

COMSOL Conference 2010

NUMERICAL SIMULATION OF EXACT TWO-DIMENSIONAL GOVERNING EQUATIONS FOR INTERNAL CONDENSING FLOWS

By:

Soumya Mitra and Ranjeeth Naik

Advisor:

Dr . Amitabh Narain

Michigan Technological University

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Condensing Flows in Applications

Electronic/Computer Cooling

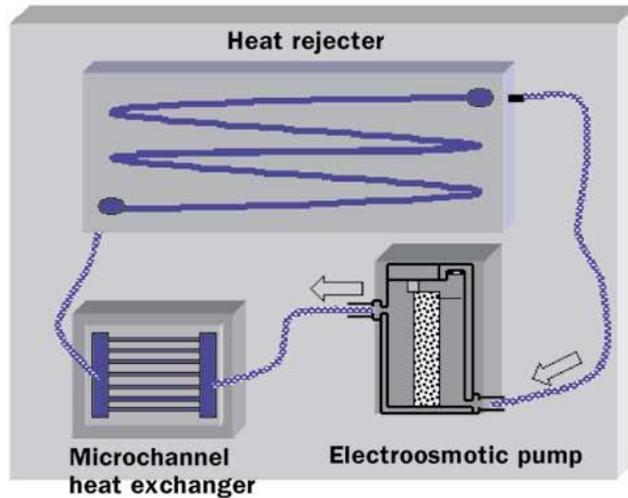


Image Courtesy: <http://electronics-cooling.com/articles>

Space Based Applications



Image Courtesy: <http://www.boeing.com>

Heat pipes, Rankine Power Cycles, Thermal Management Systems, Design of ISS-based two-phase flow facility, etc.

Research Purpose:

- Facilitate more effective design of “thermal” systems – miniature or not.
- Significantly enhance chance of successful operation of condensers in ground/space based applications.

Overview:

- ❖ Problem Formulation
- ❖ COMSOL / MATLAB Implementation
- ❖ Validation of Computational Results
 - By Other Computational Tools
 - With Experiments
- ❖ Differences between Gravity Dominated and Shear Driven Flows

Background Literature

- Available knowledge for exact and approximate model equations for two-phase flows and interface.
- Classical solutions of external condensing flow problems.
- Experimental data and correlations for internal condensing flow problems.
- Level-set methods and its implementation
- Experimental data and correlations for external flow problems.
- Analytical and semi-empirical data and theoretical results for internal condensing flows .
- Theoretical results on dynamic instabilities and turbulence.

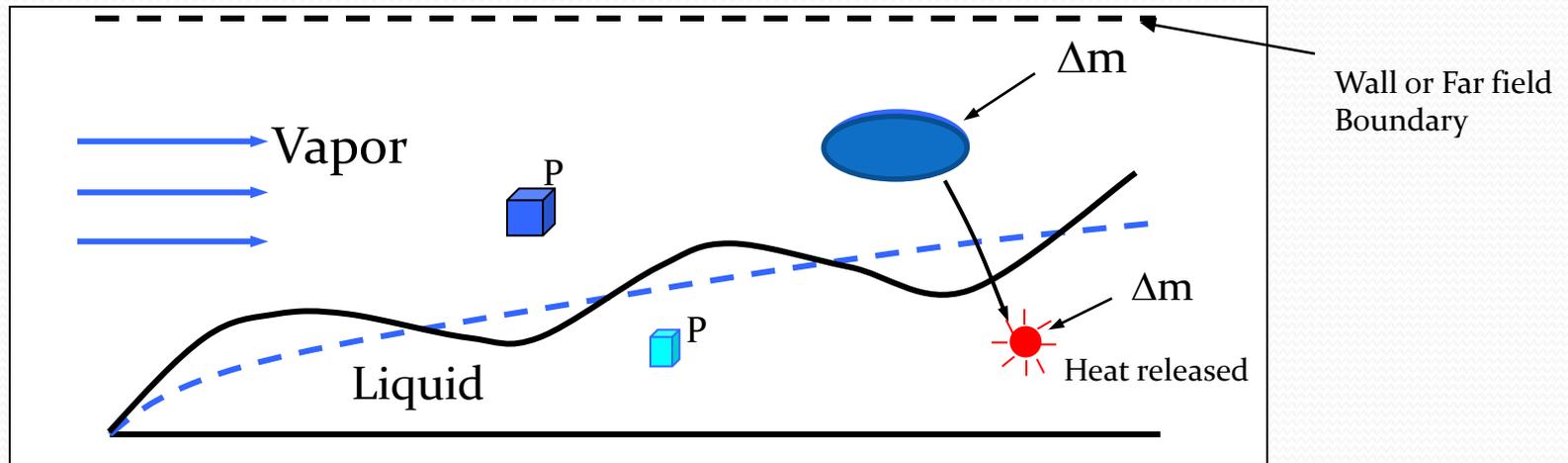
Next..

Basic Simulation Strategy

Based on first-principles

- Continuum governing equations
- Interface conditions

(Kinematics, Mass, Momentum, Energy Transfer & Thermodynamic)



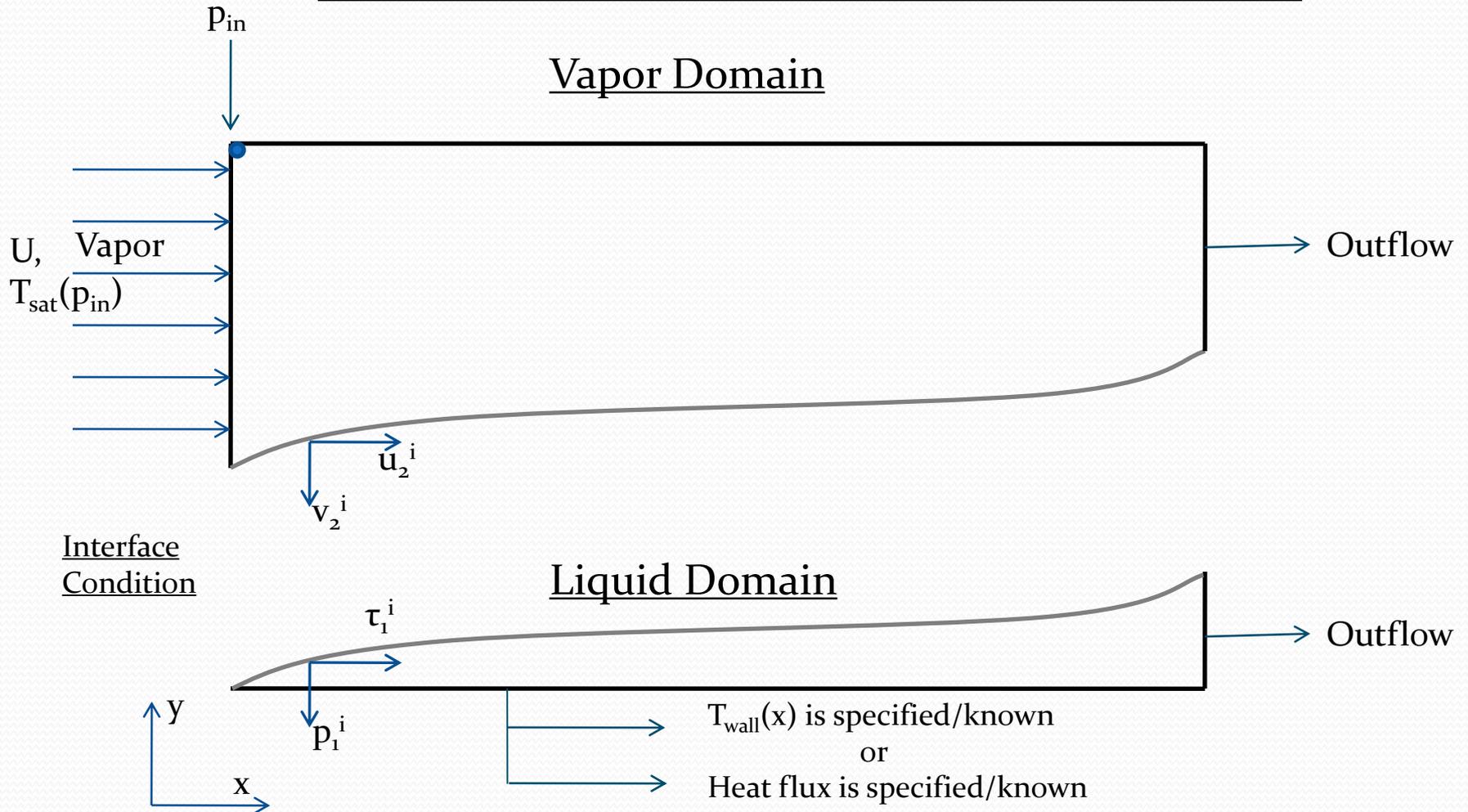
■ Other conditions

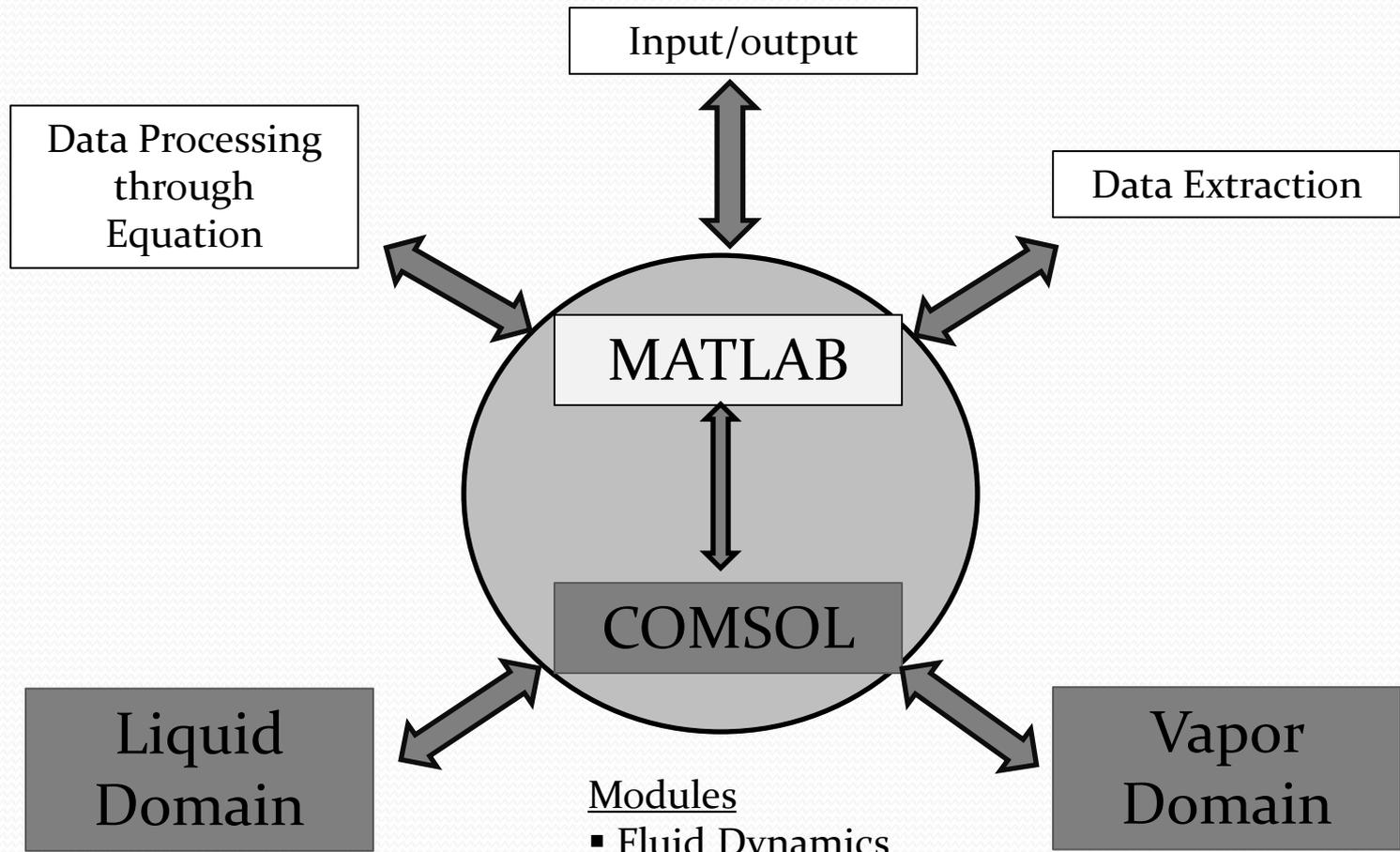
- Wall conditions
- Conditions at infinity (if any)
- Inlet/outlet conditions
- Initial conditions ($t = 0$)

Special features

- Latent heat released with huge increase in density
- Interface conditions bring in additional non-linearities – they connect the vapor and liquid flows, and also determine its time varying location

COMSOL/MATLAB Based Simulation Tool





Modules

- Fluid Dynamics
- Heat Transfer
- Deformed Mesh
- Level-Set ???

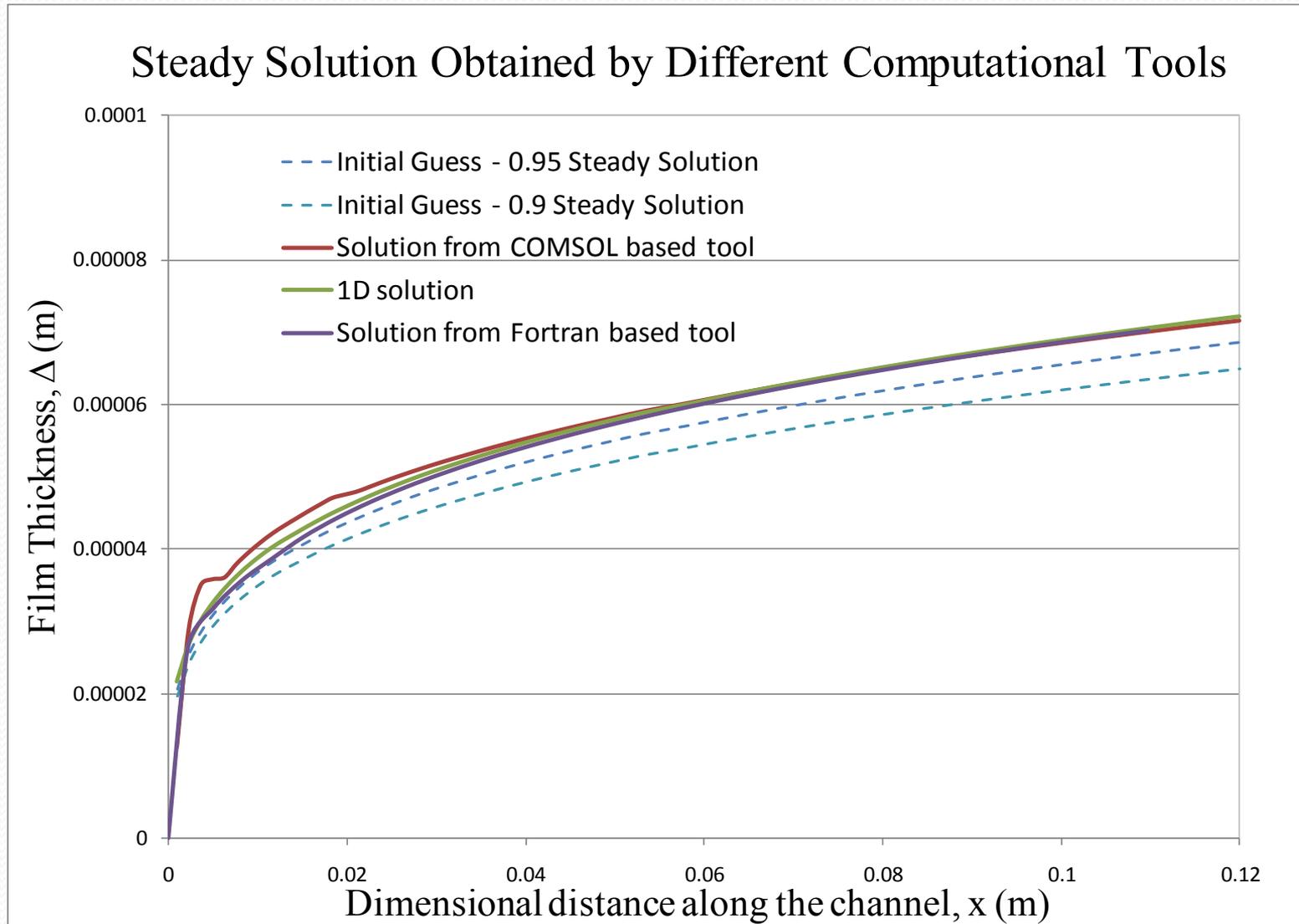
Current Simulation Capabilities Annular Internal Condensing Flows

