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Electro-Optics Center

*A Manufacturing Technology Center of Excellence*

# **Three-Dimensional Simulation of Signal Generation in Wide- Bandgap Semiconductor Radiation Detectors**

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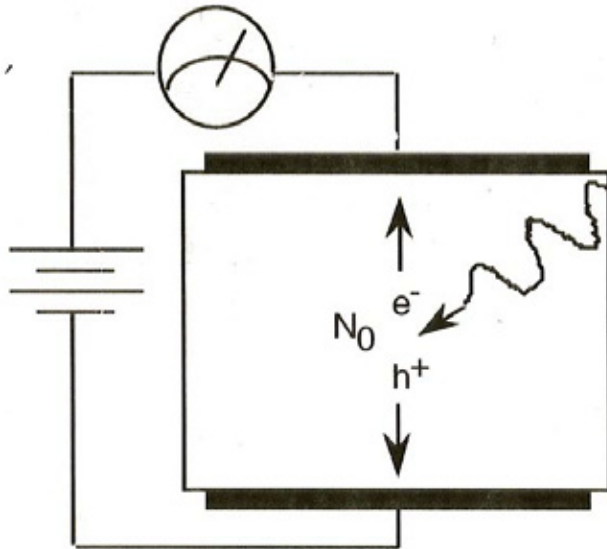
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# Outline



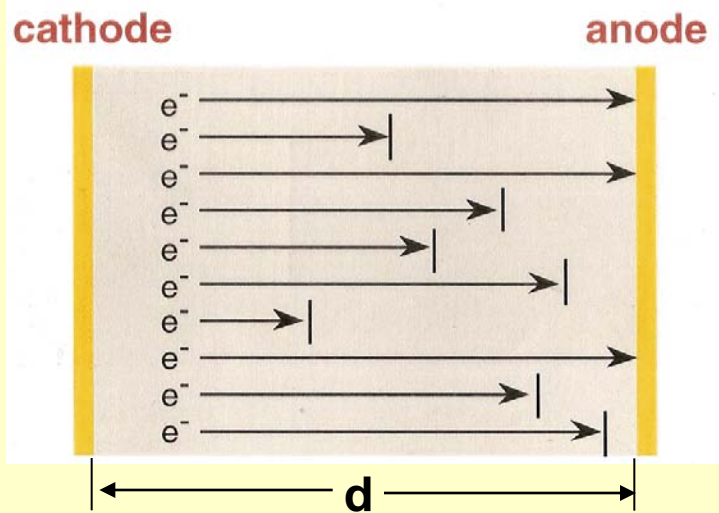
- Operation of a semiconductor radiation detector
- Hole tailing and the need for special electrode configurations
- Comsol-Matlab model
- Planar vs. Quasi-hemispherical detectors

# Semiconductor Radiation Detector Geometry



- A bias voltage is applied to the detector.
- Interaction creates  $N_0$  electron-hole pairs, proportional to the energy deposited by the photon.
- The charge carriers move to the electrodes, inducing a current.
- The integrated current should be  $qN_0$ .

# Signal Generation in a Semiconductor Detector



$$N(t) = N_0 e^{-t/\tau_e} \quad \leftarrow \text{trapping}$$

$$I_e(t) = e\mu_0 EN(t)/d \quad \leftarrow \text{Application of Ramo's theorem}$$

$$Q_e = \int_0^{t_{ce}} I_e(t) dt$$

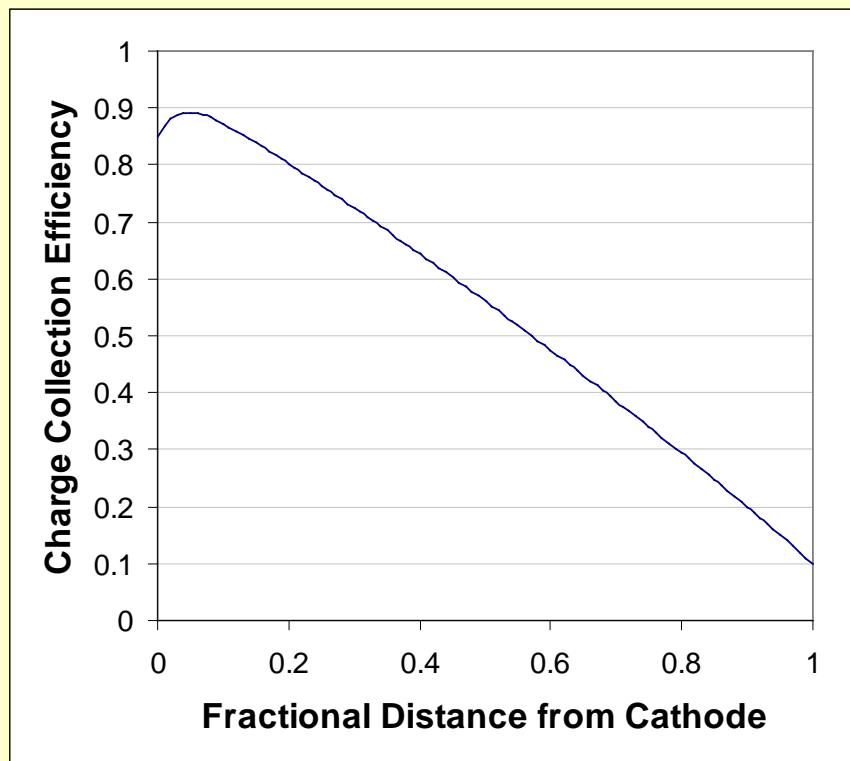
Putting these 3 equations together and adding the hole contribution gives the Hecht relation:

