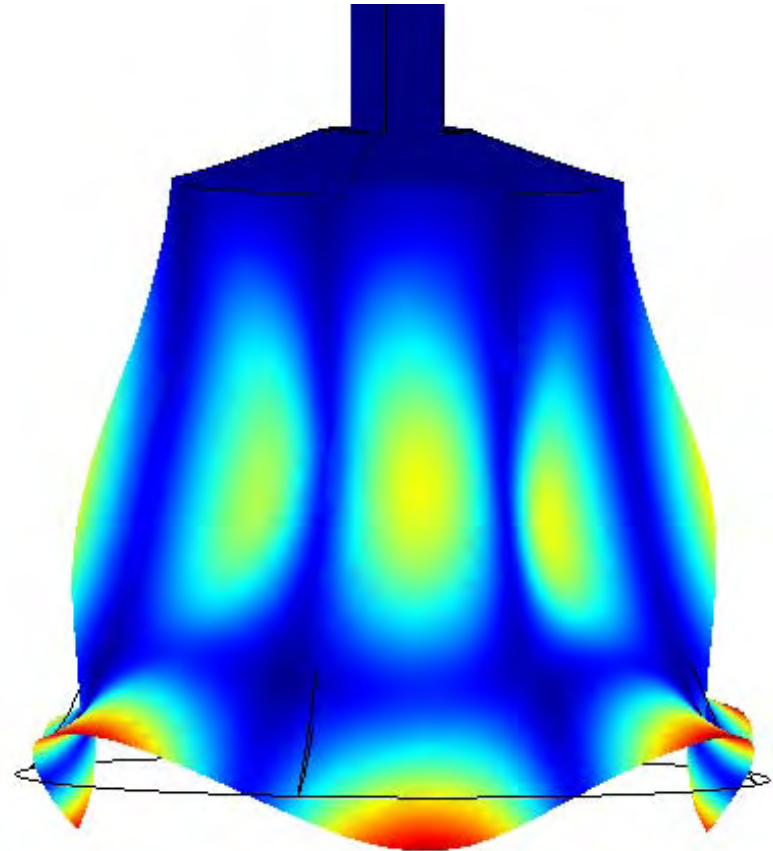
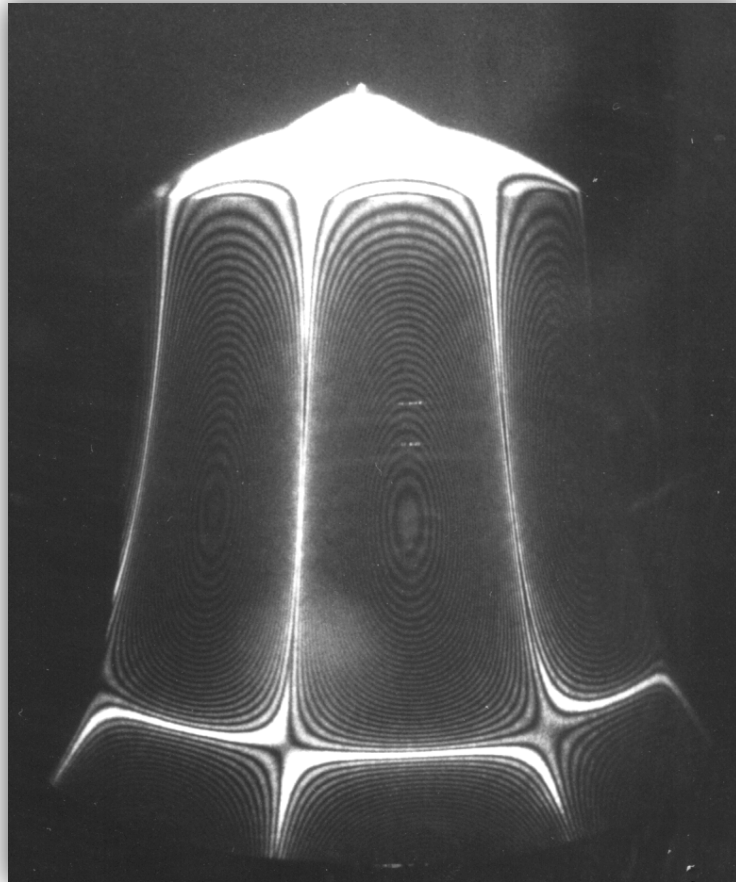
$$\bar{\mathbf{M}} \ddot{\bar{\mathbf{x}}} + \bar{\mathbf{K}} \bar{\mathbf{x}} = \bar{\mathbf{0}}$$