- Boundary value problem (BVP) for steady solutions
- Initial boundary value problem (IBVP) for unsteady solutions

Validation of Computational Results

1. The computational results from the COMSOL / MATLAB tool is compared with the following computational tools:
 - ✓ 2-D simulation tool based on SIMPLER algorithm
 - ✓ Independently developed 1-D analytical tool
2. The computational results are also compared with the experimental results:
 - ✓ Internal condensing flows inside an inclined channel (Lu & Suryanarayana)

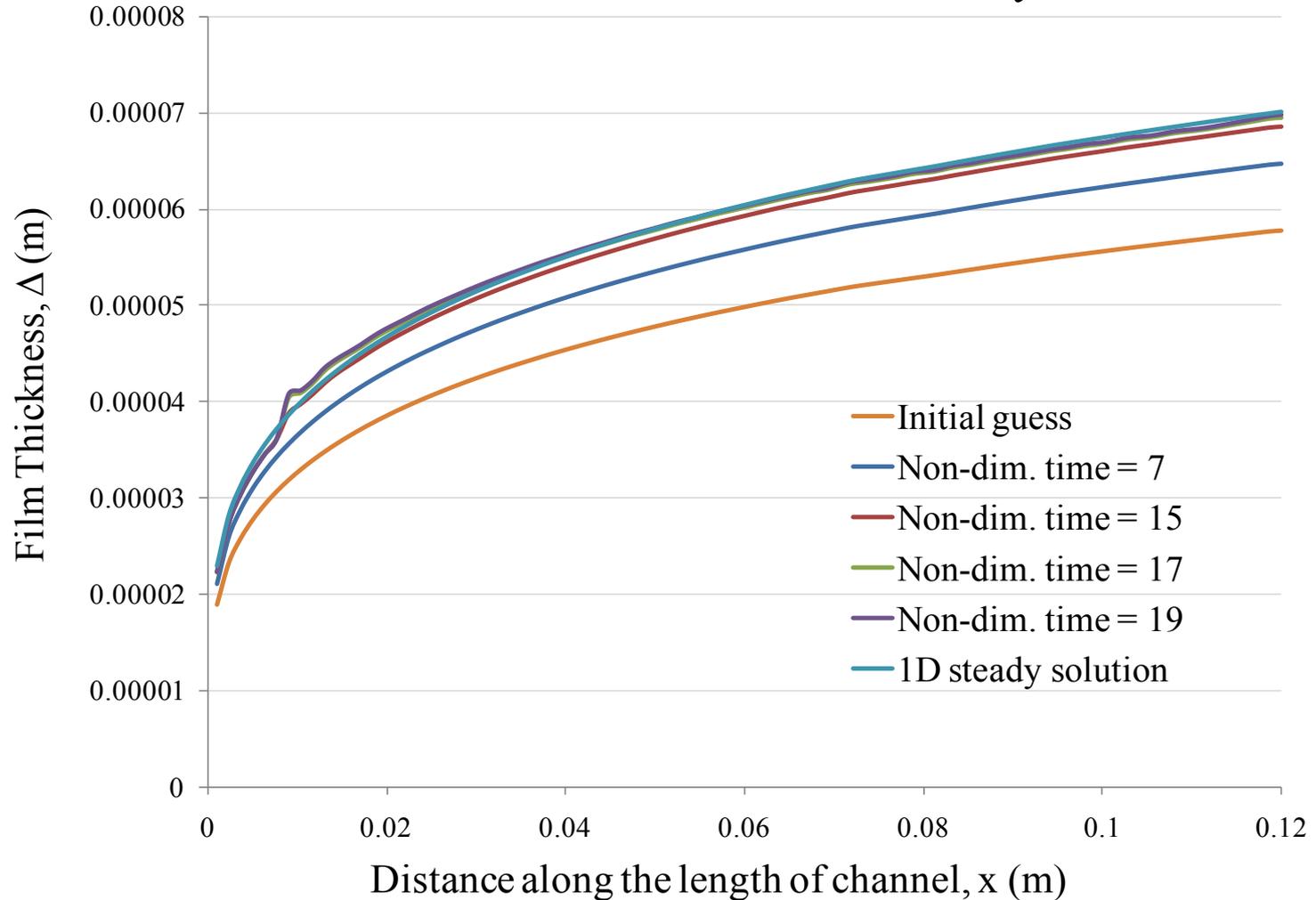
Validation by Comparison with Other Computational Results



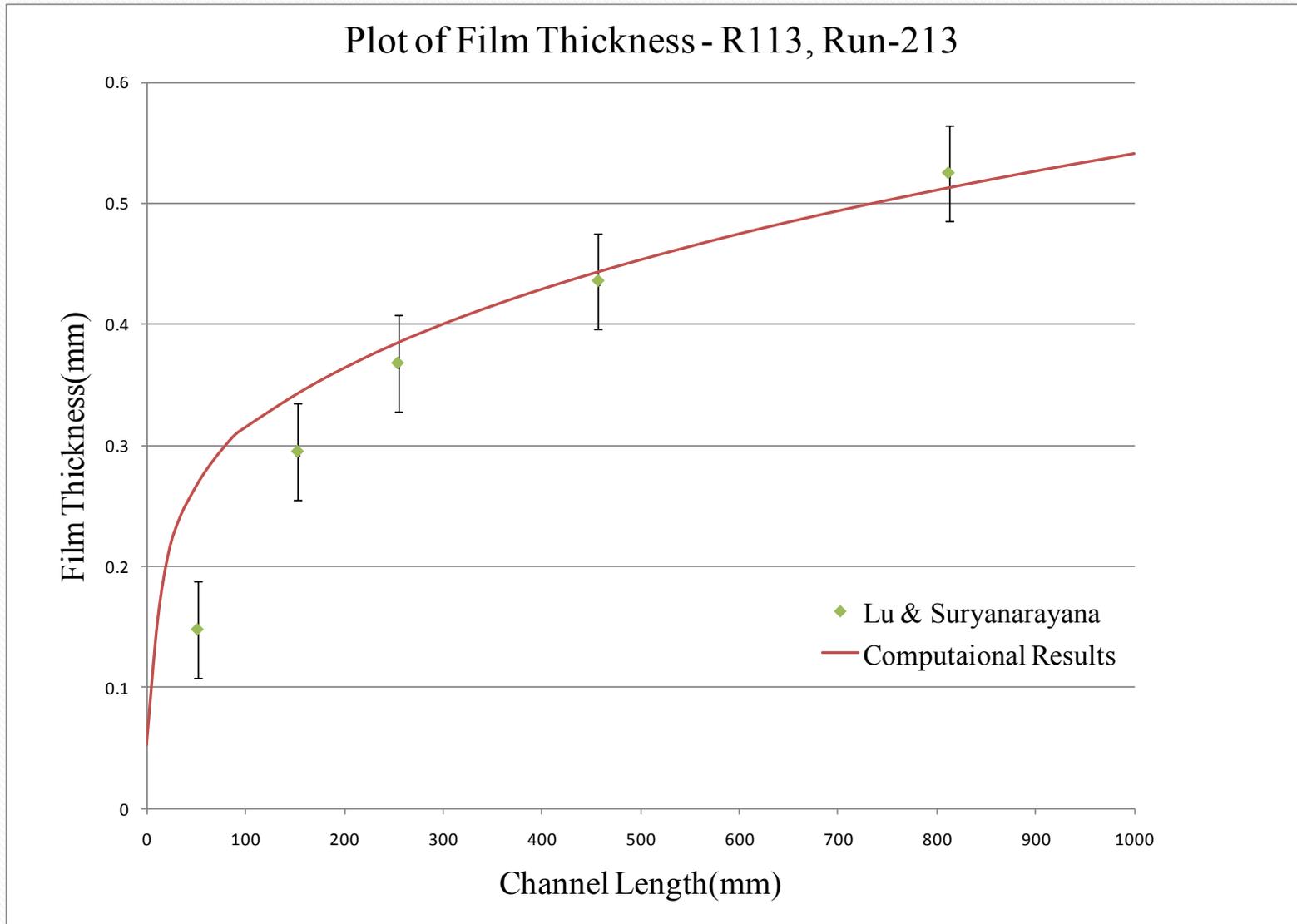
Gravity Driven and Shear Driven Flows

Gravity driven and shear driven flows are quite different with regard to

Film Thickness Values Obtained from the Unsteady Simulation



Comparison of the Comsol Simulation with Lu and Suryanarayana for Run-213



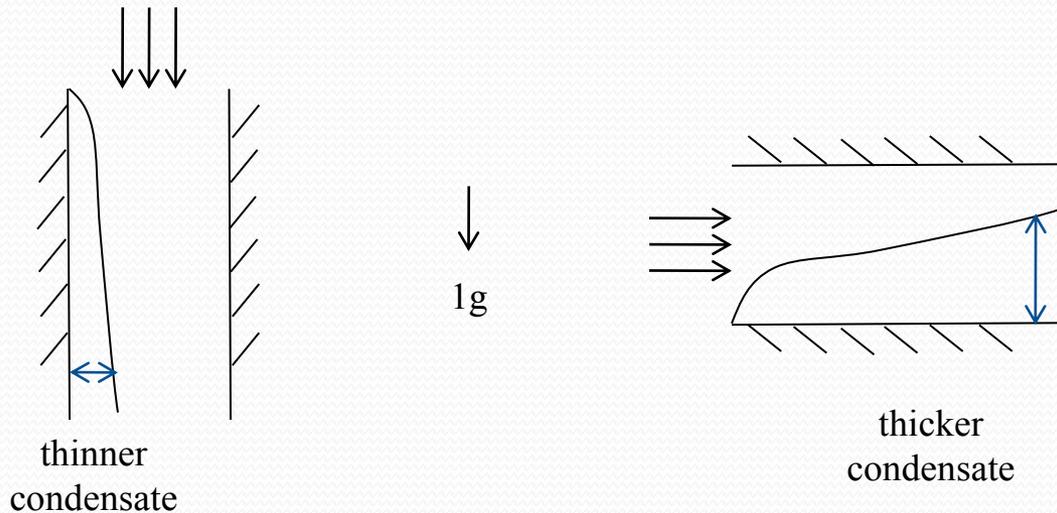
Validation by Comparison with Experiments of Lu and Suryanarayana

Comparison of Lu & Suryanarayana Experimental data with Computaional Results for R113 with an Inclination of 1 degree

Run	Fluid	U m/s	Delta_T °C	Film Thickness Experimental,mm					Film Thickness Computaional, mm					Error between Exp and Comp (%)
				50.8	152.4	254	457.2	812.2	50.8	152.4	254	457.2	812.2	
208	R-113	0.861764	22.28	0.147	0.296	0.344	0.37	0.4	0.226	0.298	0.339	0.394	0.456	9.1
211	R-113	1.10659	21.2	0.134	0.271	0.298	0.368	0.397	0.218	0.290	0.331	0.386	0.449	12.3
223	R-113	1.256109	37.03	0.165	0.294	0.358	0.423	0.504	0.253	0.333	0.378	0.438	0.505	8.5
213	R-113	1.281019	39.73	0.148	0.295	0.368	0.436	0.525	0.257	0.338	0.384	0.445	0.514	8.6
215	R-113	1.277654	21.65	0.106	0.195	0.247	0.345	0.38	0.219	0.289	0.328	0.381	0.440	23.2
206	R-113	1.710475	30.95	0.17	0.28	0.34	0.375	0.412	0.236	0.309	0.350	0.405	0.466	10.7

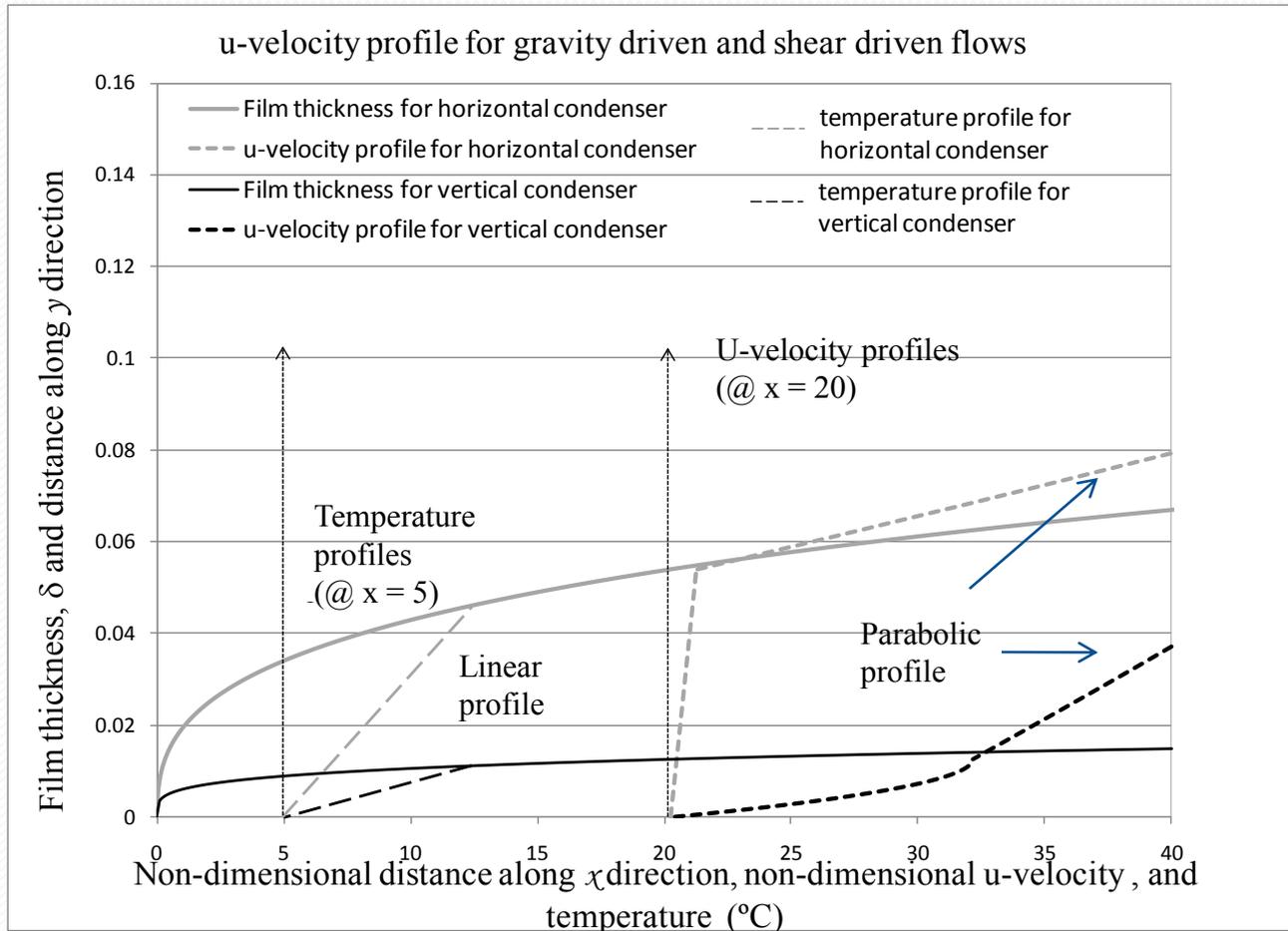
Relevant Results

Annular flow regime is responsible for rejecting most of the heat from a condenser. The associated liquid condensate motion is strongly affected by the orientation of the gravity vector \bar{g} if the duct's hydraulic diameter $D_H \geq 2\text{mm}$.