$$Q = \frac{qN_0E}{d} \left[ (\mu\tau)_e \left( 1 - e^{-(d-x_0)/(\mu\tau)_e E} \right) + (\mu\tau)_h \left( 1 - e^{-x_0/(\mu\tau)_h E} \right) \right]$$

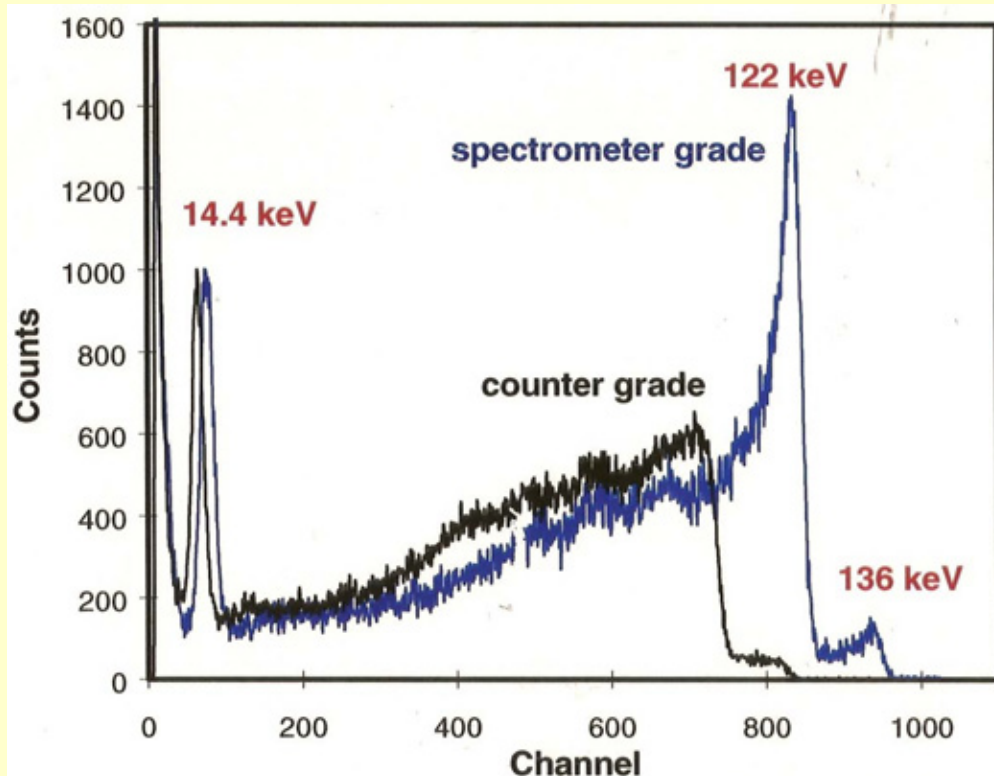


# "Hole Tailing" in Wide-Bandgap Semiconductors

Typical charge collection profile from Hecht relation



$^{57}\text{Co}$  spectra for two CdZnTe detectors  
 $10\times 10\times 3\text{ mm}^3$



# Electrode Designs to Correct for Hole Tailing



Various ways to weight signal induction towards the anode:

- Coplanar Grid
  - Subtract signals from two interdigitated electrodes
  - Need two preamplifiers plus differencing amp
- Segmented
  - “Small-pixel effect”
  - Need a separate amplifier for each pixel or strip
- Guard Ring Structures
  - “Frisch grid” to shield the anode
- Coaxial
  - Machine crystal into cylindrical shape and drill a hole through the center
- Quasi-hemispherical

