



Presented at the COMSOL Conference 2009 Milan

# Virtual Experiments: Numerical Computations as a Powerful Tool for Engineers

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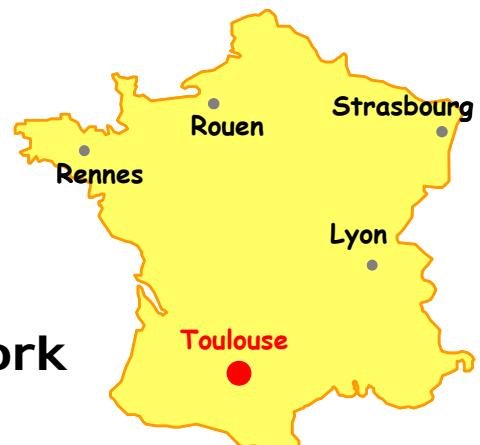
# INSA: National Institute of Applied Sciences



## In Toulouse

- 2100 Students
- 500 Graduates each year
- More than 500 Foreign Students
- 223 Permanent Academic Staff
- 10 Engineering Specialities
- 9 Research Laboratories

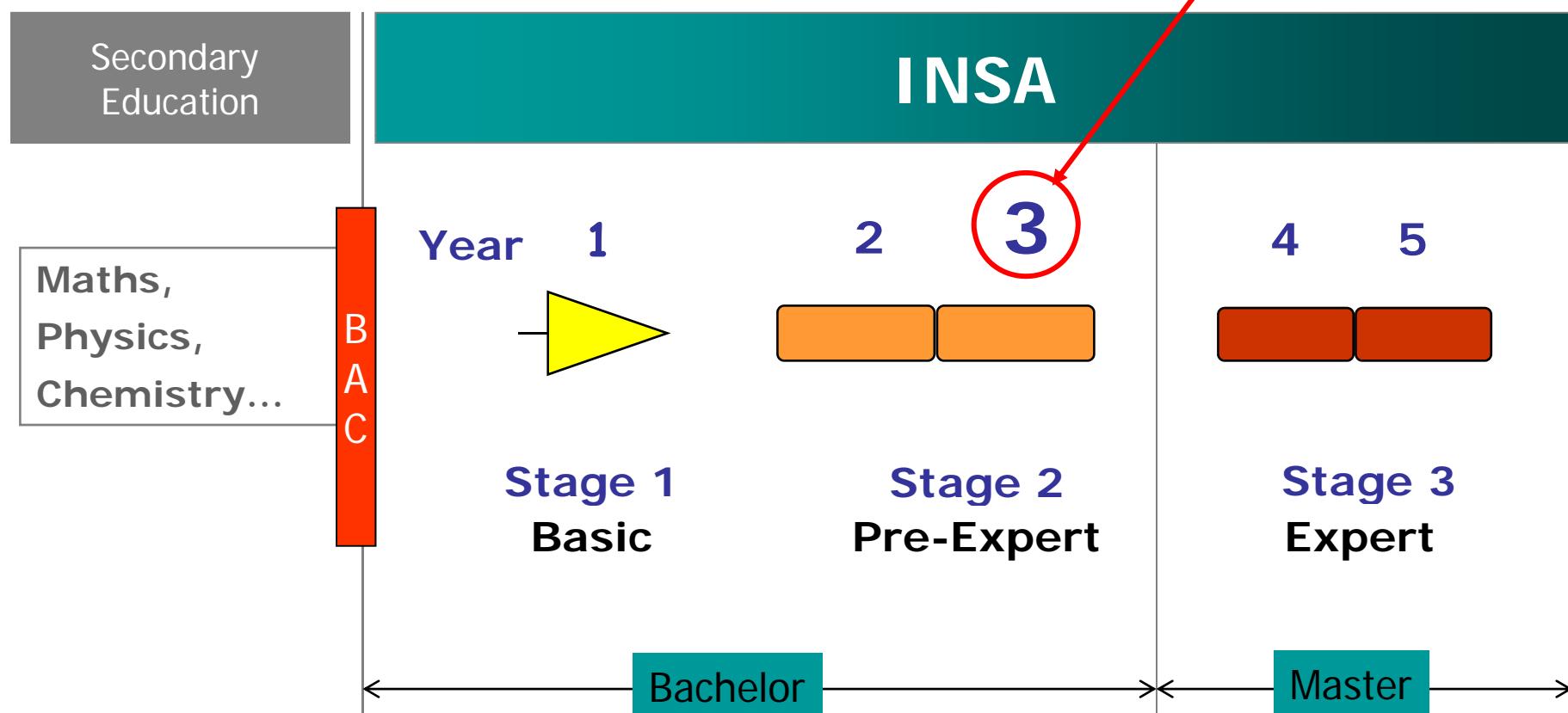