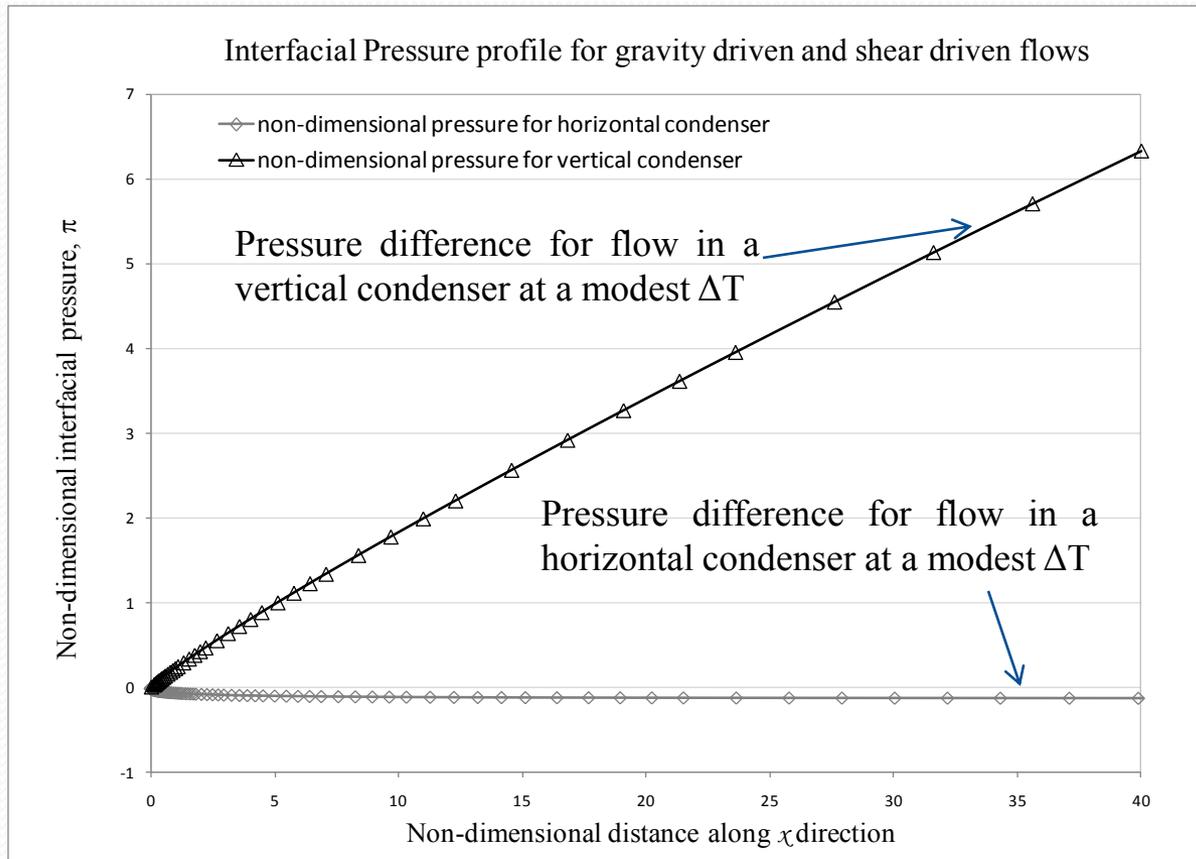
Gravity Driven and Shear Driven Flows

Gravity driven and shear driven flows are quite different with regard to film thickness, velocity, and temperature profiles.

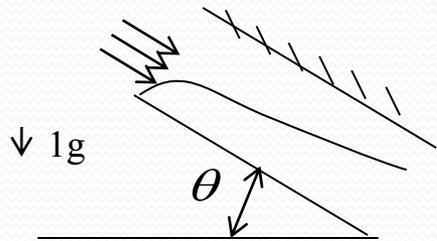


Gravity Driven and Shear Driven Flows

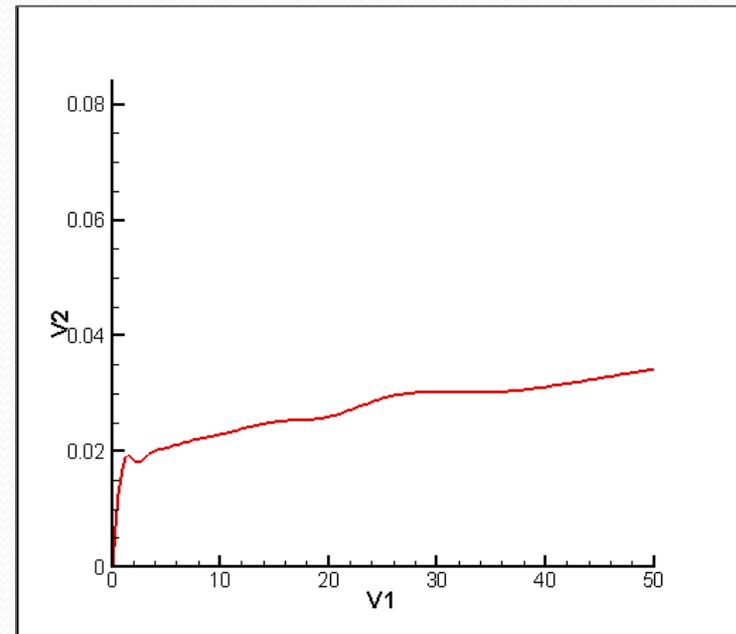
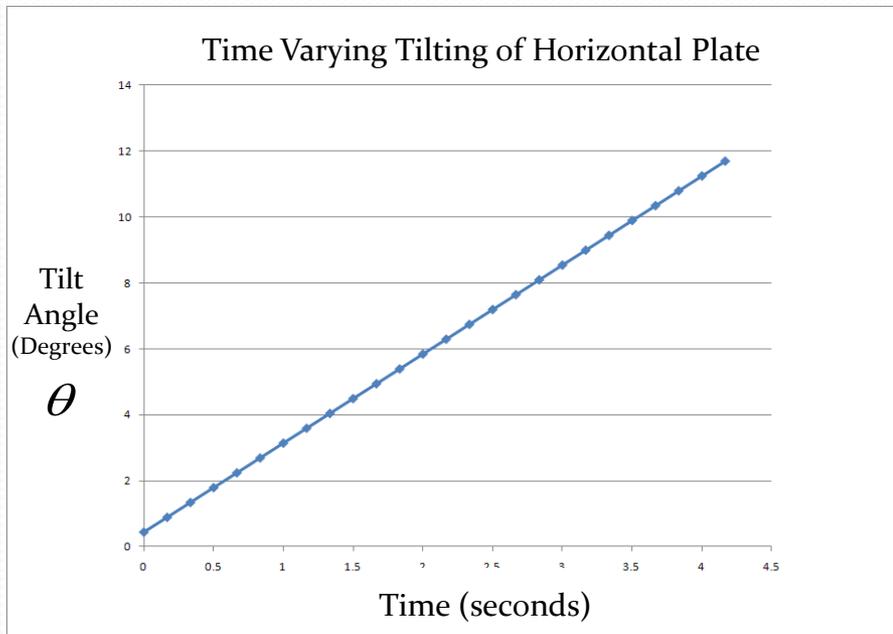
Gravity driven and shear driven flows are quite different with regard to cross-sectional pressure variations as well



Gravity Driven and Shear Driven Flows



Effect of time-varying gravity vector (\bar{g}) on film thickness



V_1 - Distance along the condenser
(Non dimensional)

V_2 - Film thickness (Non dimensional)

For small inclinations ($\sim 10^\circ$) of the condensing plate, the flow becomes gravity driven in mm-scale condensing flows

Summary

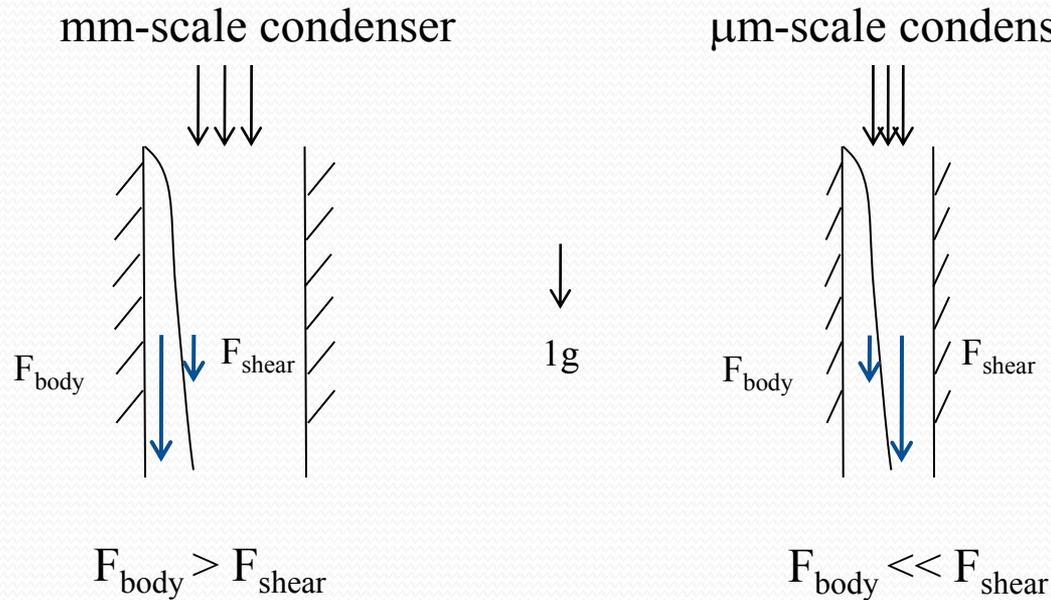
- An algorithm for successful and accurate computational simulations of steady and unsteady condensing flows has been presented.
- The results from the computational tool using COMSOL are in good agreement with the 2-D computational code based on SIMPLER Algorithm and a completely independent quasi 1-D tool.
- Relevant results from the reported computational tool developed here are shown to be in agreement with the experimental results for the inclined channel flow experiments.
- Differences between gravity dominated flow and shear driven flows are discussed.

Thank You

Questions ?

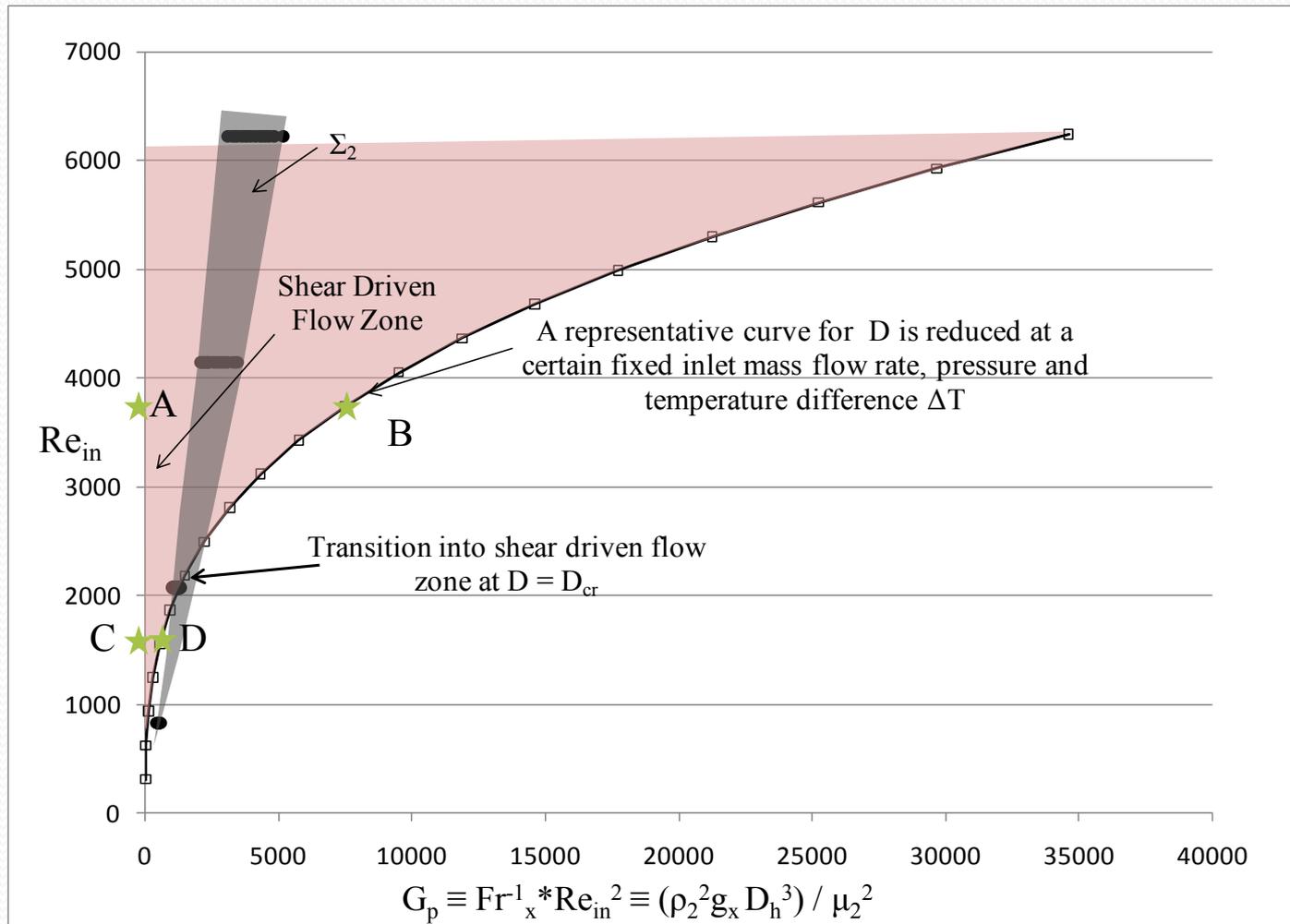
Vertical Flows for mm- μ m Scale Condensers

A condenser's gravity-sensitivity can be minimized by using suitable array's of μ m-scale ducts. This makes body force effects small relative to shear forces – at a pressure penalty.