# Signal Generation for Arbitrary Electrode Configurations

*General Form of Ramo's Theorem*

$$i(t) = q \mathbf{v} \cdot \mathbf{E}_1 \quad (\mathbf{E}_1 = \text{"weighting field"})$$

*Constant Mobility Approximation*

$$\mathbf{v} = \mu_{e(h)} \mathbf{E}$$

*Constant Trapping Lifetime, No De-trapping*

$$q(t) = q_0 e^{-t/\tau_{e(h)}}$$

*Put it all together*

$$\frac{Q_{e(h)}}{eN_0} = \int_0^{t_{c,e(h)}} \mu_{e(h)} e^{-t/\tau_{e(h)}} \vec{E} \cdot \vec{E}_1 dt$$

# Comsol Radiation Detector Model

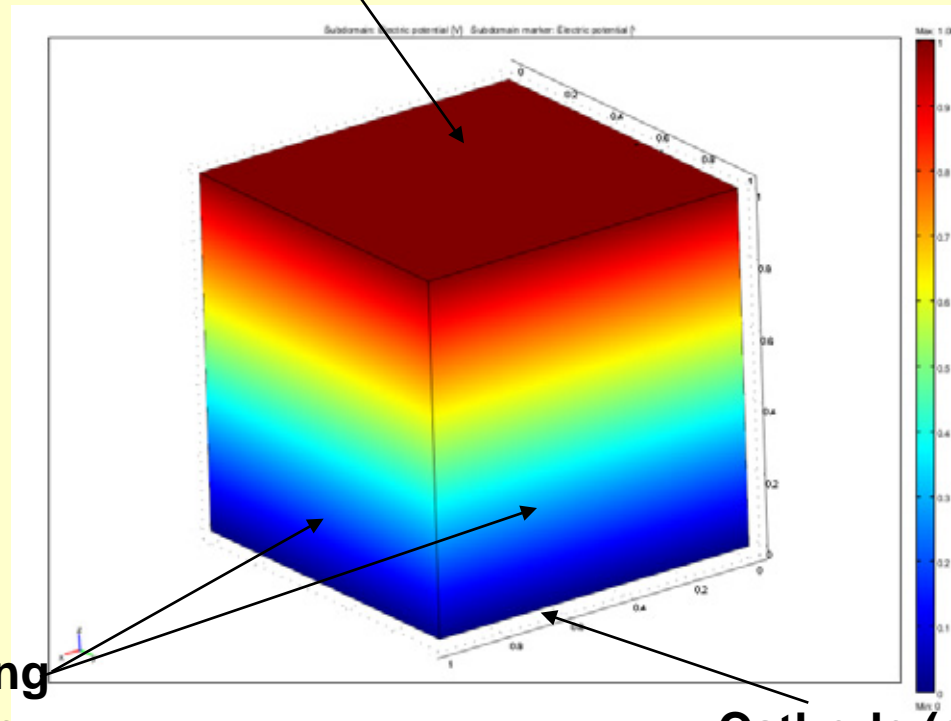


- Electrostatics with Conductive Media application mode to compute electric fields
- Export FEM structure to Matlab
- Integrate induced current in Matlab to compute charge collection efficiency as a function of interaction point
- Repeat for numerous interaction points to get a charge collection profile



# FEM Model for Planar Detector

Anode (applied bias)



Insulating surfaces

Cathode (grounded)

For the case of two electrodes, one grounded, the physical and weighting fields are the same except for a factor of the bias voltage.