$$\left(\bar{\mathbf{A}} - \lambda \bar{\mathbf{I}} \right) \bar{\mathbf{X}} = \bar{\mathbf{0}}$$

$$\lambda = 4\pi^2 f^2$$

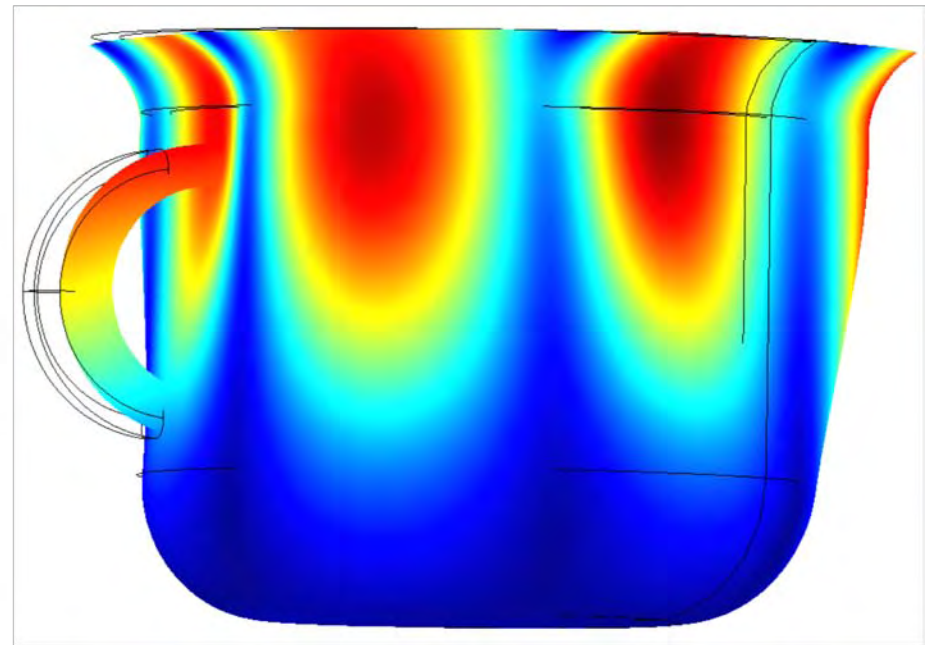
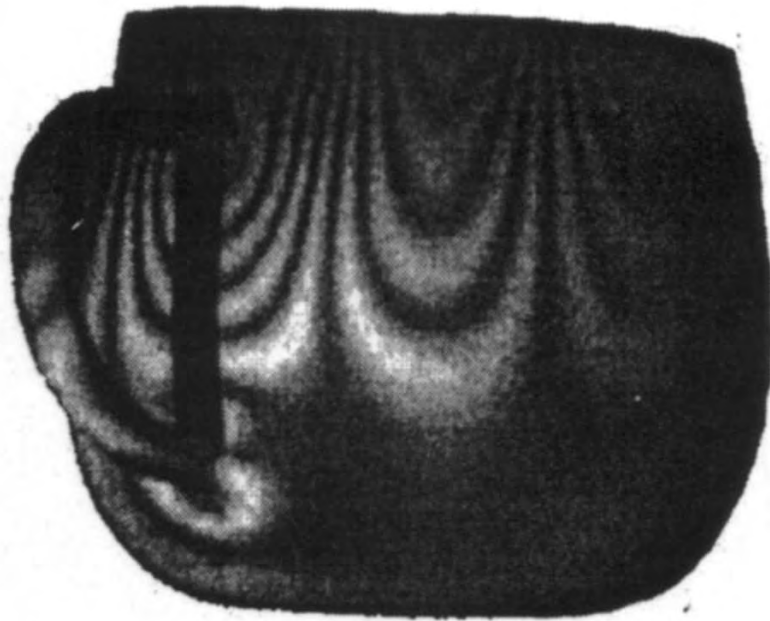
Results:

Vibrational Modes of a Handbell



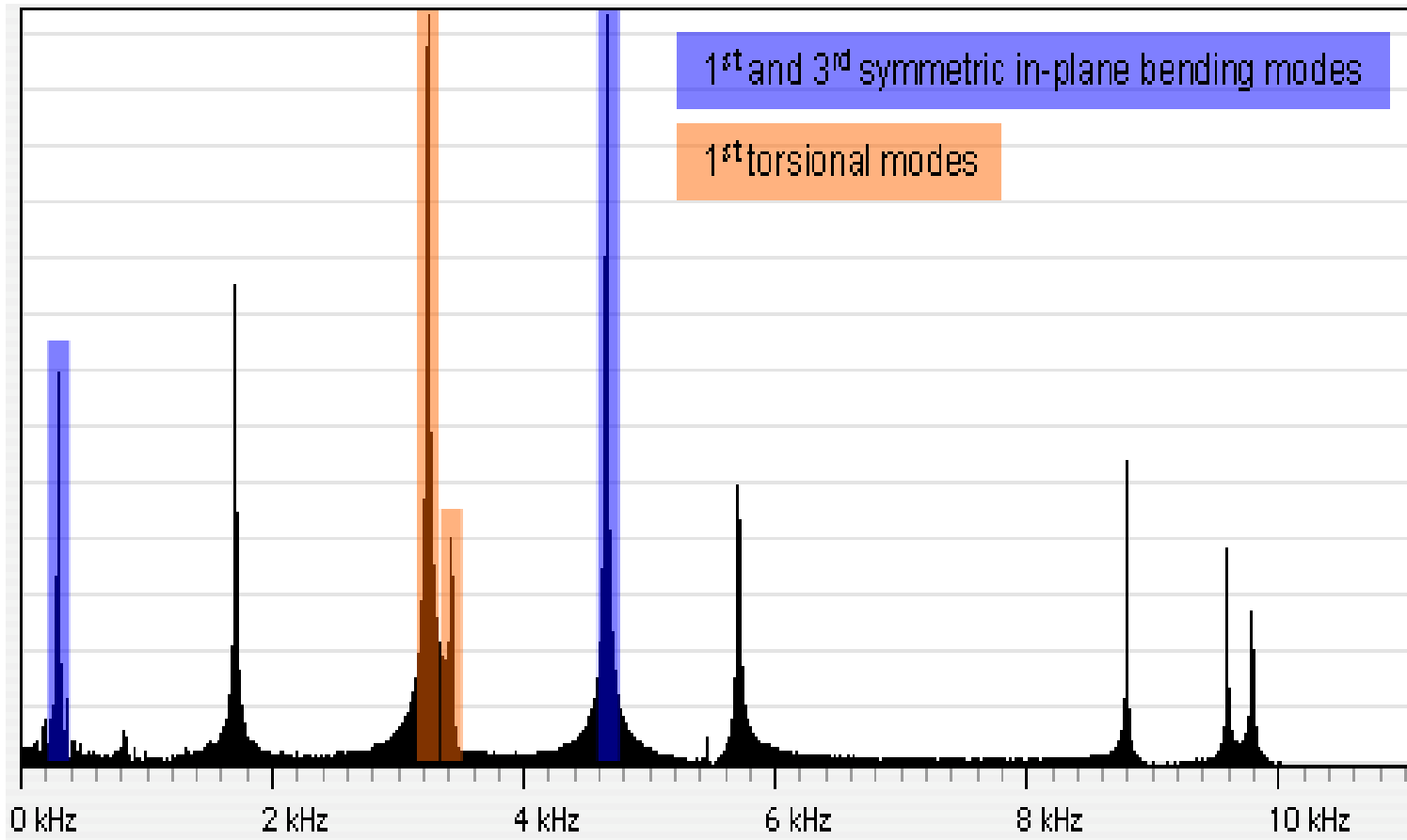
Results:

Vibrational Modes of a Coffee Cup



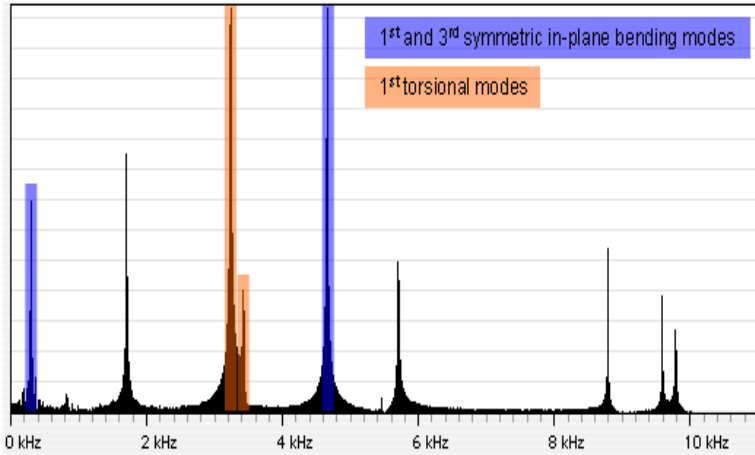
Results:

Vibrational Modes of a Tuning Fork



Results:

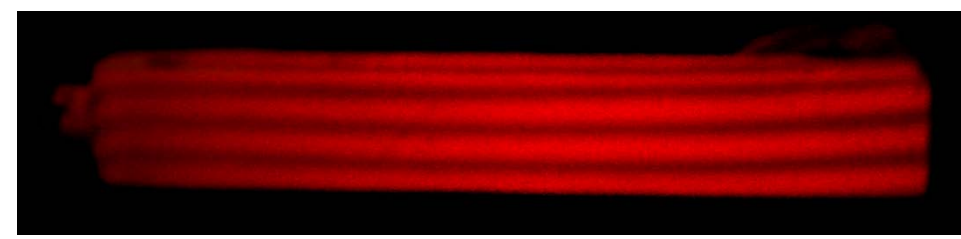
Vibrational Modes of a Tuning Fork



1st in-plane symmetric mode



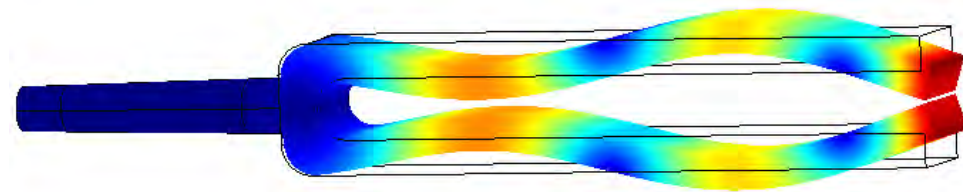
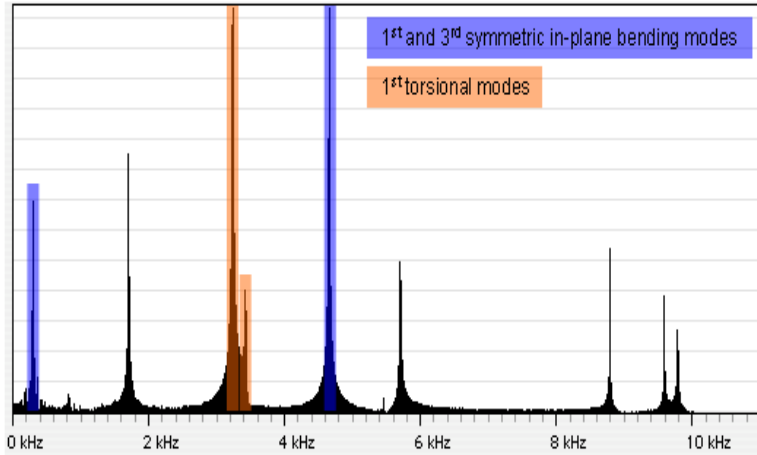
COMSOL (278 Hz)



Stroboscopic Holography (273 Hz)

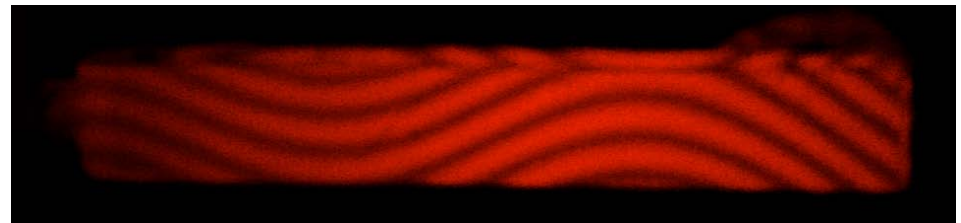
Results:

Vibrational Modes of a Tuning Fork



COMSOL (4560 Hz)