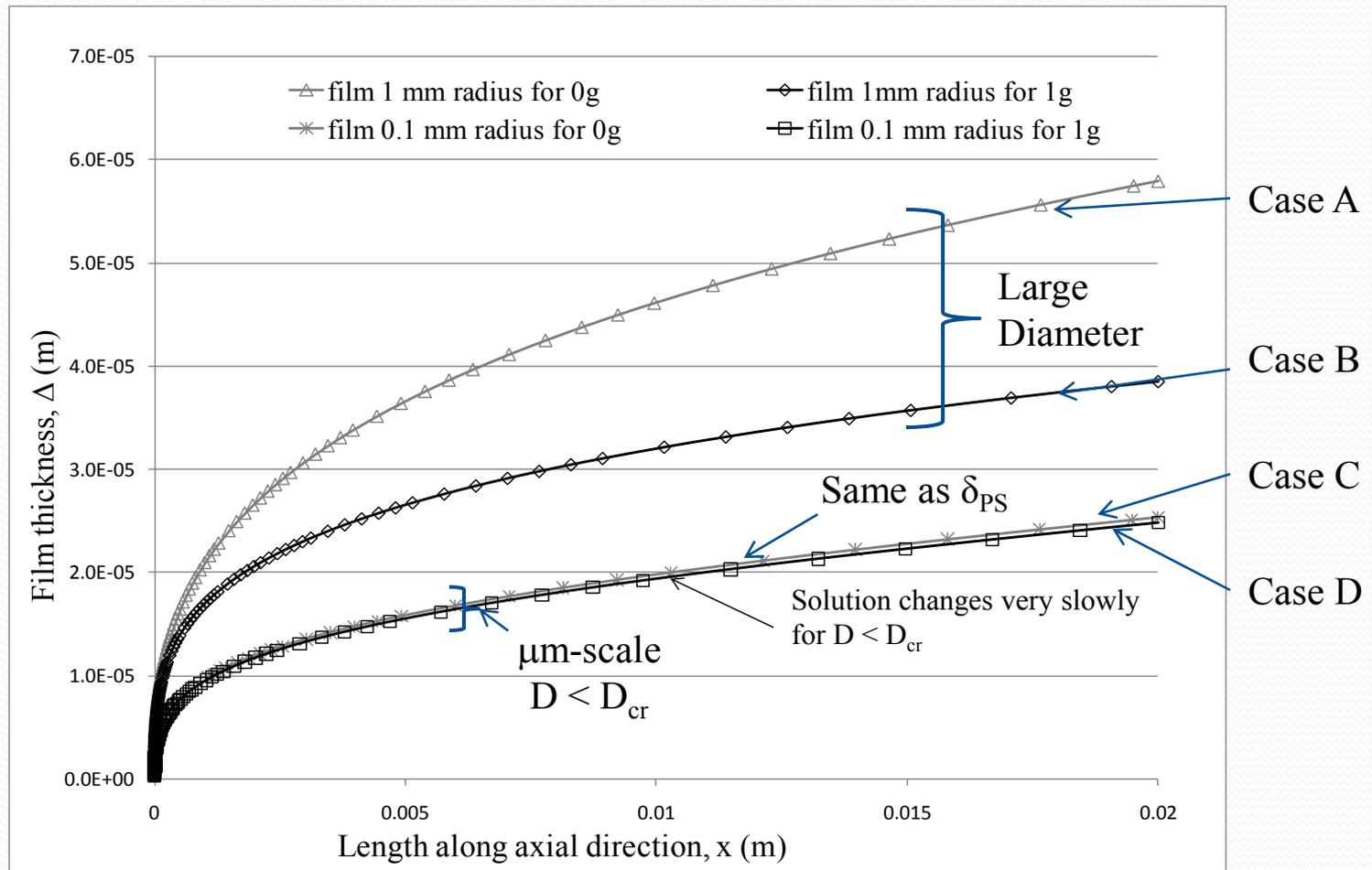
Condensing Flows in μm Scale Ducts are Shear/Pressure Driven

Gravity parameter $G_p \equiv (\rho_2^2 g_x D_h^3) / \mu_2^2$ is reduced by $D_h \rightarrow \mu\text{m}$ scale, and $D_h < D_{cr}$, the flow becomes shear driven for a range of gravity values and for a given average inlet speed, ΔT , and working fluid



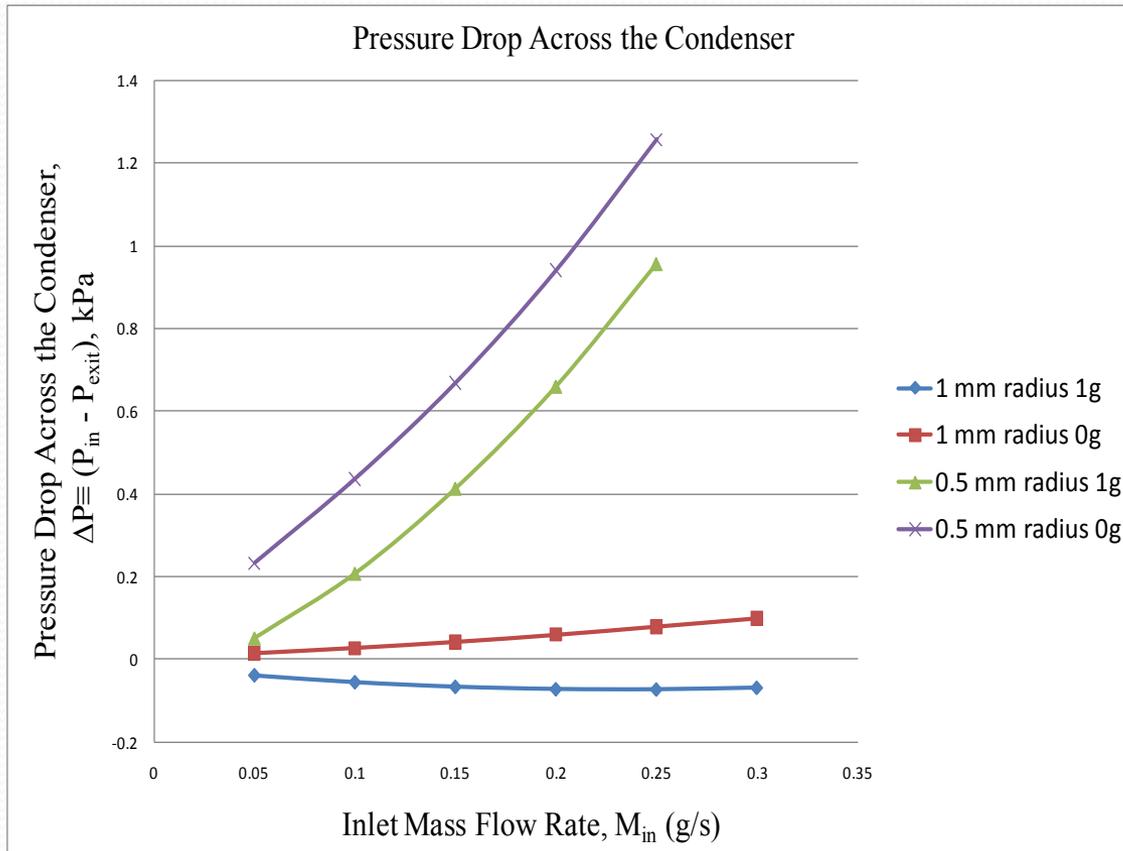
Effect of Hydraulic Diameter on the Nature of Flow

As $D_h \rightarrow \mu\text{m}$ scale, and $D_h < D_{cr}$, the flow becomes shear driven and gravity-insensitive



Effect of Hydraulic Diameter on the Nature of Flow

As $D_h \rightarrow \mu\text{m}$ scale, and $D_h < D_{cr}$, the flow becomes shear driven and is accompanied with significant rise in pressure drop



Ongoing research investigations for condensing flows in μm -scale ducts will account for:

- Significant $T_s(p^i)$ variation over the flow
- Significant vapor density variation
- Significant surface tension effects

Validation of Computational Results and Experiments

The condensing flow simulation results presented earlier are based on accurate computational simulations that have been quantitatively verified by experiments for gravity driven flows.

Flow Regimes in Internal Condensing Flows

Gravity Driven Flows ($D_h > 1$ mm)

Mostly Annular

(Rabas et. al. [2000],
Narain et. al. [2009] – [2010]*)

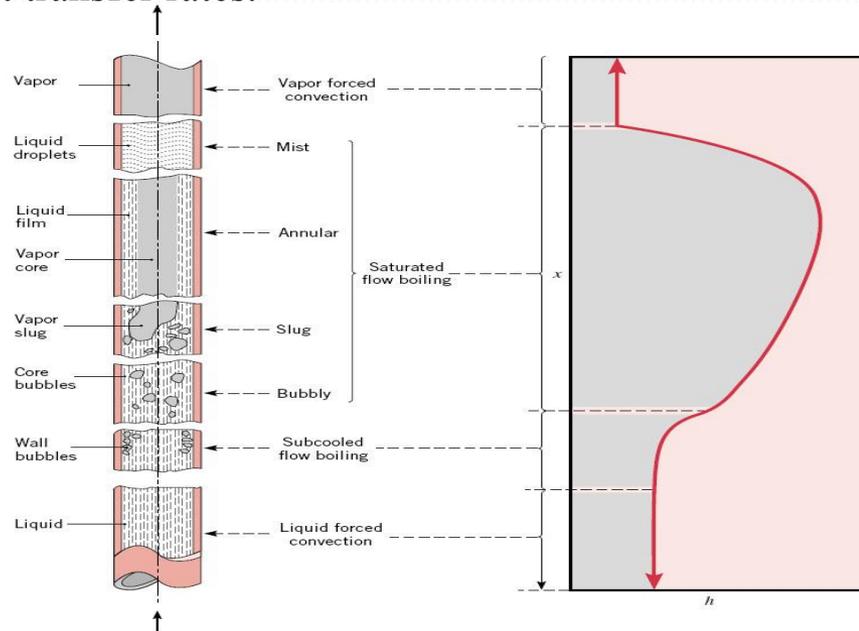
Shear Driven Flows

- Annular for:
Horizontal mm scale partially condensing flows
- Results are consistent with Cheng et. al. [2005],
Garimella et. al. [1999] (Complex Morphology)

(?) ← Horizontal Tube (> mm-scale) → (?)

Sensitivity of Boiling/Evaporating Flows to Gravity Vector

For flow inside boilers/evaporators, the effects of \bar{g} vector changes are expected to be less dramatic as compared to flow inside condensers. This is because “thermal” boundary conditions on the heater surface primarily couple with inlet mass flow rate values - which causes body forces to have a secondary influence on heat transfer rates.



Courtesy: Incropera et.al [Textbook].

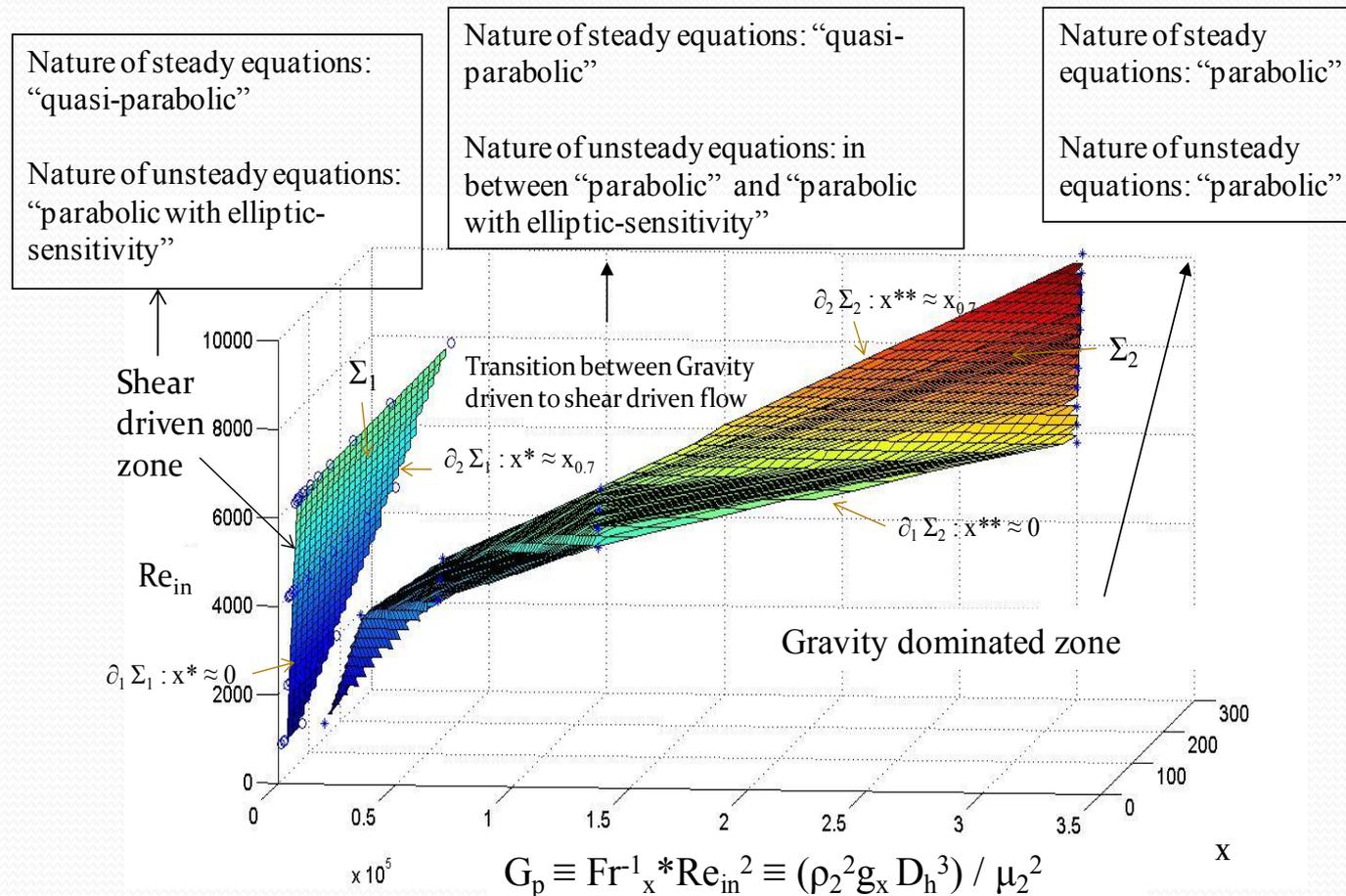
The sensitivity of flow boilers need to be ascertained (**research is needed**).

We do not know what flow boiling information exists with regard to g-sensitivity of Fairchild Corporation's existing aircraft designs. Our forthcoming boiler experiments require that, for air force needs, the boiler be placed on a suitable shaker.

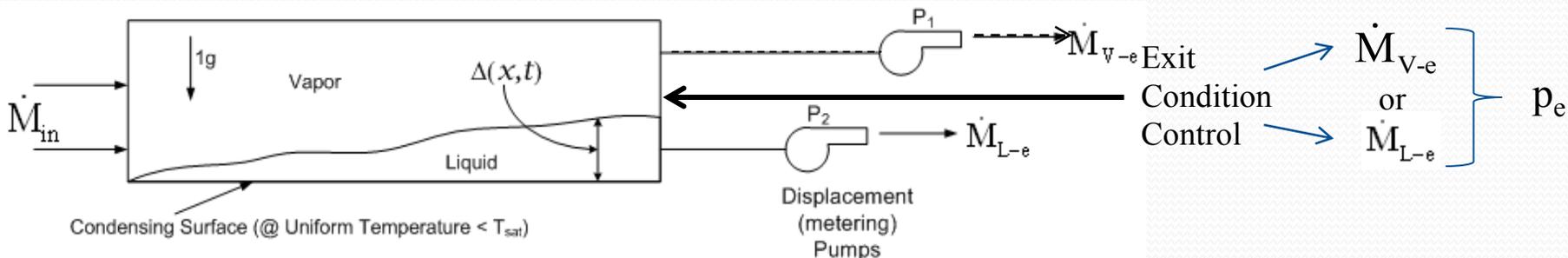
FUNDAMENTAL RESULTS ON “ELLIPTIC-SENSITIVITY” IN THE PRESENCE OF FLOW FLUCTUATIONS

- Theoretical and experimental results on “Elliptic-sensitivity” are presented for condensers.
- Analogous experimental results for boilers are expected within a year.