# Integration of Electron/Hole Currents



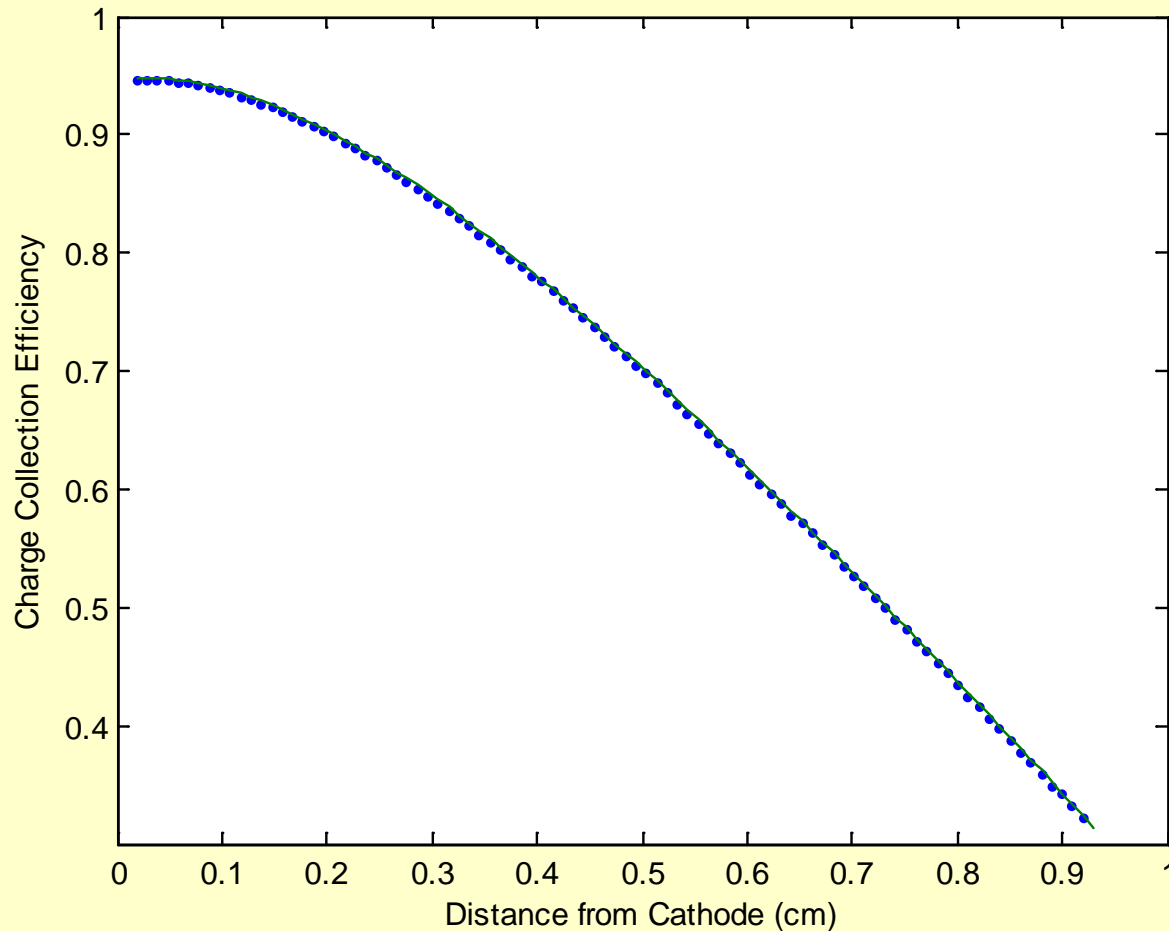
- Discretize the integral
- Take constant-distance jumps for better efficiency
- Repeat until a boundary is reached
- Compute electron and hole contributions separately and add

$$\frac{Q_{e(h)}}{eN_0} = \sum \mu_{e(h)} e^{-t_i/\tau_{e(h)}} \vec{E}(\vec{r}_i) \cdot \vec{E}_1(\vec{r}_i) \Delta t_i$$