## INSA Network





# INSA Toulouse Teaching

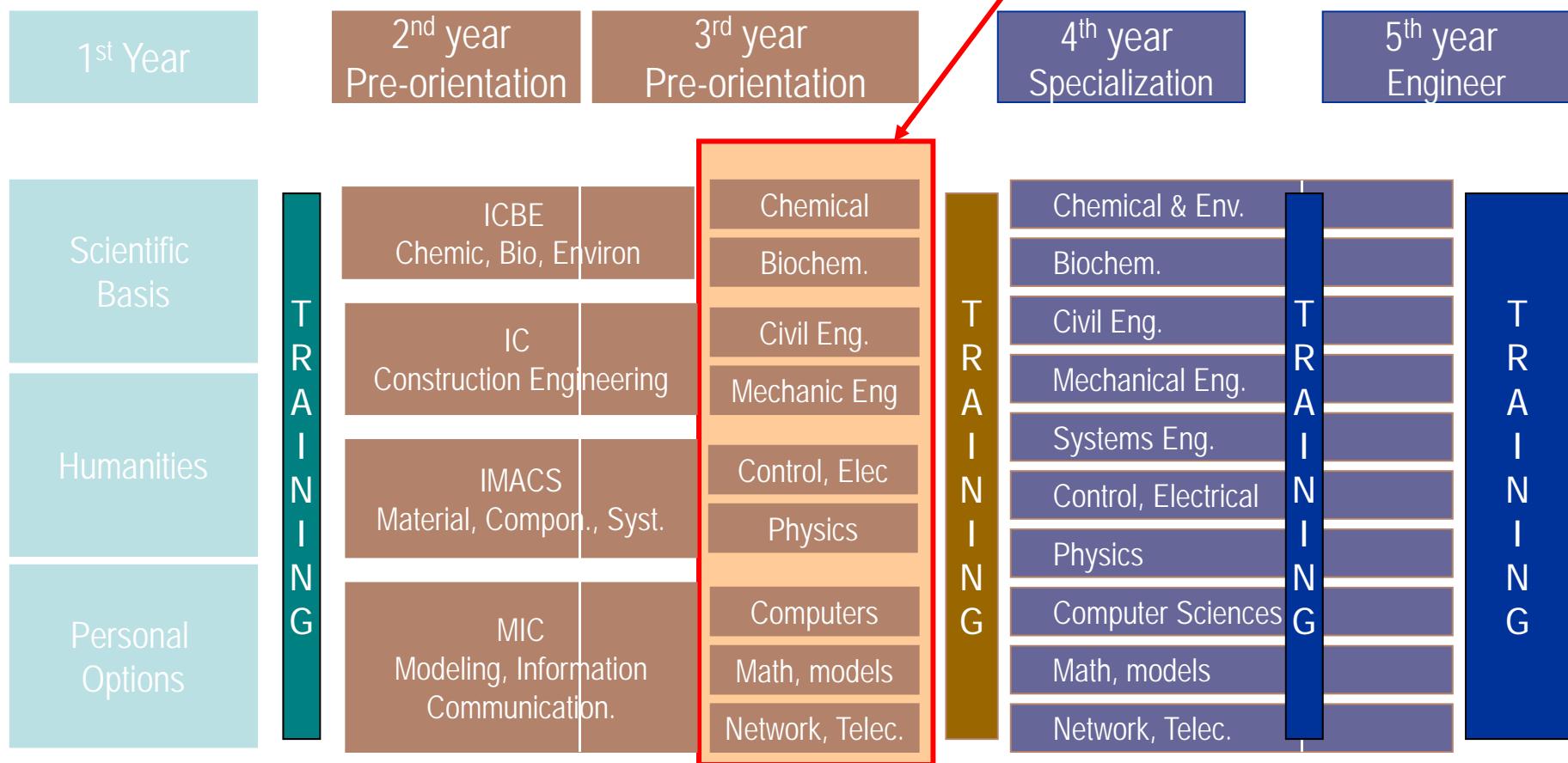
Virtual  
Experiments  
Course





# INSA Toulouse Teaching: Course details

**Virtual  
Experiments  
Course**

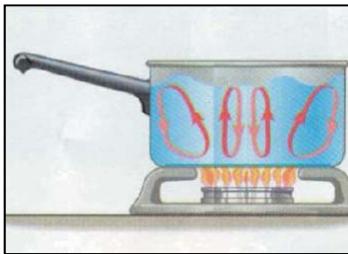


# Virtual Experiments Course

**Objective:** To initiate student to multiphysics numerical simulation by approaching concrete cases

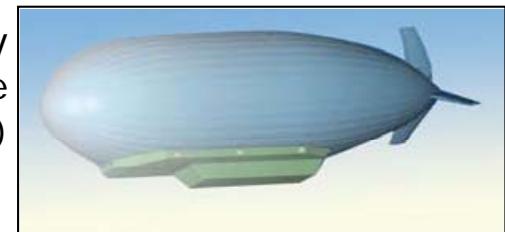
**Outline:**

- Quick description of **Finite Element Method**
- **4 projects** performed by students (about 10h each)