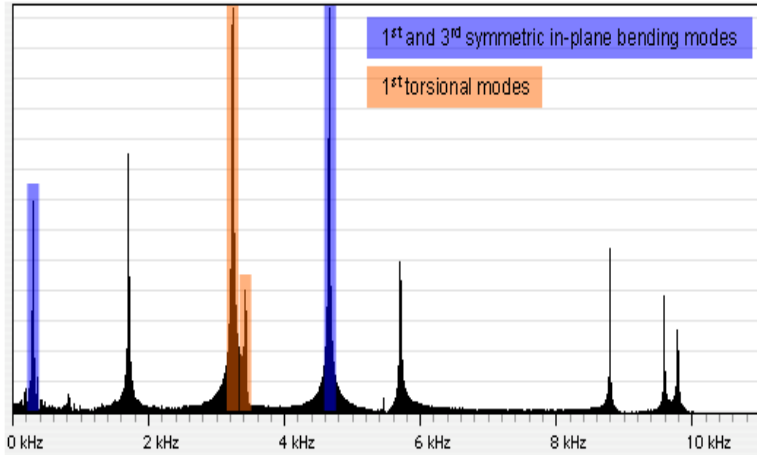
3rd in-plane symmetric mode



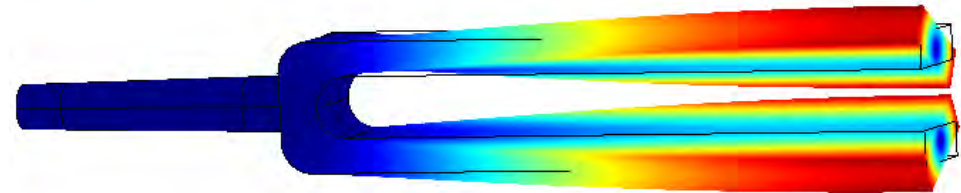
Stroboscopic Holography (4647 Hz)

Results:

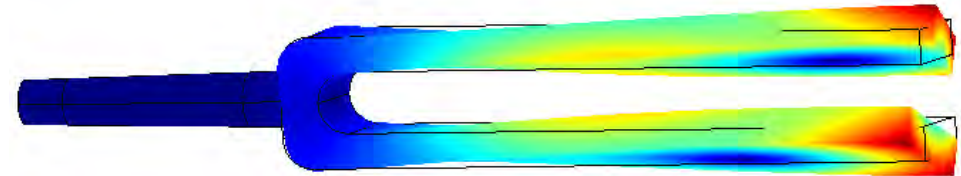
Vibrational Modes of a Tuning Fork



1st torsional modes



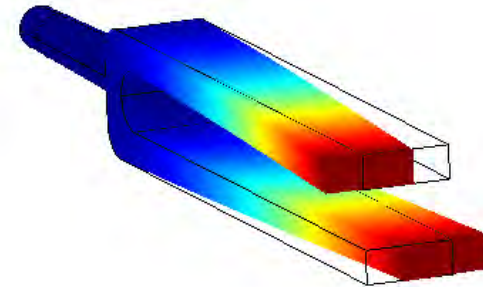
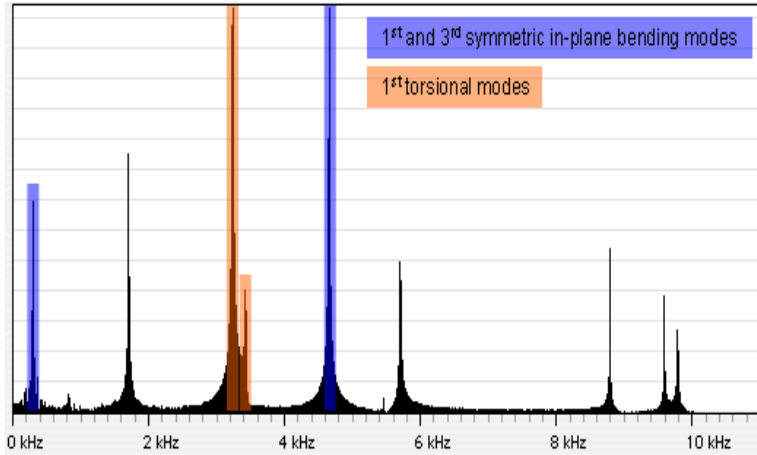
Out-of-phase torsional mode (3240 Hz)



In-phase torsional mode (3462 Hz)

Results:

Vibrational Modes of a Tuning Fork



COMSOL (582 Hz)

↑
?
1st out-of plane bending mode



Stroboscopic Holography (530 Hz)

Concluding Remarks

- COMSOL and optical diagnostics can serve as complementary tools in the undergraduate advanced laboratory.
- Together, COMSOL and optical diagnostics can provide students of applied physics, optics, and engineering with a fuller and richer understanding of acoustic vibrations.
- COMSOL can serve to illuminate aspects of acoustic vibrations that might be overlooked by purely experimental approaches (and vice versa).