$$\Delta t_i = \frac{\Delta r}{\mu_{e(h)} |\vec{E}(\vec{r}_i)|}$$

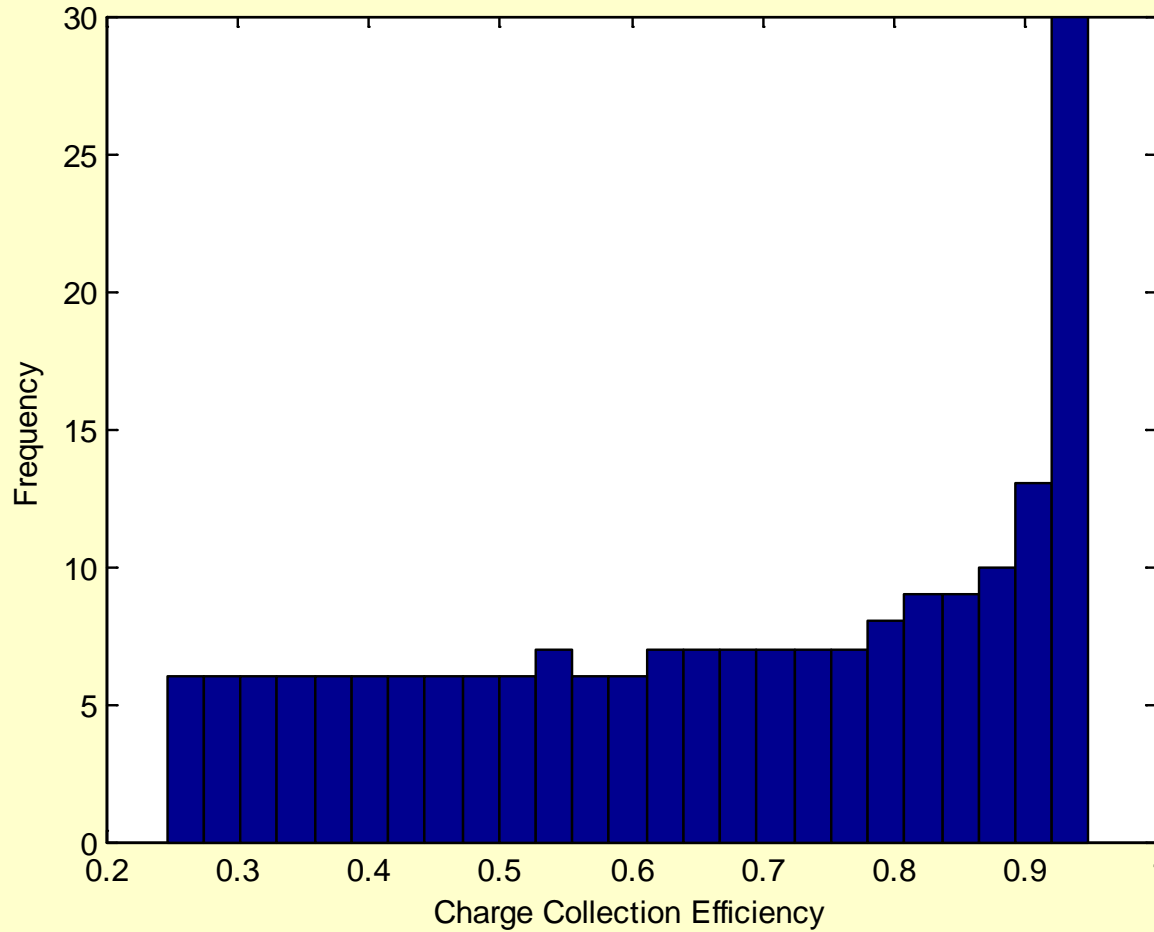
$$\Delta \vec{r}_i = \mu_{e(h)} \vec{E}(\vec{r}_i) \Delta t_i$$

# Charge Collection Profile for Planar Detector



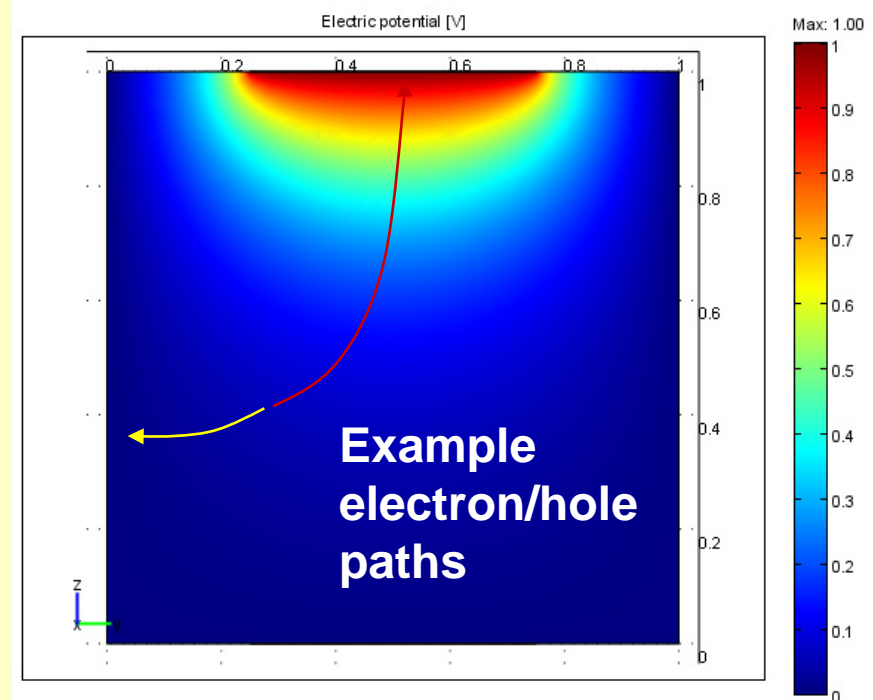
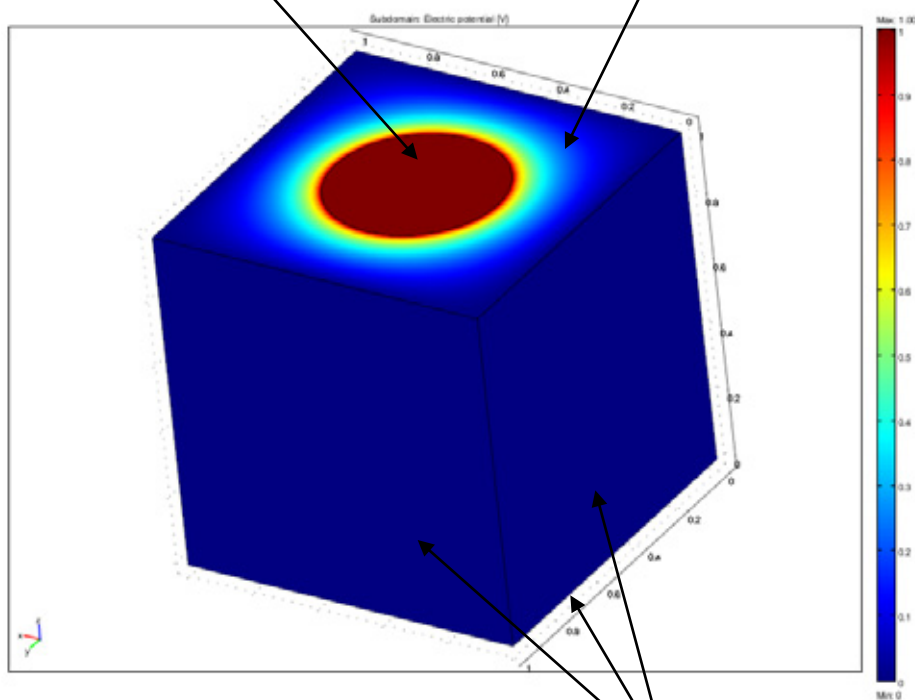
- Comsol-Matlab model
- Hecht equation