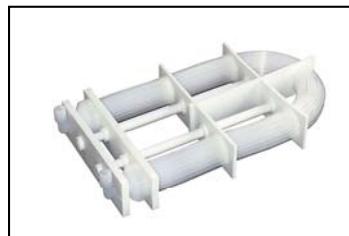


**1.** Natural convection in a pan  
([www.nanoscience.info](http://www.nanoscience.info))

**2.** Application of buoyancy to airship (Aerospace Adour Technologie)

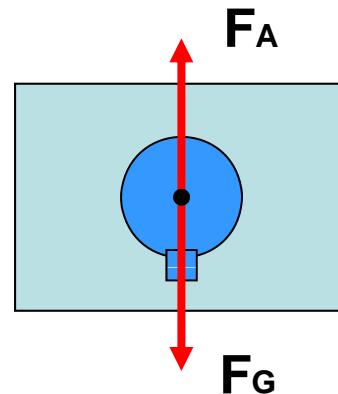
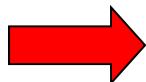
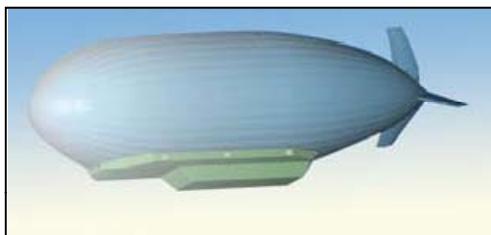


**3.** Hollow fiber cartridge to filter tap water  
(Dom source)



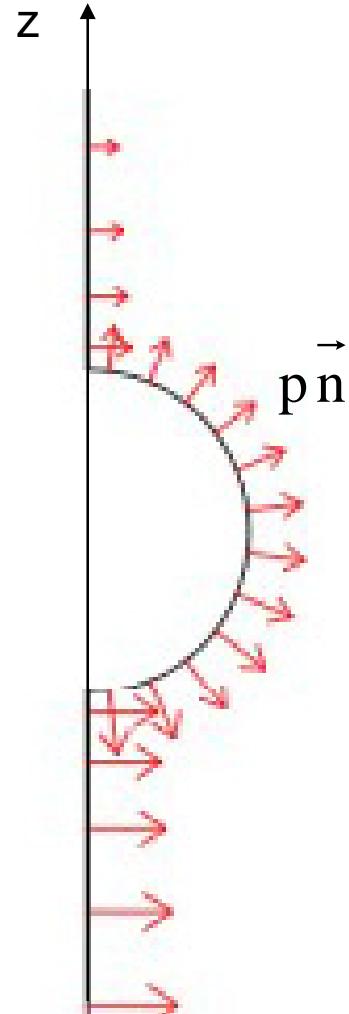
**4.** Heat exchanger  
([www.directindustry.fr](http://www.directindustry.fr))

## 2. Application of buoyancy to airship



- **Buoyancy force**
  - **Gravity force due to natural convection**
- ⇒ **Static of fluid**  
outside
- ⇒ **Combined incompressible NS equation  
 and convection diffusion heat transfer equation**  
inside

# Application of buoyancy to airship



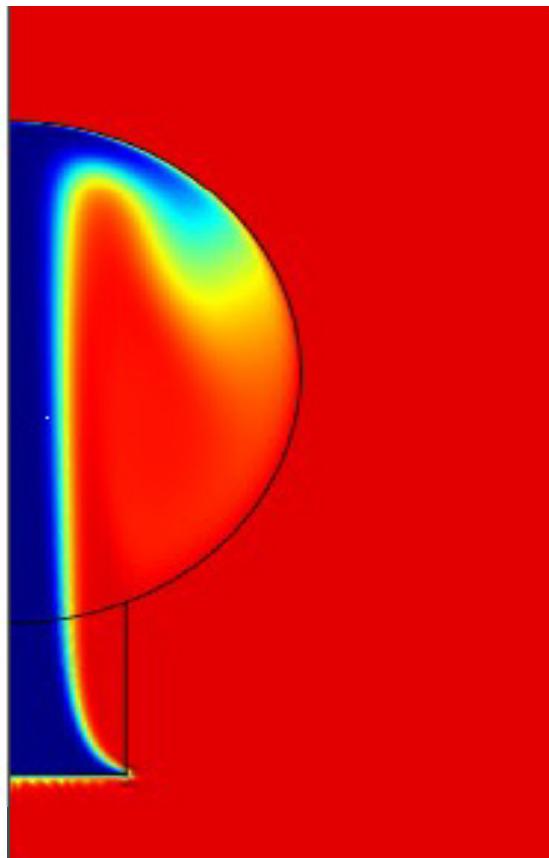
## 1st step : buoyancy analysis Pressure around a sphere