Shear/Pressure driven condensing (boiling?) flows exhibit a key phenomenon due to fundamentally different behavior compared to gravity driven flows. This is marked on our transition map for annular internal condensing flows



“Elliptic – Sensitivity” for Shear Driven Internal Condensing Flows (Consider Partially Condensing Annular/Stratified Flows)

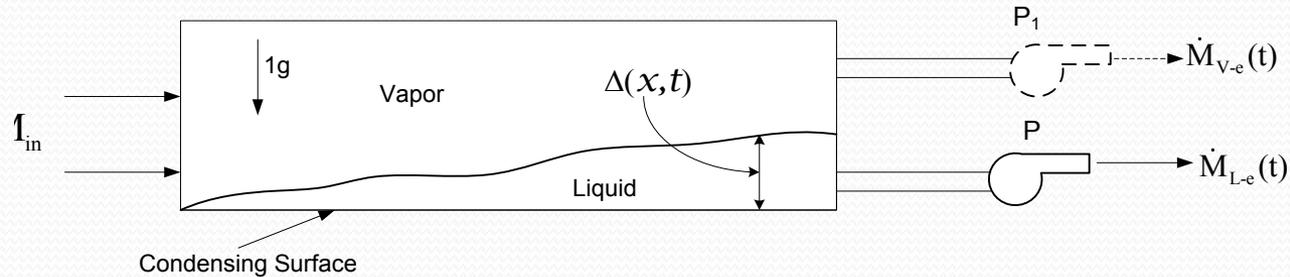


In the above thought experiment, one asks whether the exit condensate flow rate (\dot{M}_{L-e}) (or natural pressure difference Δp) can be changed to achieve multiple quasi-steady solutions (not necessarily annular/stratified). In other words: do these flows exhibit “elliptic-sensitivity” (i.e. do these flows listen to both upstream and downstream conditions) ?

- **Yes!** Because net mean energy into the control volume can be changed by a change in the interface energy transfer (associated with interface location and mass transfer).

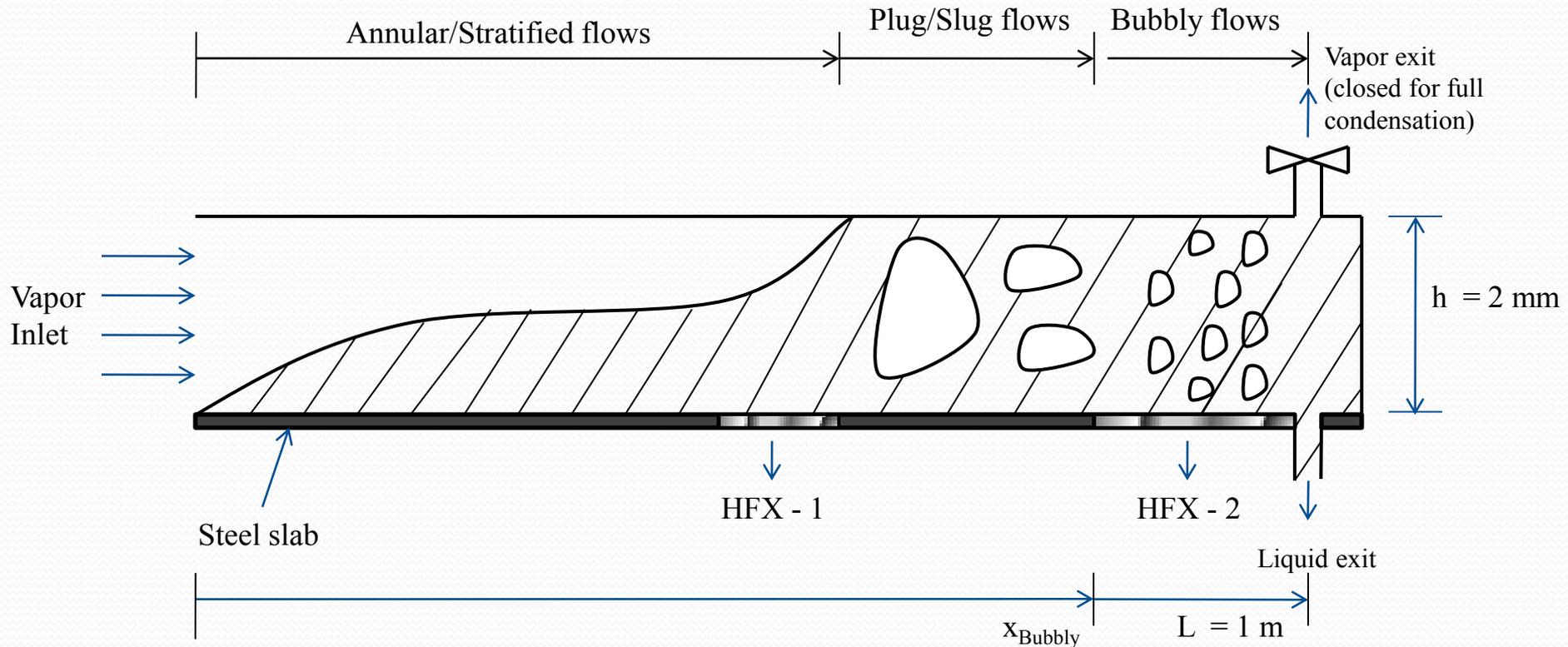
Clearly, the above different Δp impositions are impossible for single-phase flows or adiabatic two-phase flows (with zero interfacial mass transfer) because, the information only travels downstream (i.e. they are parabolic flows), and energy flow across the interface being zero

Basic Results on the Special Nature of Condensing Flows



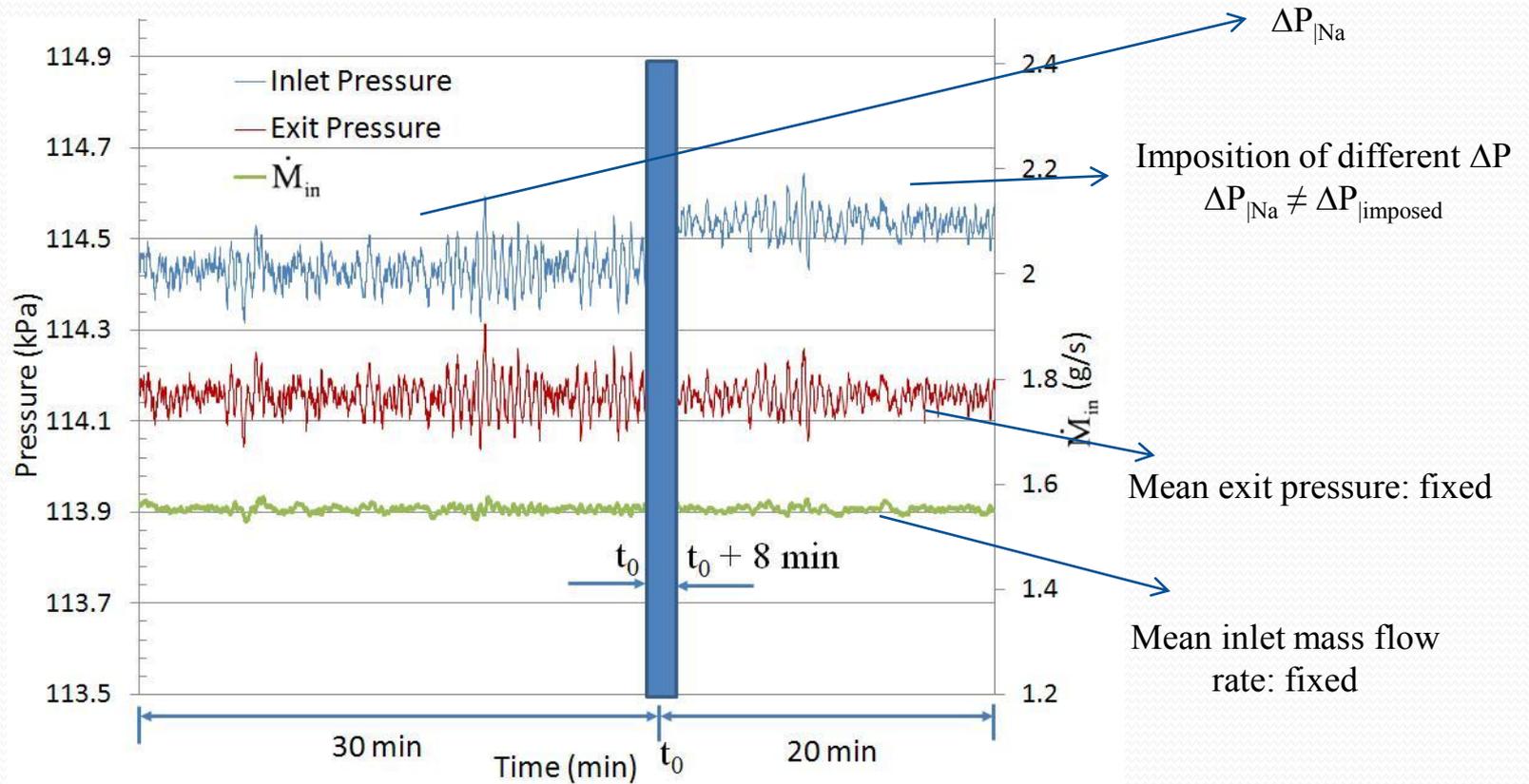
- For any internal condensing flow (shear or gravity driven), there is a unique steady (termed “natural”) annular/stratified (or “film” condensation) solution/realization which can be realized when the set up allows the flow to seek its own exit condition.
- However one can “actively” impose different steady or quasi-steady exit conditions - other than the “natural” one - for purely shear driven or “mixed” flows. This typically leads to other time dependent or quasi-steady solutions which may cause the flow regime boundaries (from annular stratified to non-annular (plug, slug, etc.) flows) to shift.

Test-Section and Schematic of the Observed Flow

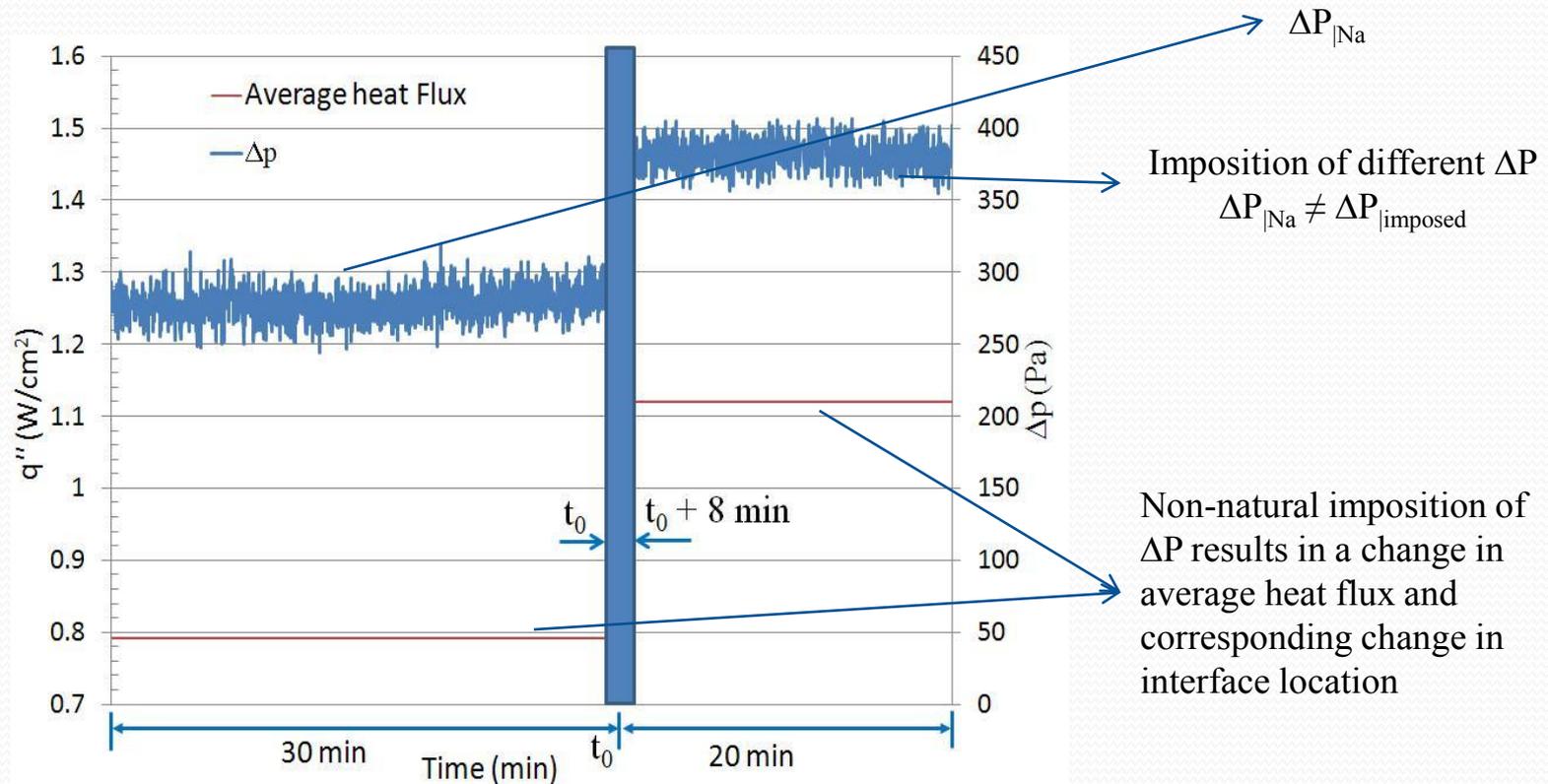


HFX - 1, HFX - 2: These are heat flux meters which have thermo-electric coolers underneath them.