# Charge Collection Histogram for Planar Case



# FEM Model for Quasi-Hemispherical Detector

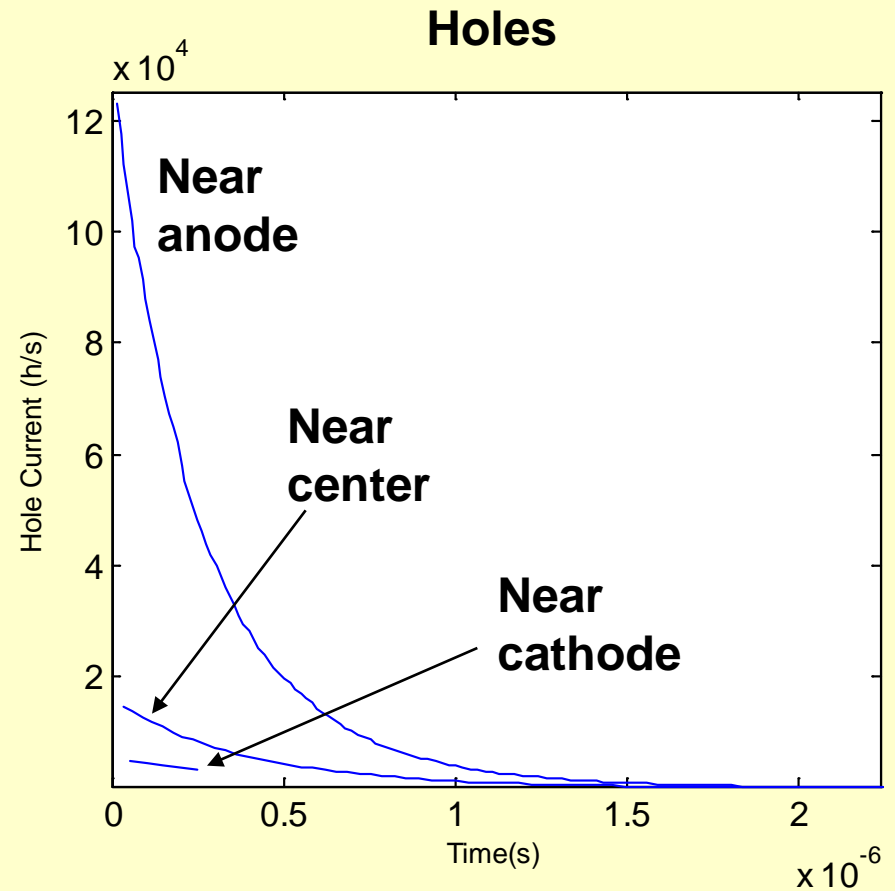
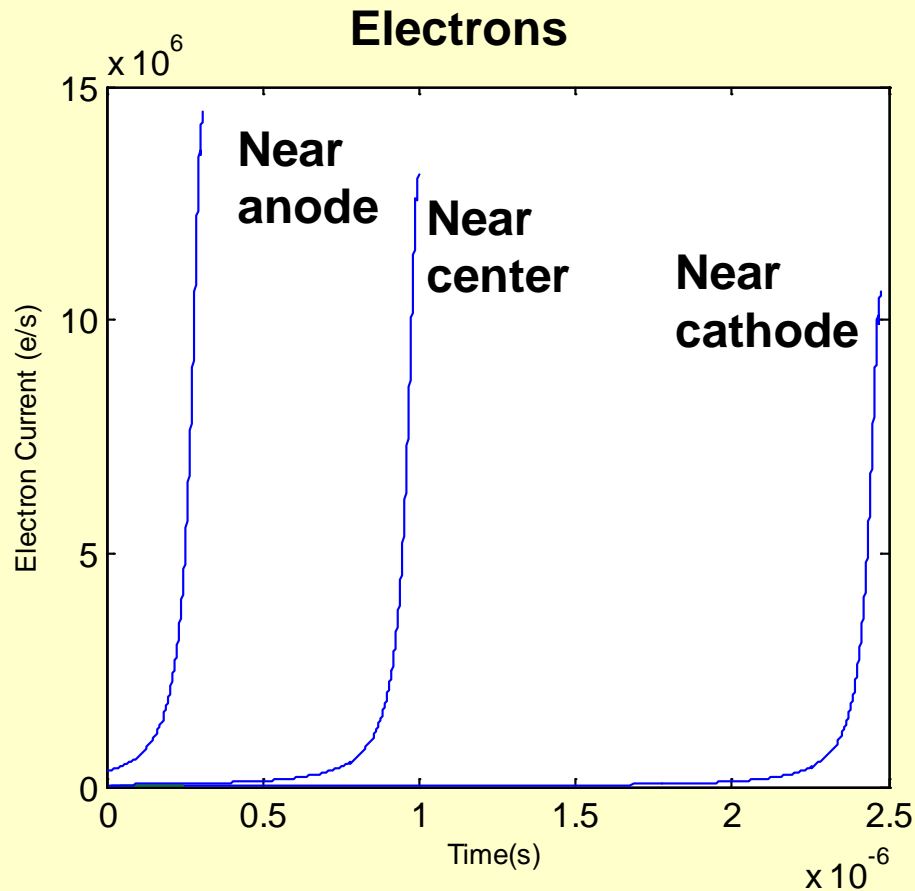
Anode (applied bias)    Insulating surface    X-Z Section of Equipotential Map