- Quiescent fluid with gravitational force
- Pressure map in the fluid obtained with N-S equations
- Integrate the pressure to obtain the buoyancy force
- Recover the Archimede law by varying properties

$$\mathbf{F}_A = \iiint (-p \hat{n}) \cdot \mathbf{e}_z dS$$



# Application of buoyancy to airship



## 2nd step : thermal coupling Flow induced by thermal convection

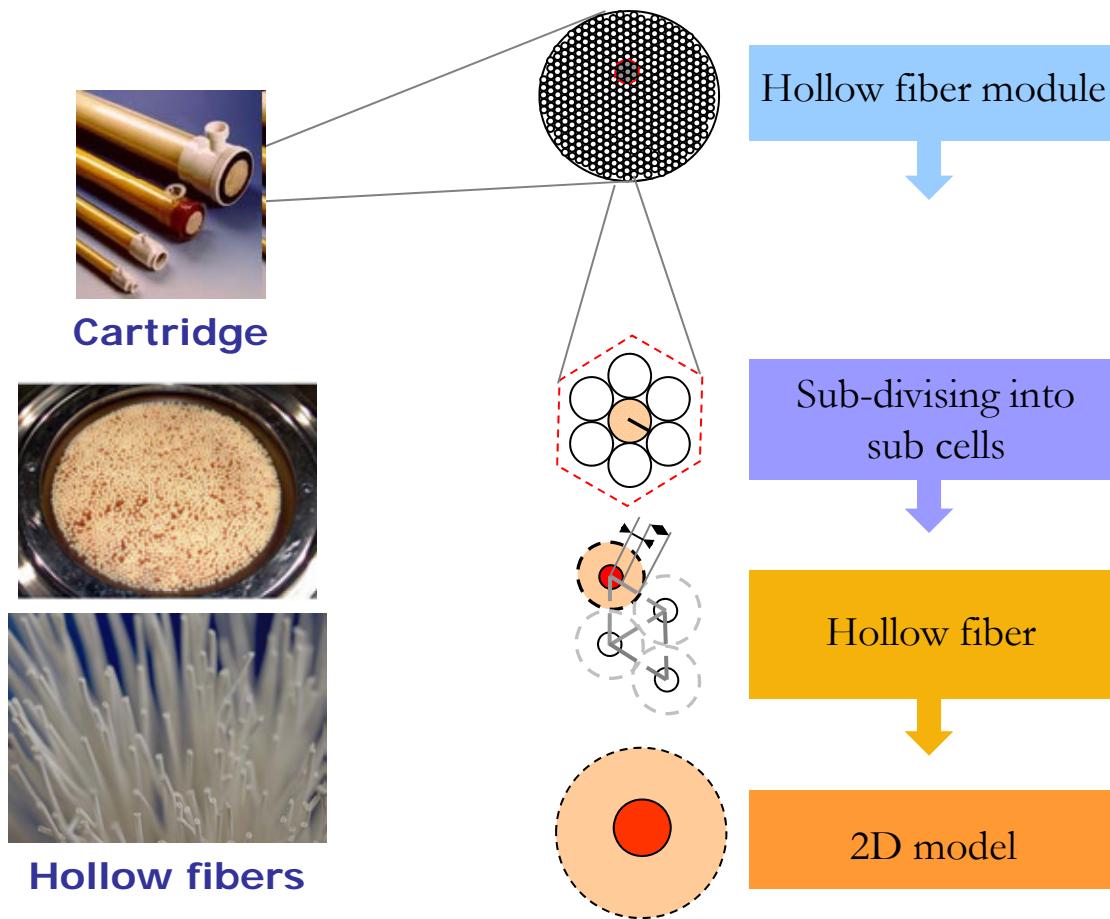
- Coupling N-S and heat transfer with the Boussinesq approximation
- Buoyancy force calculated by surface pressure integration
- Weight calculated by volume integration

**Discussion on the available force of the airship**

$$F_G = \iiint \rho(T) g dV$$

### 3. Hollow fiber cartridge to filter tap water

**Real Filter** → **Simplified Model**



- Regular arrangement of cylinders
- The fluid flow is calculated on a **unit cell** of this arrangement