Experimental Proof of Elliptic-Sensitivity

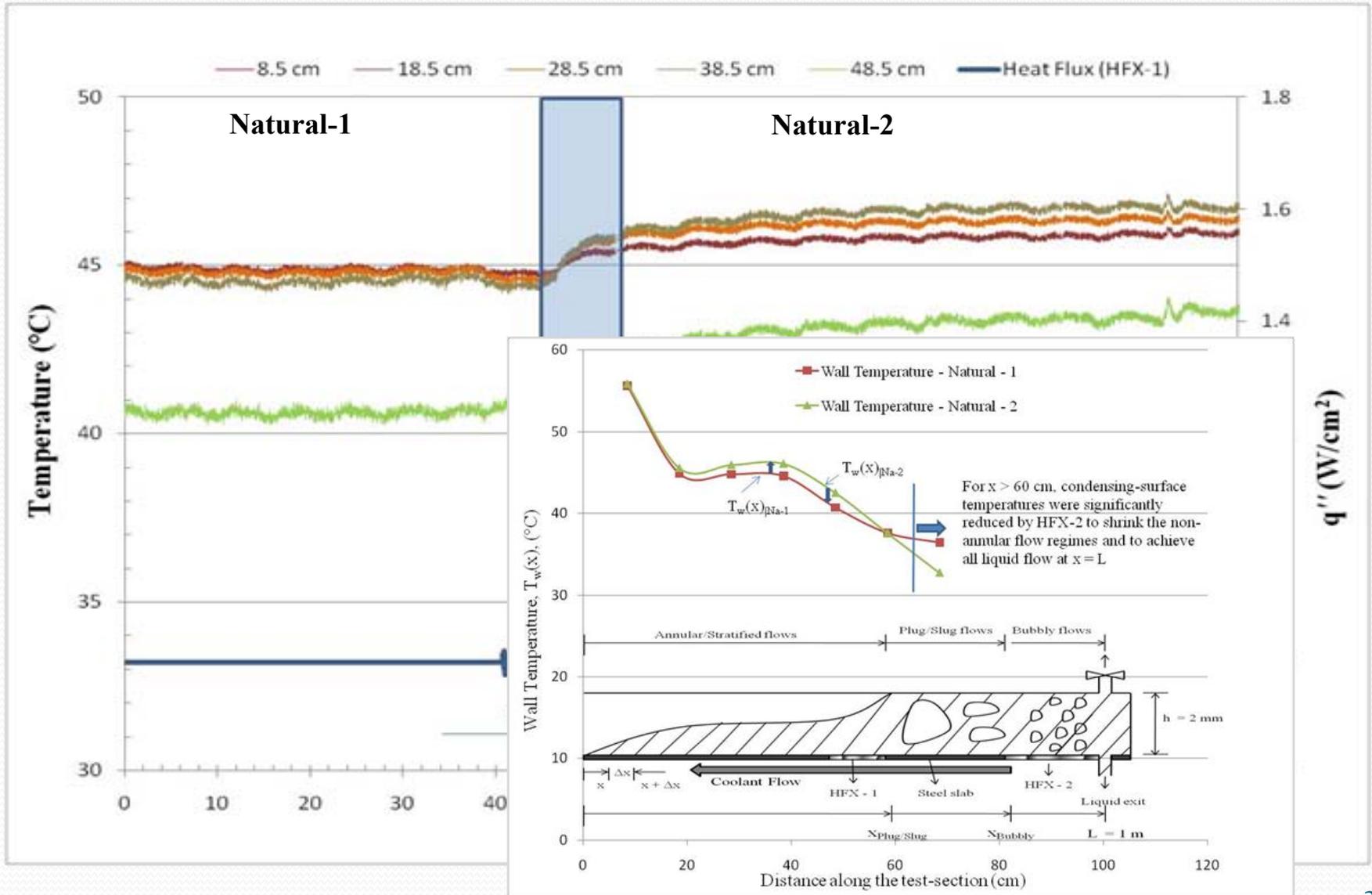


Experimental Proof of Elliptic-Sensitivity



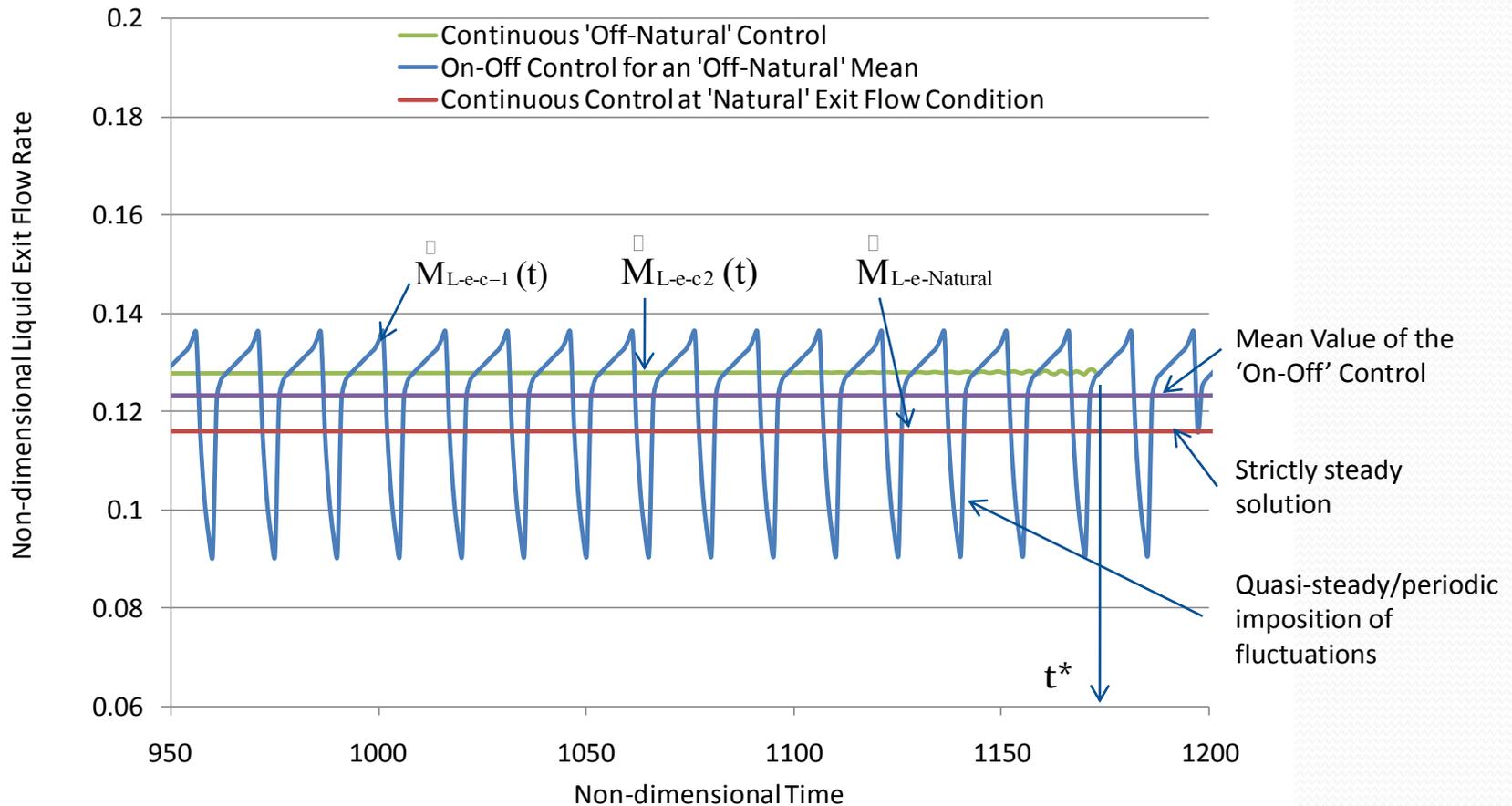
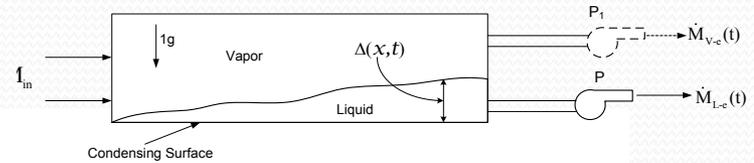
For this representative case, the 90 Pa change in Δp results in approximately 38 % enhancement in the average heat flux.

Experimental Proof of Elliptic-Sensitivity

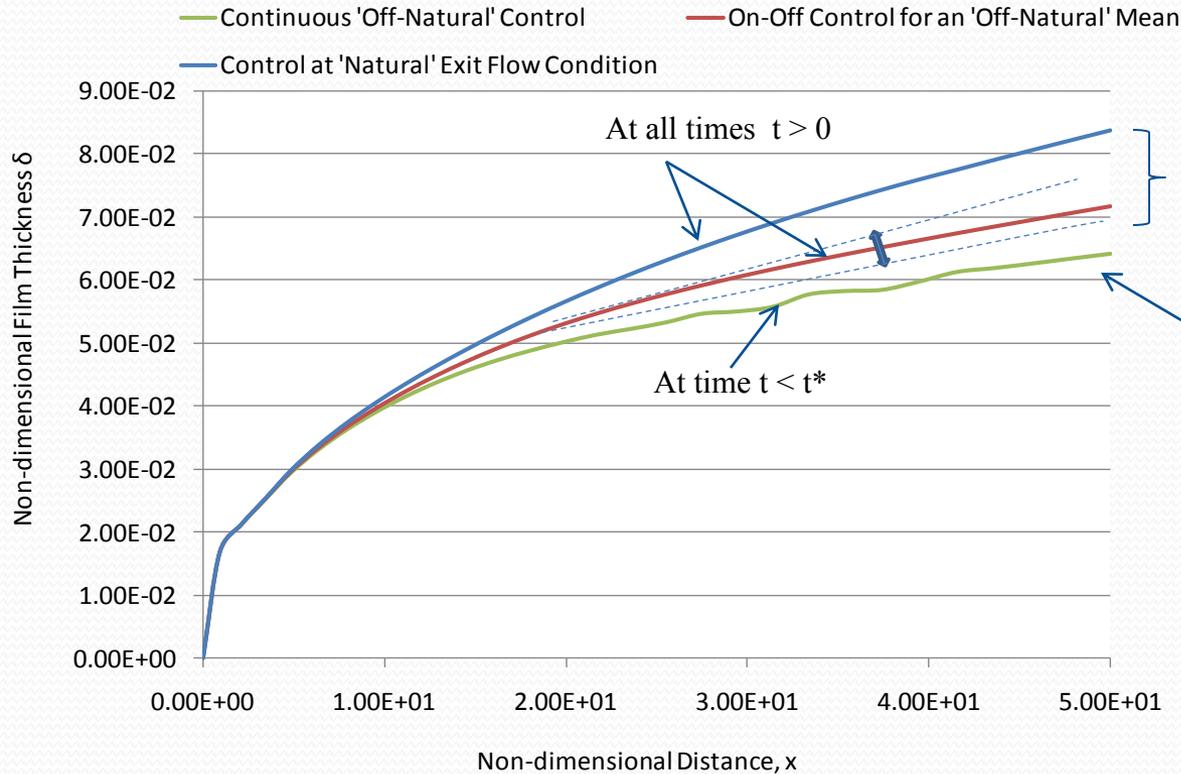


Theoretical/Computational Proof of Elliptic-Sensitivity

Input: Imposition of different $\bar{M}_{L-e}(t)$



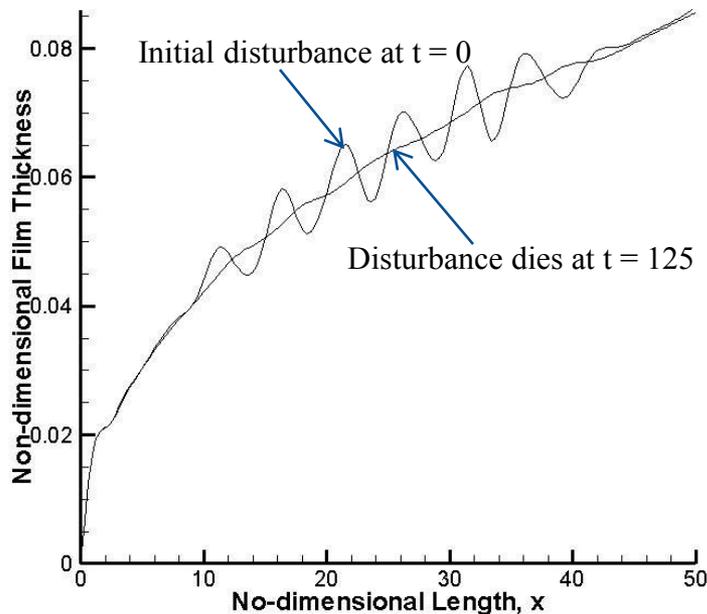
Control through Liquid Mass Flow Rate at the Exit



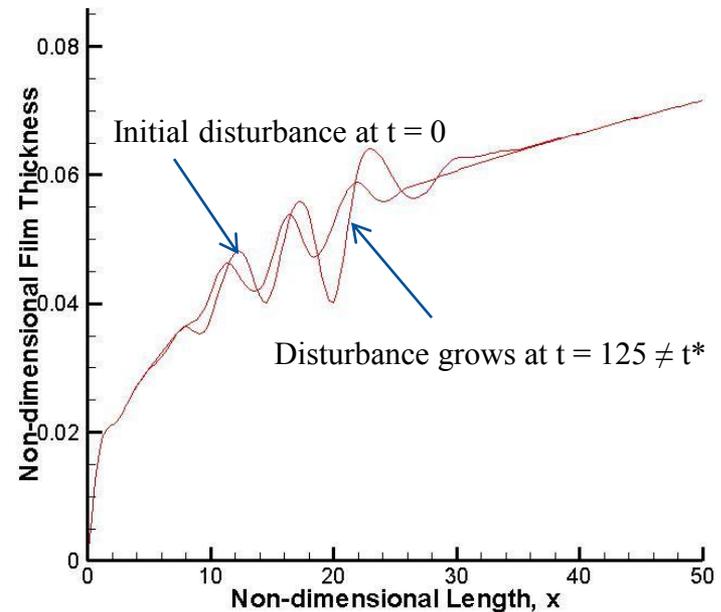
For all times annular/stratified solutions exist for these “special” controls at or near “natural” value.

Solution becomes non-annular at time $t > t^*$ (for $t > t^*$), no annular/stratified solution exists for all “off-natural” constant steady controls. This is further substantiated by the instability result for a constant steady control case with mean at an “off-natural” value.

Dynamic Stability at “Natural” and Instability for Continuous “Off-Natural” Control



Steady Imposition at „Natural“ is Stable

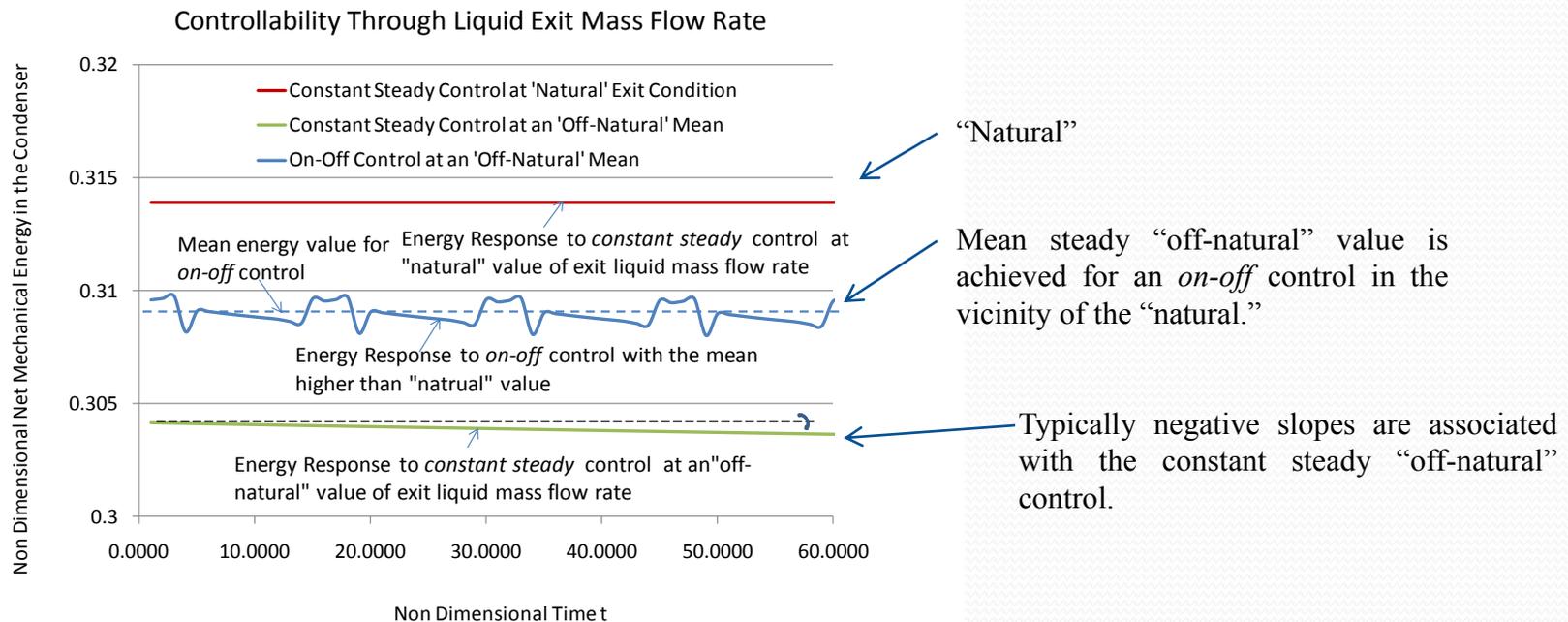


“Off-Natural” Steady Imposition is Unstable

But “Off-Natural” Quasi-Steady Imposition is Robust

Energy Response to Exit Condition Imposition

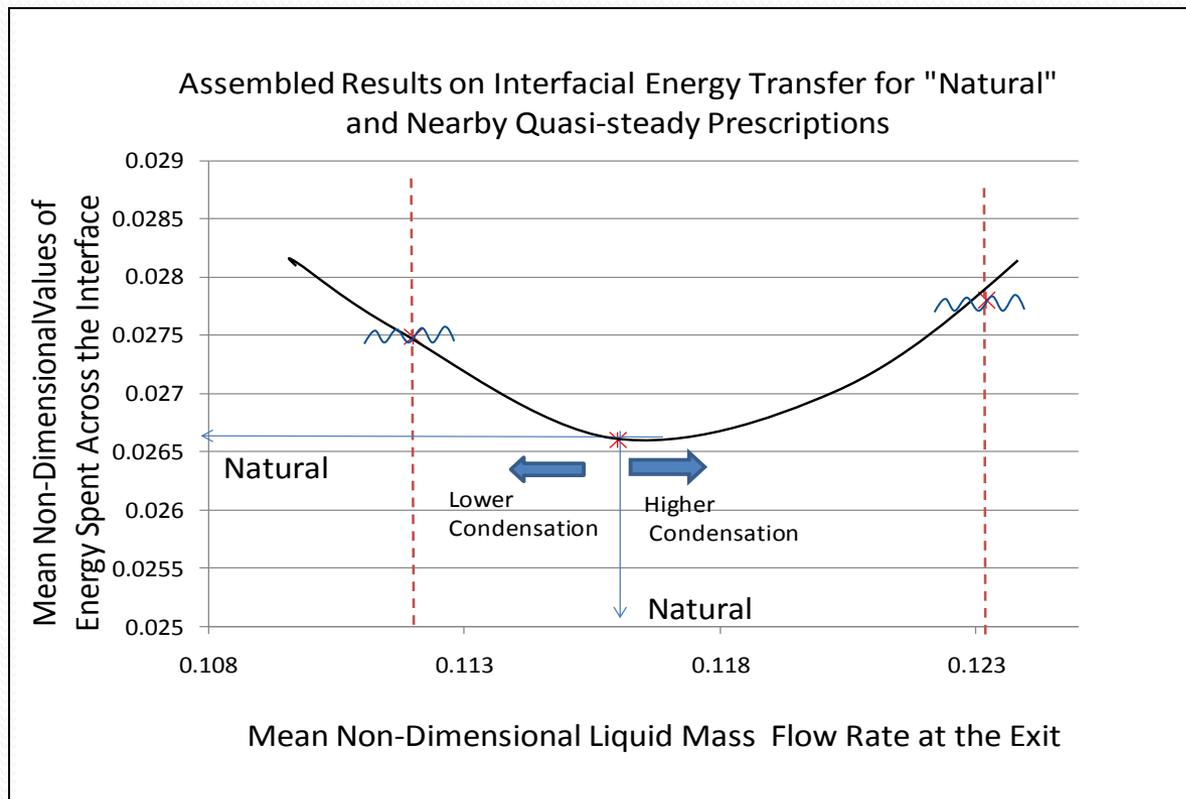
Consider: Non-Dimensional Net Mechanical Energy into the Condenser (Partial Condensation) versus time