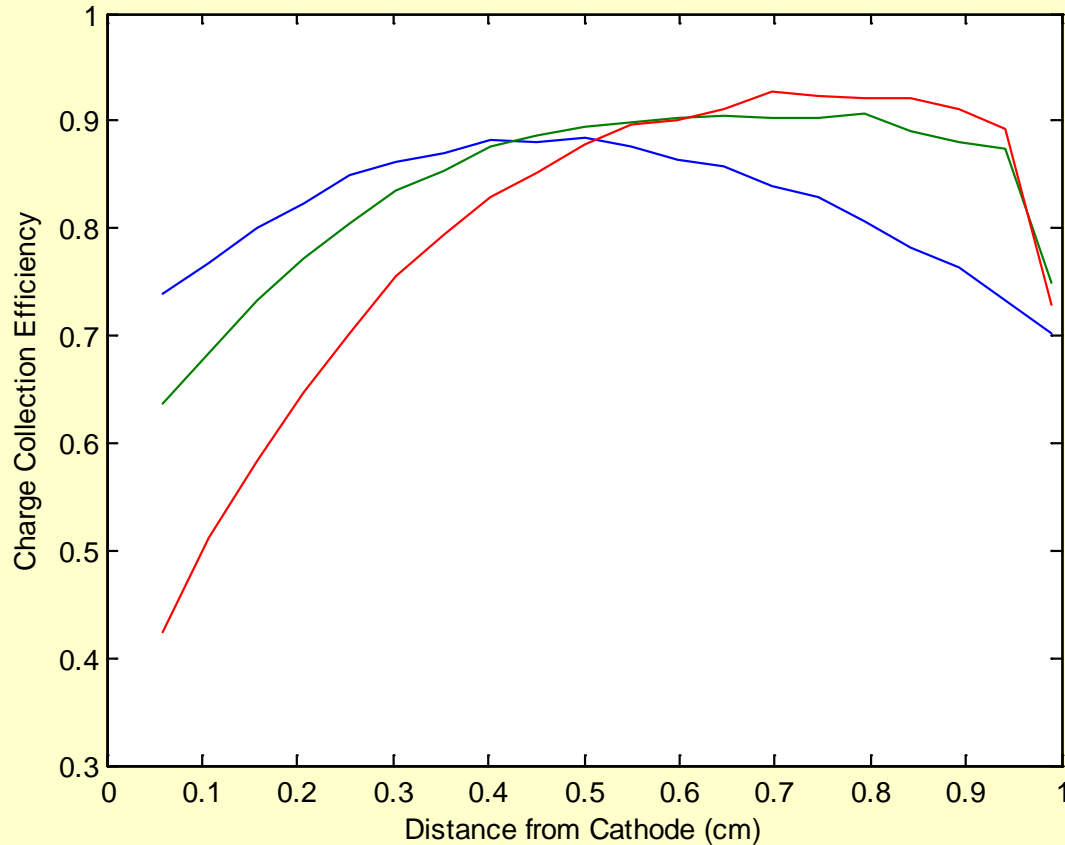
Cathode (grounded)