**Happel's free surface model \*:**

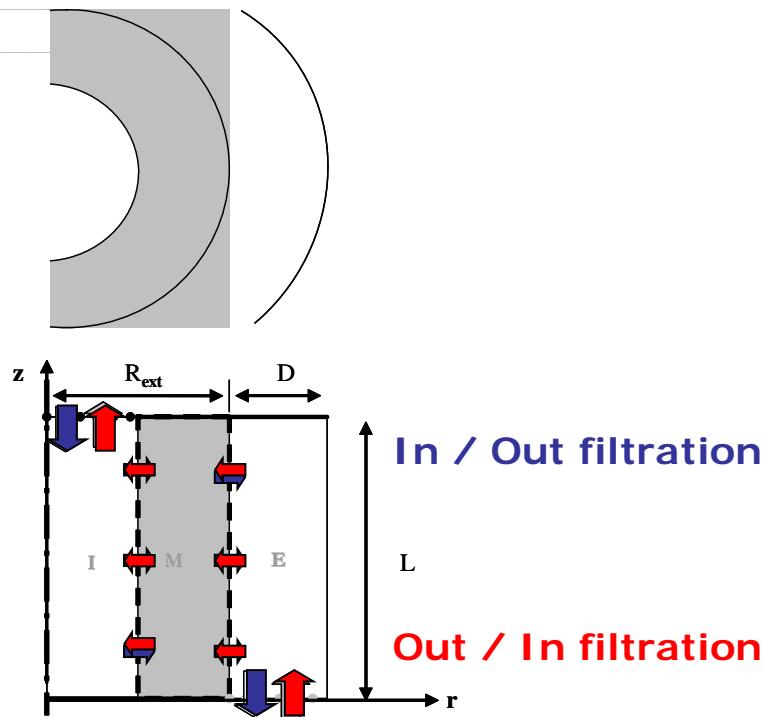
- The inner cylinder consists of **one single hollow fiber**
- The outer cylinder is a **fluid envelope** with a free surface used to account for packing effect

\* Happel, Viscous flow relatives to array of cylinders, AIChE, 1959

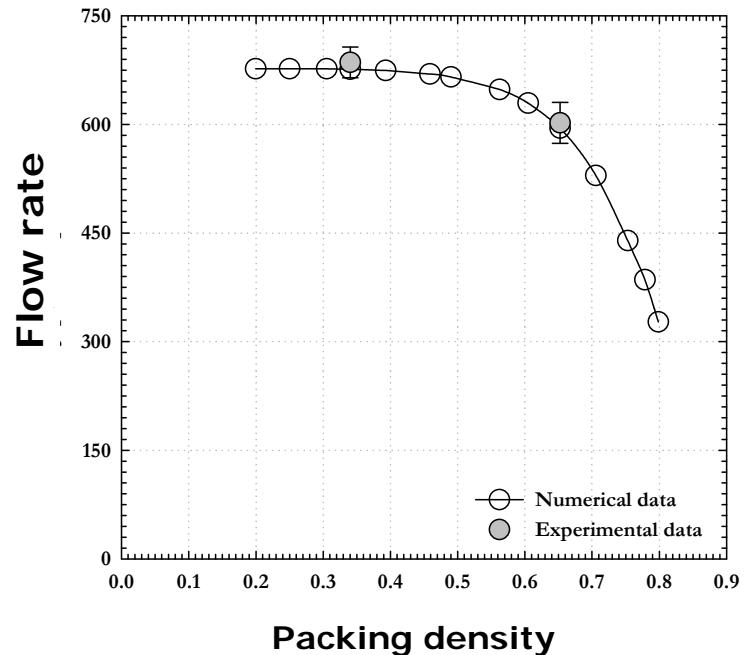
# Hollow fiber cartridge to filter tap water