- For constant steady control of exit liquid mass flow rate at “off-natural” value, energy keeps piling with a non-zero positive slope or draining inside the domain. This leads, eventually, to a situation
- where annular/stratified solutions do not exist after a certain transition time. These annular/stratified flows are unstable and only their transition behavior for negligible to non-zero initial disturbances can be computationally studied with the help of the current simulation technique.

Energy Response to Exit Condition Imposition

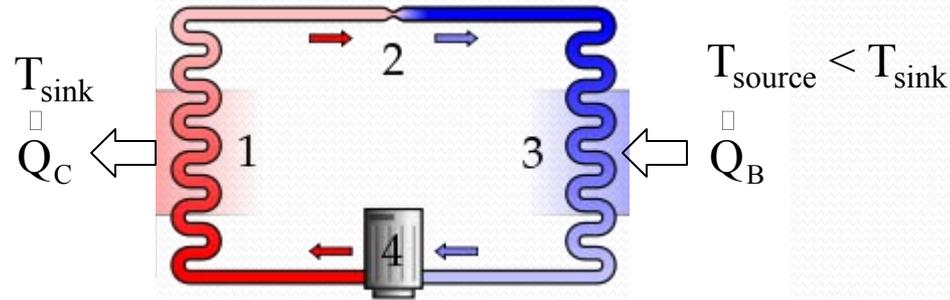
Consider: Mean Overall Interface Energy Transfer Rates (Non-Dimensional)
for Different Quasi-Steady Realizations



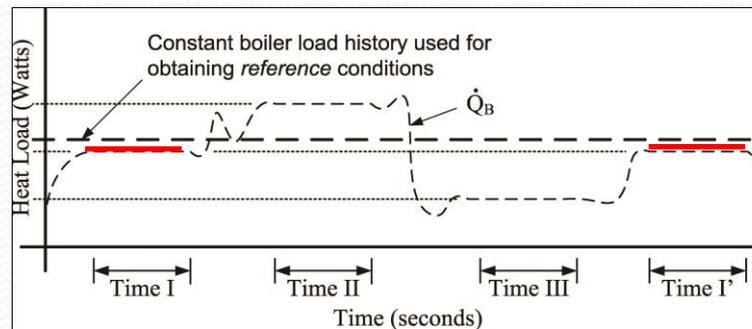
EFFECT OF ELLIPTIC-SENSITIVITY ON SYSTEM PERFORMANCE

(ONGOING AND FUTURE RESEARCH)

Implications of “Elliptic-Sensitivity” on System Level Repeatability



For the same steady \dot{Q}_B , M , T_{source} , and T_{sink} ; and a transient load history shown below, there could be significant drifts in boiler temperature for a given load history due to elliptic-sensitivity associated with the two-phase components.



That is, performance of boiler at **Time I** may not be same as that at **Time I'**.

Research Needs

- We need to learn what aspects of our facility can be altered/ upgraded to address issues of interest to ongoing *Air Force-Fairchild Corporation's* CRADA.
- We would like to collaborate and learn from you. We can do this by doing experiments and simulations that are not covered by NSF (3 year grant on μm -scale condensing flows) and NASA (1 year grant on flow boiling) grants. The possibilities are:
 - i. Do a μm -scale tubular boiling experimental research of Air Force's interest.
 - ii. Collaborate with Air Force on putting our μm -scale boilers/condensers on a suitable shaker that model different g-force history segments of your interest. For this, we may need a miniaturization of our facility as well as change in our working fluid (from FC-72 to fluids of your interest). The new equipment can be developed at AFRL or MTU. However suitable shaker experiments can be performed by additions to the existing MTU facility.
 - iii. Provide simulation support for annular regime condensing/boiling flows under different g-force histories (e.g. on shakers, aircraft g-force history, etc.)
 - iv. Learn your planned system and flow control details to see how “elliptic/parabolic sensitivity” issues discovered (and being developed) by us for flow condensation and flow boiling may be of assistance to you.



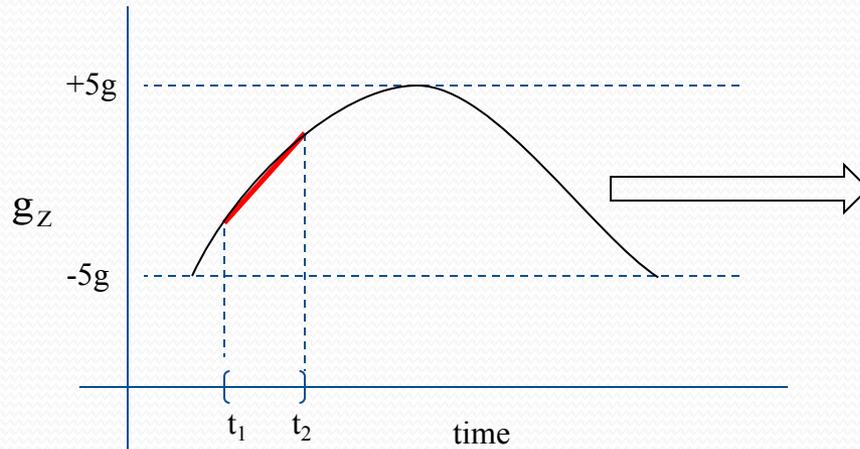
Conclusions

1. Novel “transition maps” for steady annular/stratified condensing flows yield a proper subdivision of the parameter space into gravity, shear, and mixed driven flow zones. This is of help in a-priori estimation of effects of changes in steady gravity levels.
2. For mm-scale ducts, the steady flow computational results as obtained from the 1-D/2-D solution techniques have been validated by comparisons with vertical tube experiments. Similar computational results and associated horizontal channel condensing flow experimental results are being synthesized.
3. “Elliptic-sensitivity” results for condensing flows (results for boiling flows are expected) were established both theoretically and experimentally. Its significance for controlling thermal transients and ensuring system level repeatability was discussed.

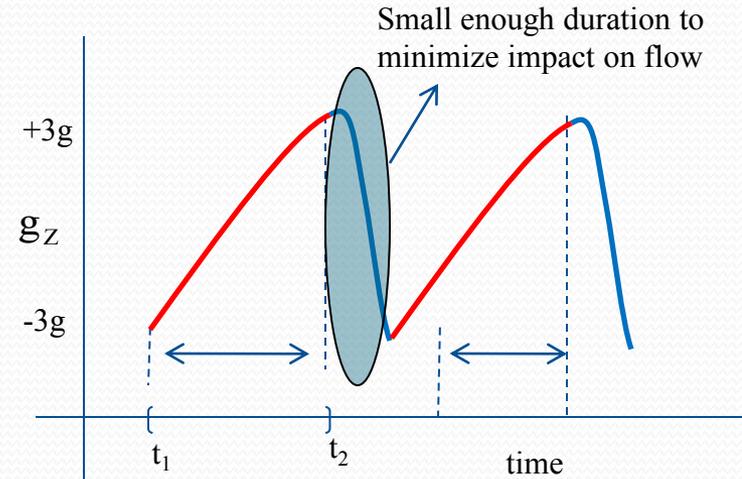
Thank You

Questions ?

Experiments Using a Shaker to Assess Gravity-Sensitivity



Sample g-force vector history for a particular aircraft maneuver in a vertical plane



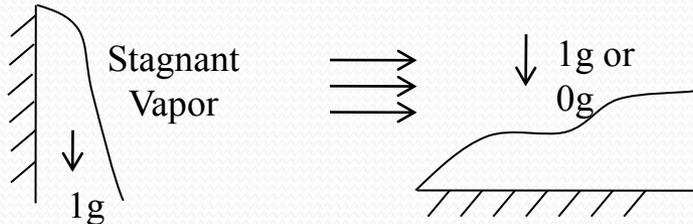
Representative $\bar{g}(t)$ profile for experiments

Can the response for any duration $[t_1, t_2]$ in an actual flight trajectory be assessed by mounting the boiler/condenser on a shaker with a periodic acceleration as shown above?

Available Knowledge/Literature

Fundamental Laminar/Laminar Solutions:

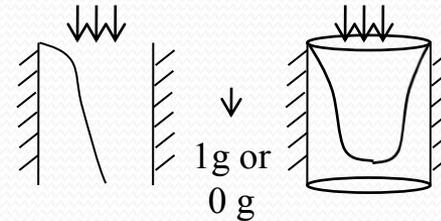
External Flows



Nusselt Problem [1914],
Narain et. al. [2007]

Koh Problem [1961],
Narain et. al. [2010]*

Internal Flows



(Narain et. al. [2004], [2009], [2010]*)

Experimental Investigations:

- Correlation for average heat transfer coefficients: (Cavallini et. al. [1974], Shah et. al.[1979], etc.)
- Flow regime visualization (Garimella et. al. [1999], Cheng et. al. [2005]), Flow regime maps (Carey [1992])

Internal Flows

Gravity Driven Flows ($D_h > 1 \text{ mm}$)

Mostly Annular

(Rabas et. al. [2000],
Narain et. al. [2009] – [2010]*)

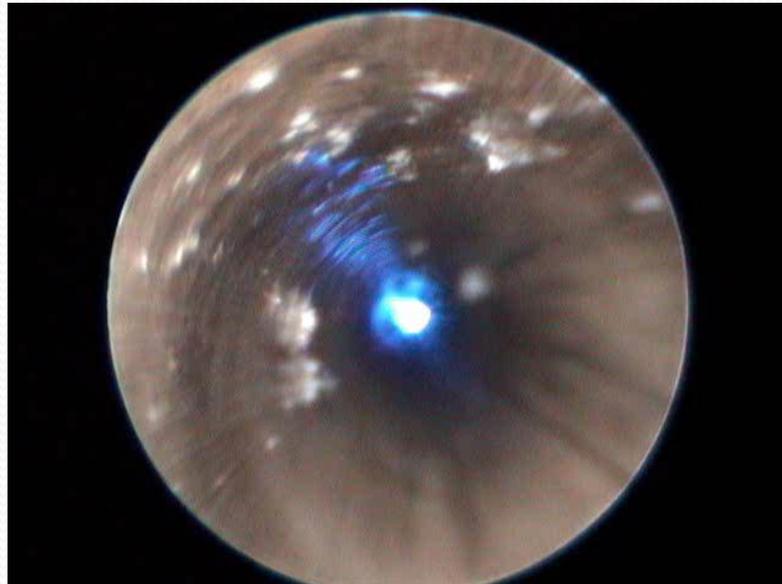
Shear Driven Flows

- Annular for:
 - Horizontal mm scale partially condensing flows
 - Small μm scale channel and cylinder with “surface tension effects”
 under “self-selected” exit conditions (Narain et. al. [2010]*).
- More commonly: Complex Morphology (Cheng et. al. [2005], Garimela et. al. [1999]), Narain et al. [2010]*

(?) ← Horizontal Tube (> mm-scale) → (?)

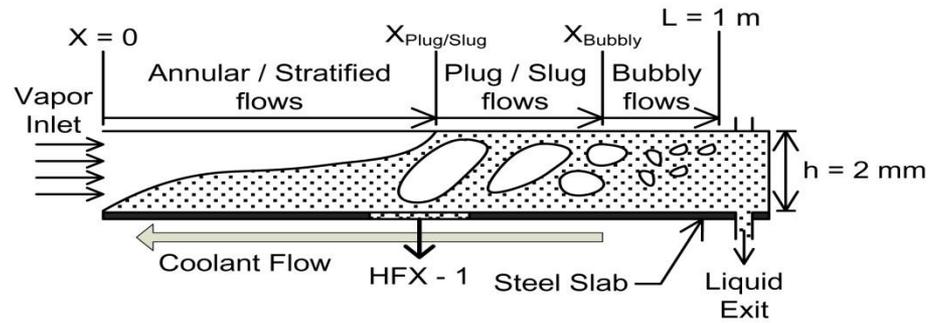
Internal Flows

Gravity Driven Flows ($D_h > 1$ mm)
Mostly Annular



(Narain et. al. [2009] – [2010]*)

Shear Driven Flows



Annular Flow

Research Tools that are Employed for Reported Results and Planned Research

Computational Simulation Tool

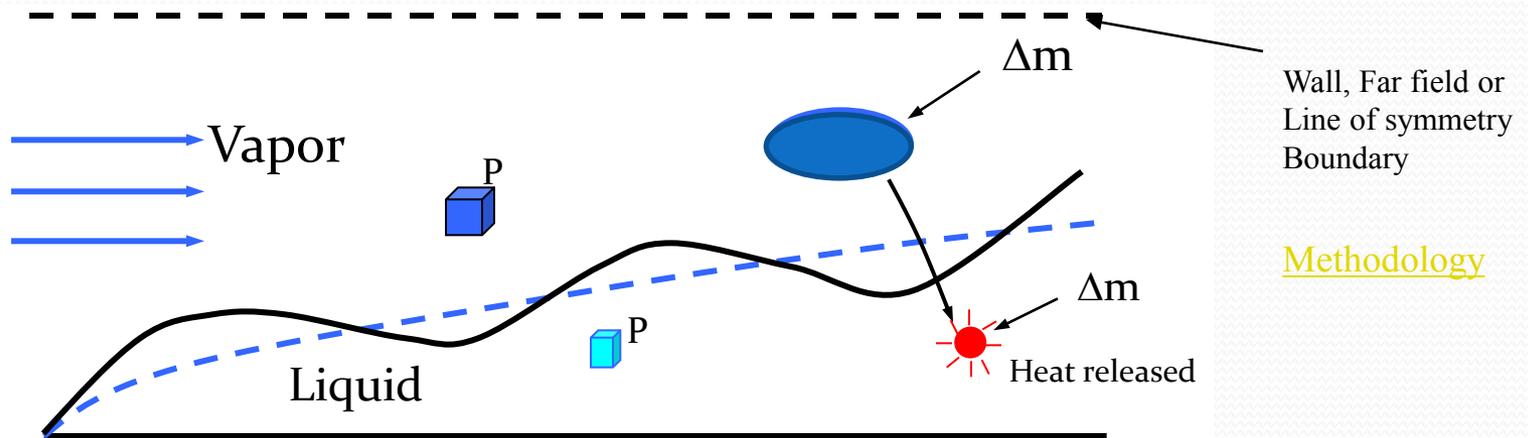
Experimental Flow Loop Facility 

Experiments
Fluid: FC72
Vertical Tube: $D_h = 6$ mm
 $2 \leq G \leq 90$ kg/m²-s
Horizontal Channel: $D_h = 2$ mm
 $2 \leq G \leq 200$ kg/m²-s