# Electron and Hole Current Waveforms



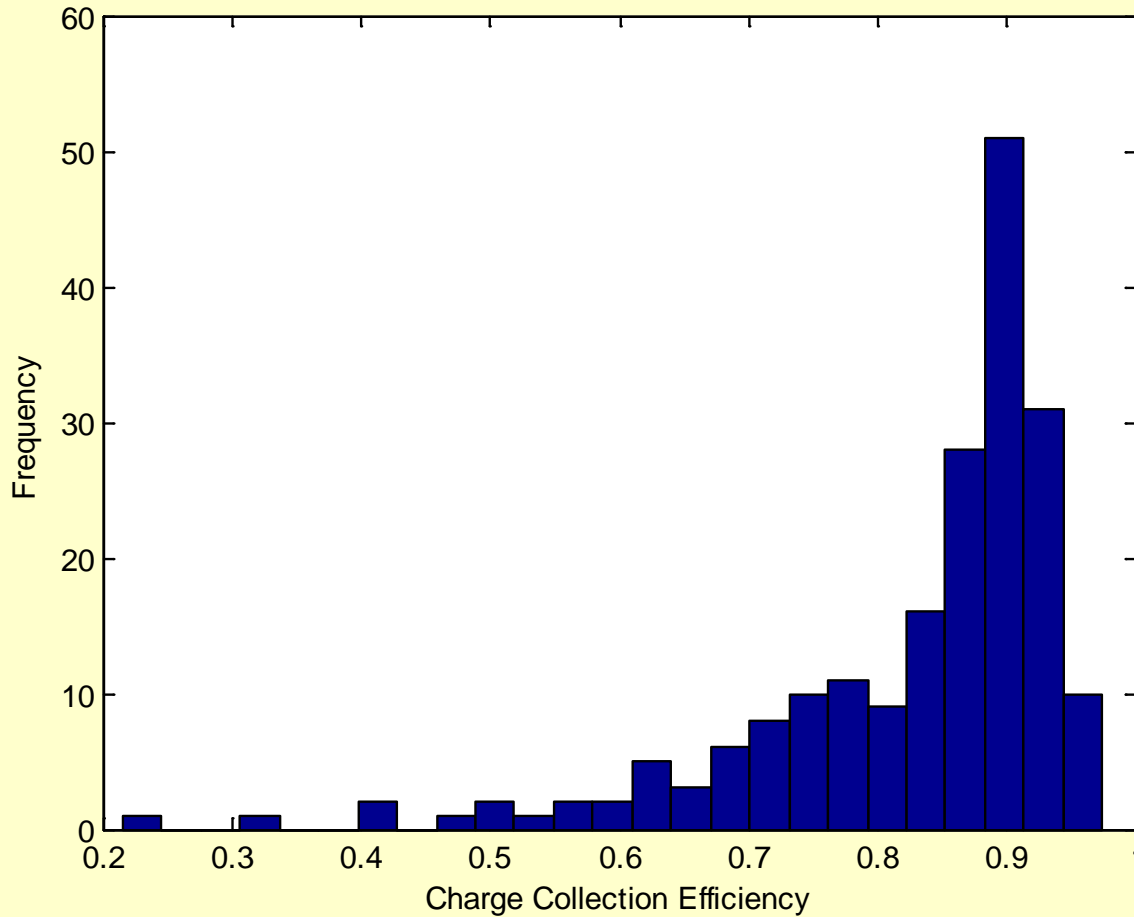
# Charge Collection Profiles Quasi-Hemispherical Case



- Center Line of Crystal
- Near Edge of Anode
- Near Corner of Crystal

# Charge Collection Histogram Quasi-Hemispherical

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# Conclusions



- Comsol Multiphysics with Matlab can easily compute signal generation in semiconductor detectors with arbitrary electrode configurations.
- Quasi-hemispherical detector can improve energy resolution and photopeak efficiency in compound semiconductor detectors without grid bias or multiple readout amplifiers.

# Thank You!



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