## 1st step : Fluid flow without particles

- Coupling Navier Stokes and Darcy Brinkman model

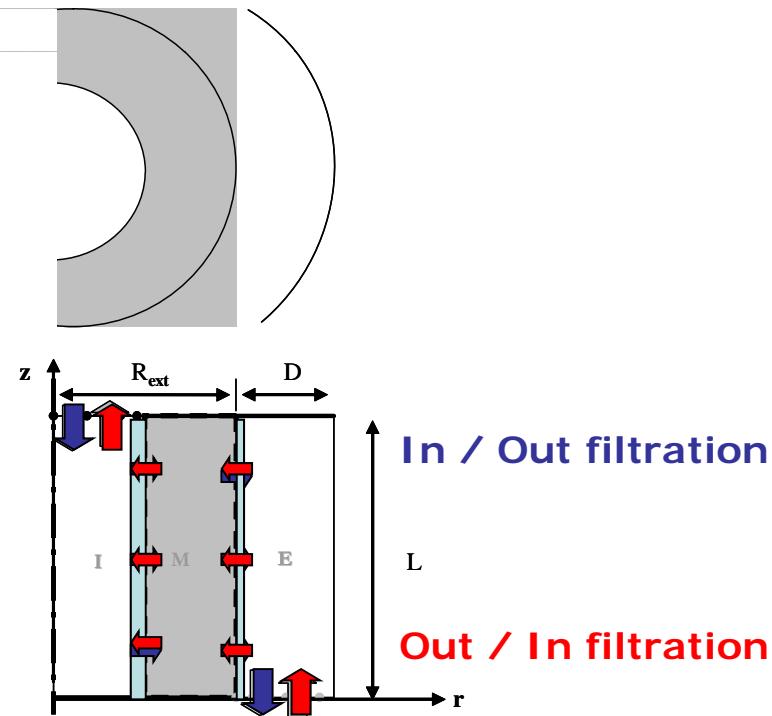


- Good agreement with experimental results
- Discussion on flow rate values



# Hollow fiber cartridge to filter tap water

## 2nd step : Fluid flow with particles

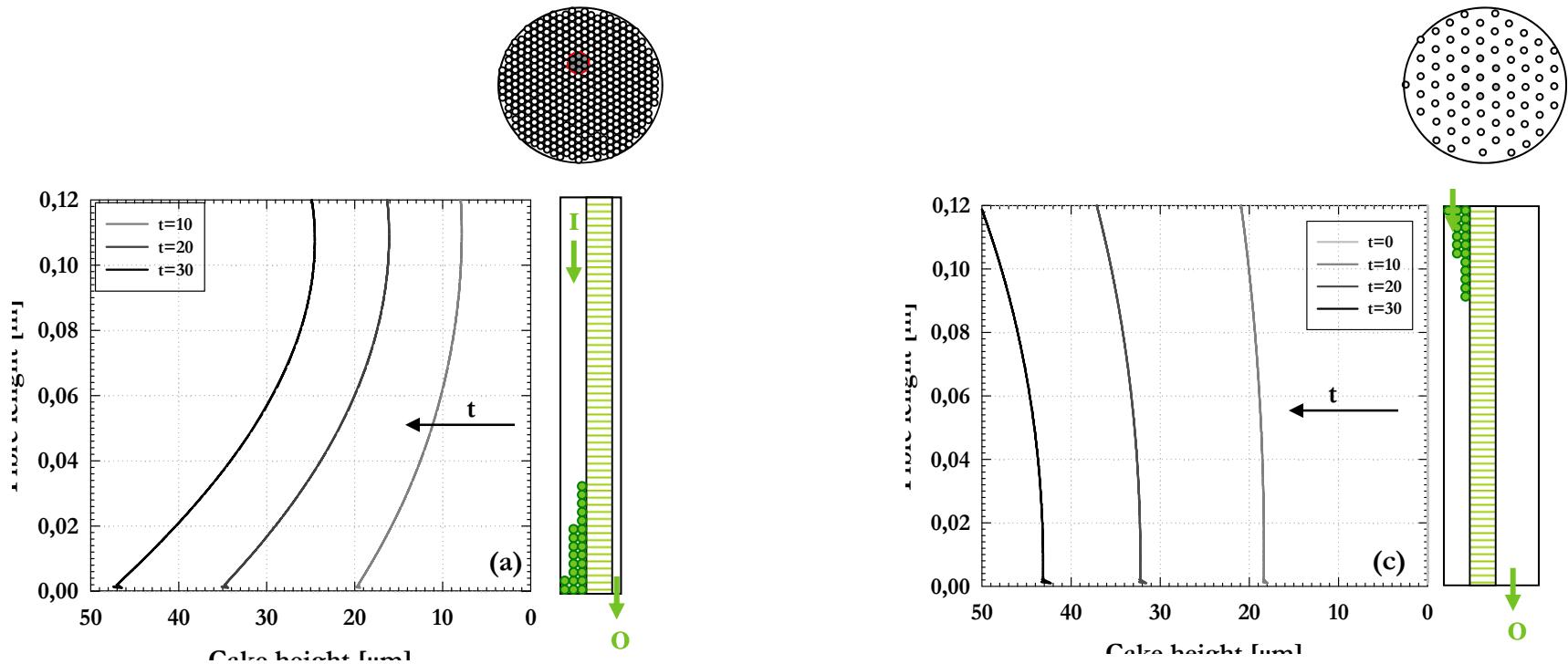


- Coupling Navier Stokes and Darcy Brinkman model
- Particles follow the streamlines
- Using moving mesh ALE to model cake formation

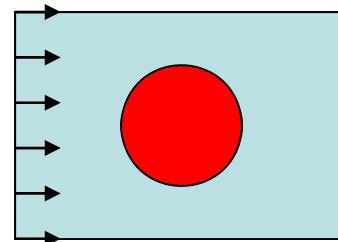
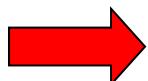
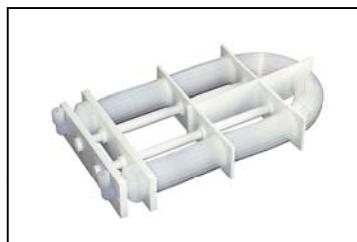
# Hollow fiber cartridge to filter tap water

**2nd step : Fluid flow with particles**

**At what time should we replace the filter cartridge?**



## 4. Heat Exchanger



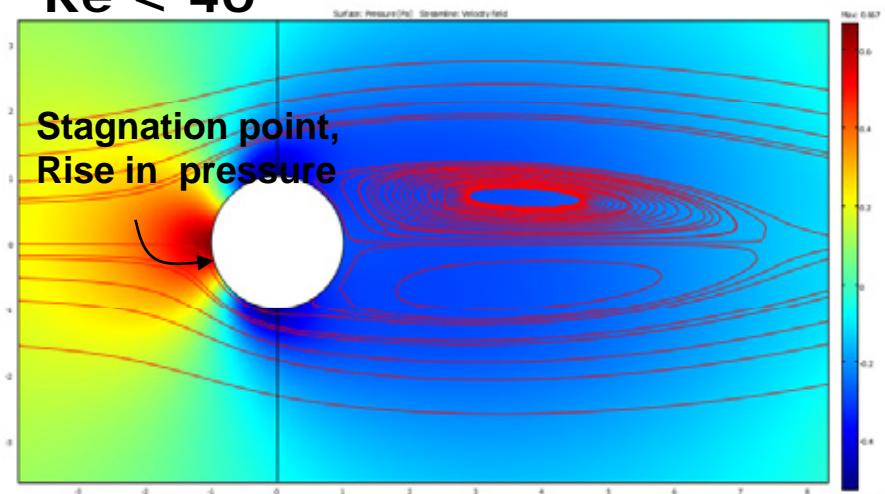
- **heated cylinder cooled by a laminar fluid flow**
- **external flow normal to the axis of the circular cylinder**
- **fluid-thermal coupling :**  
**combined incompressible NS equation**  
**and convection diffusion heat transfer equation**



# Heat Exchanger

**1st step : circular cylinder in a cross flow,  
isothermal condition**

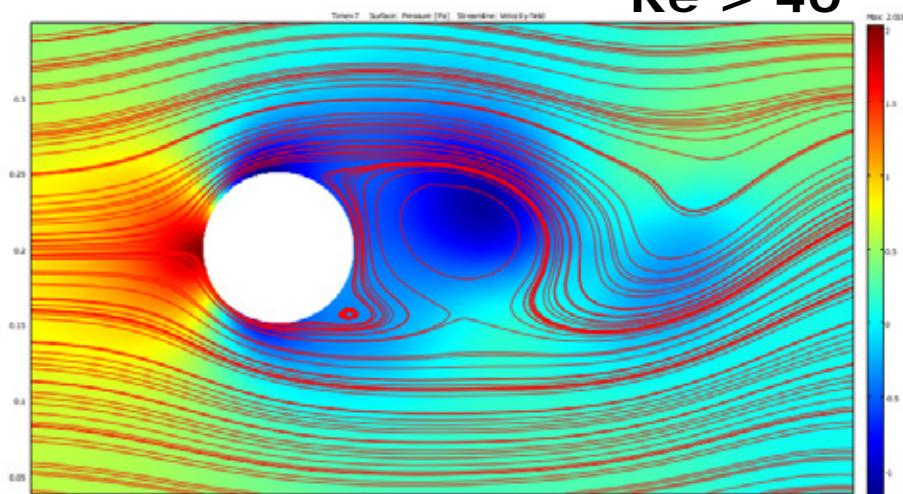
$Re < 40$



**Steady flow**

- Two symmetric vortex

$Re > 40$



**Unsteady flow**

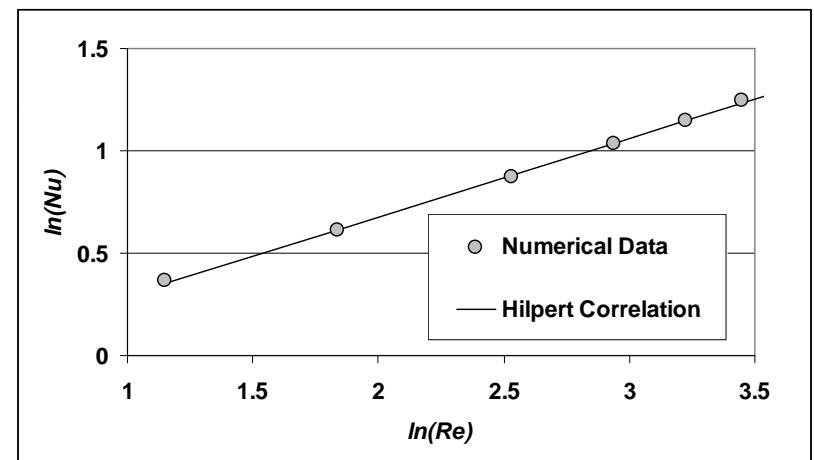
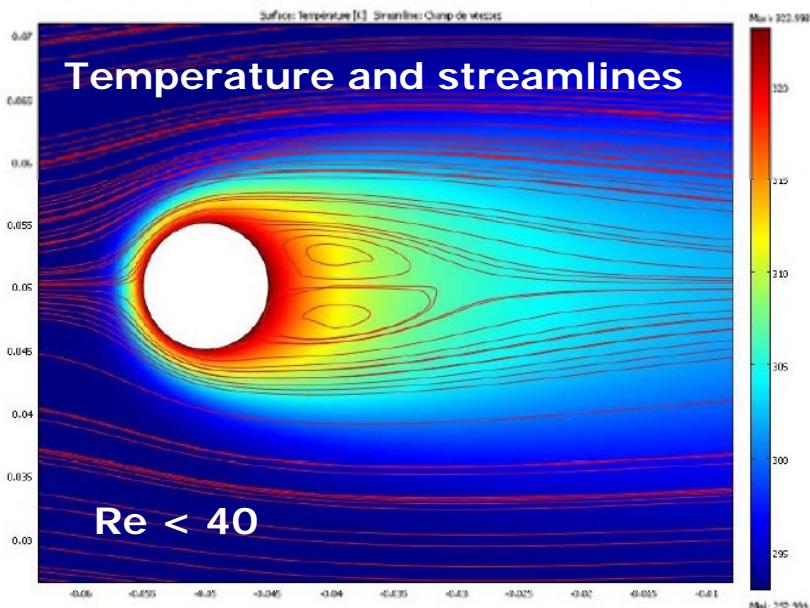
- Karman vortex street observed with a repeating pattern of swirling vortices.
- Period of the vortex shedding

**Comparison with literature results**

M. Schäfer & S. Turek, 'Benchmark computations of laminar flow around cylinder', E.H. Hirschel (editor), *Flow Simulation with High-Performance Computers II*, 547–566, 1996.

# Heat Exchanger

**2nd step : introduction of thermal coupling flow around a heated cylinder**



- Maximum of the local heat flux at the stagnation point
- Total heat flux calculated by integration of the normal local heat flux on the whole cylinder  $\Rightarrow$  Nusselt number

- Several fluids studied  
 $\Rightarrow$  Correlations of the overall average Nusselt number obtained
- Very good agreement between numerical results and Hilpert Correlation

# Conclusions

## COMSOL Multiphysics: a useful tool for teachers

### -To illustrate physical phenomena

ex:      buoyancy  
              fluid flow / porous media flow  
              convection heat transfer

### -To approach techniques of numerical simulation

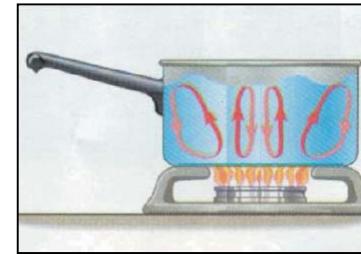
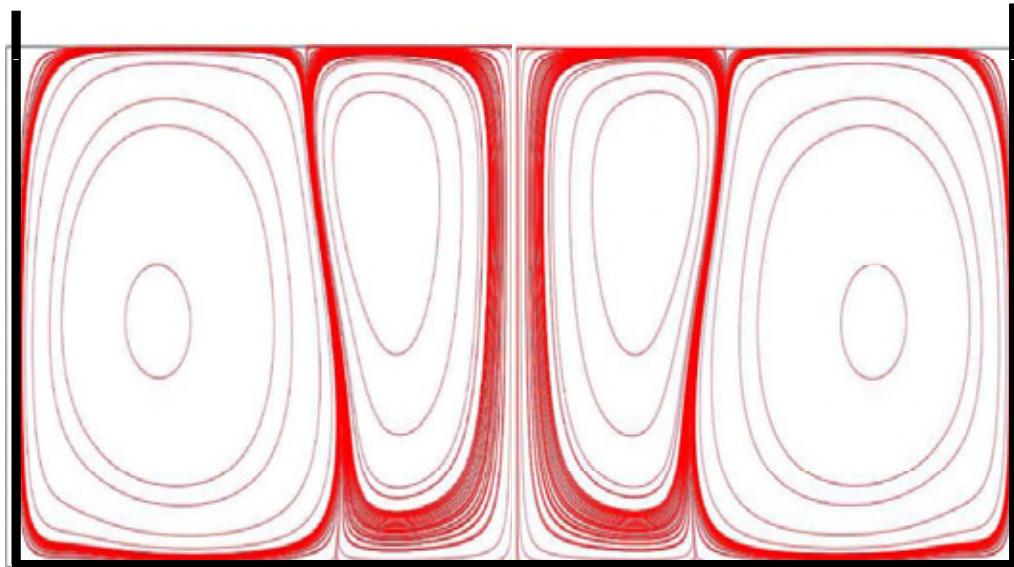
geometry,  
mesh,  
boundary conditions,  
solver,  
postprocessing



**In order to initiate future engineers to  
multiphysics numerical simulation**



# Thank you



## Natural Convection in a pan