Newly Invented Film Thickness Sensor (Narain et. al., JHT, 2010)

First Principles Underlying Flow Physics and Computational Problem

- Continuum governing equations (Mass, momentum, and energy for each differential element in the interior of the two phases)
- Interface conditions (on the unknown interface these are restrictions imposed by: kinematics, mass transfer, momentum transfer, energy transfer, and thermodynamics)



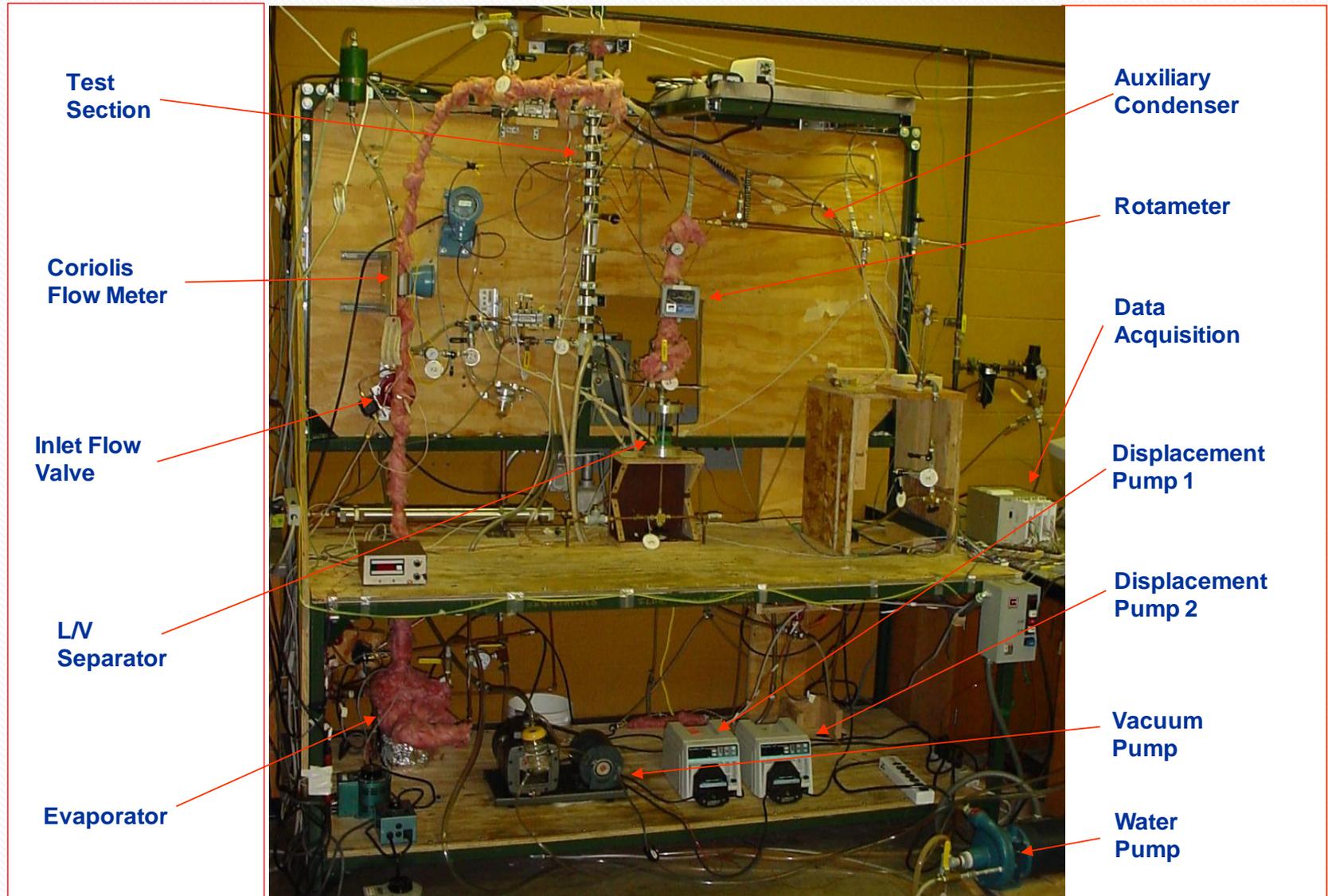
Other conditions

- Wall conditions
- Conditions at infinity (if any)
- Initial conditions ($t = 0$)
- Inlet conditions
- Exit conditions (need ?)

Special features

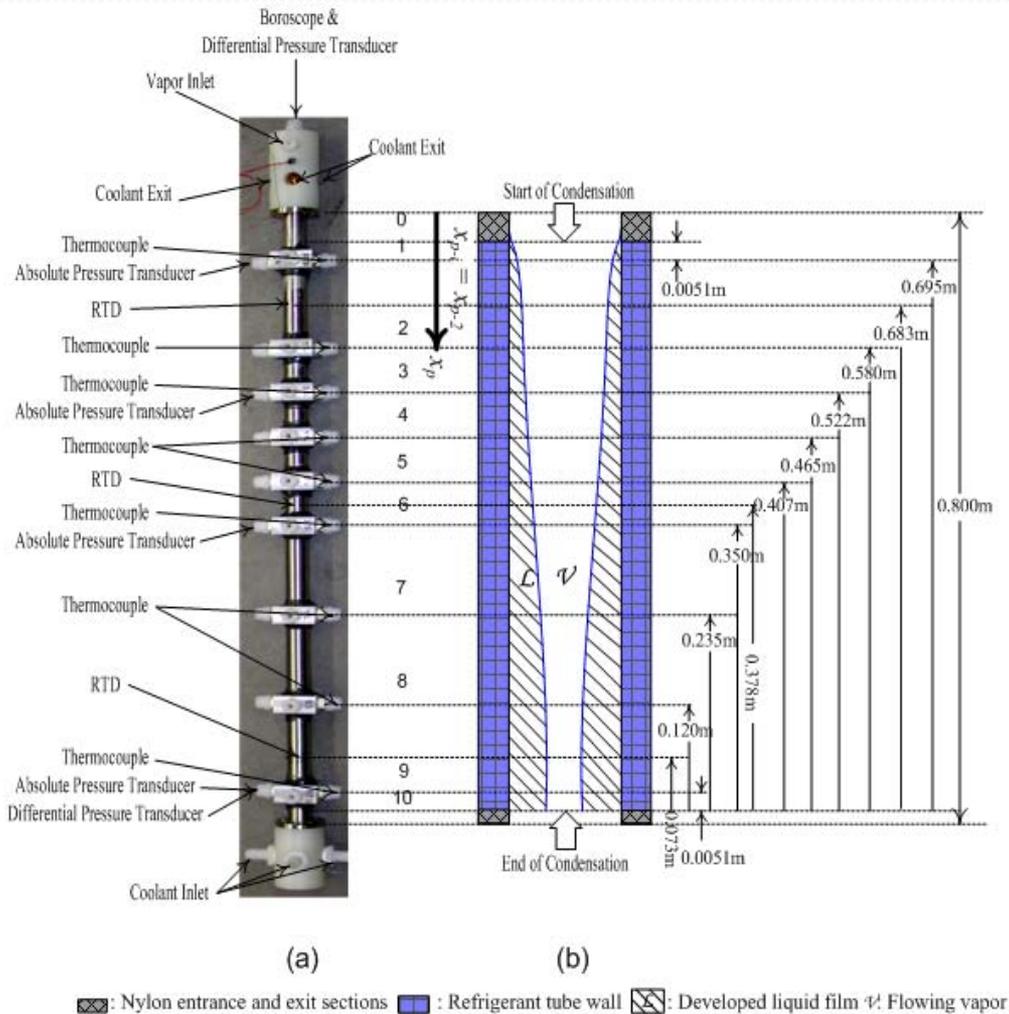
- Sharp interface
- Single-phase solutions interact through interface conditions
- Interface condition is used for interface tracking
 - Height function with adaptive grid (current)
 - Level-set function (planned)

Experimental Facility for Internal Condensing Flows

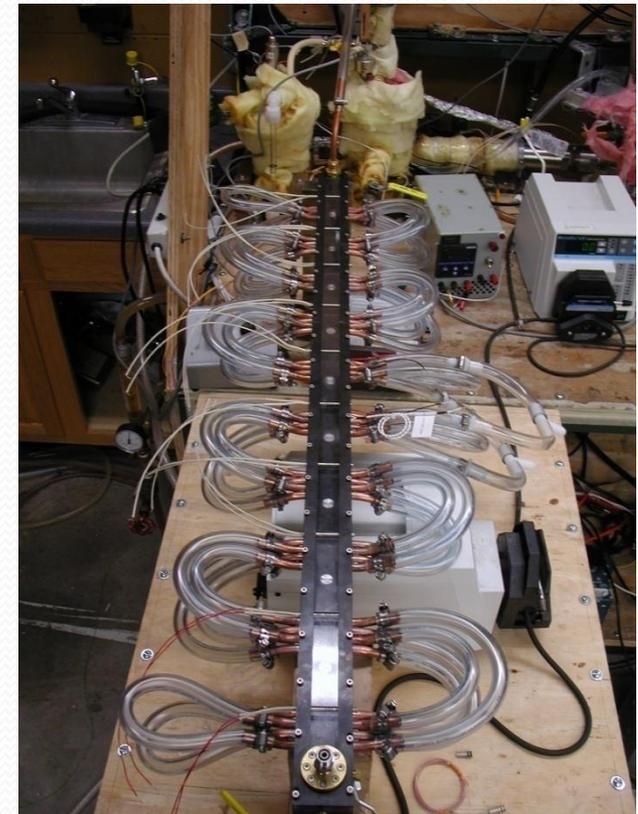


Experimental Test-Section

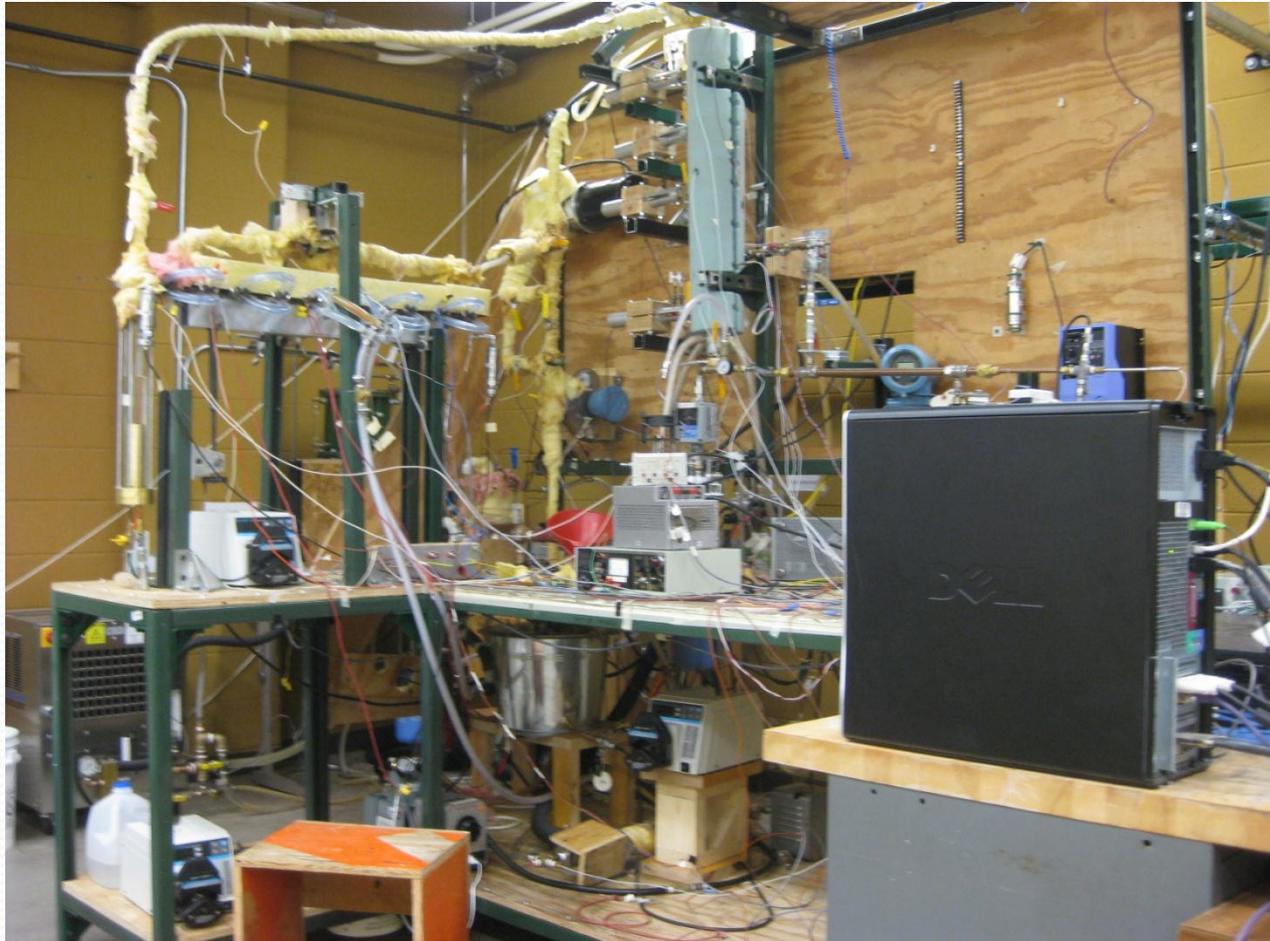
Vertical Tube



Horizontal Channel

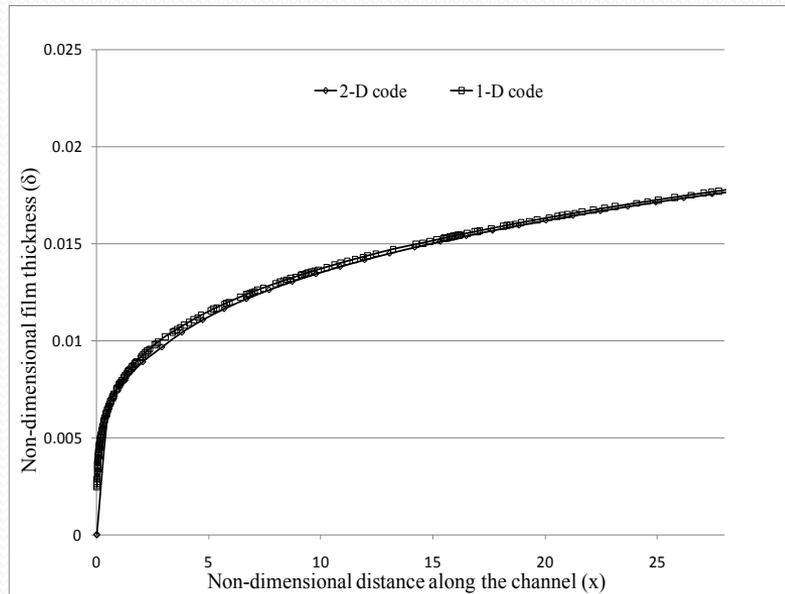


Combined Experimental Facility

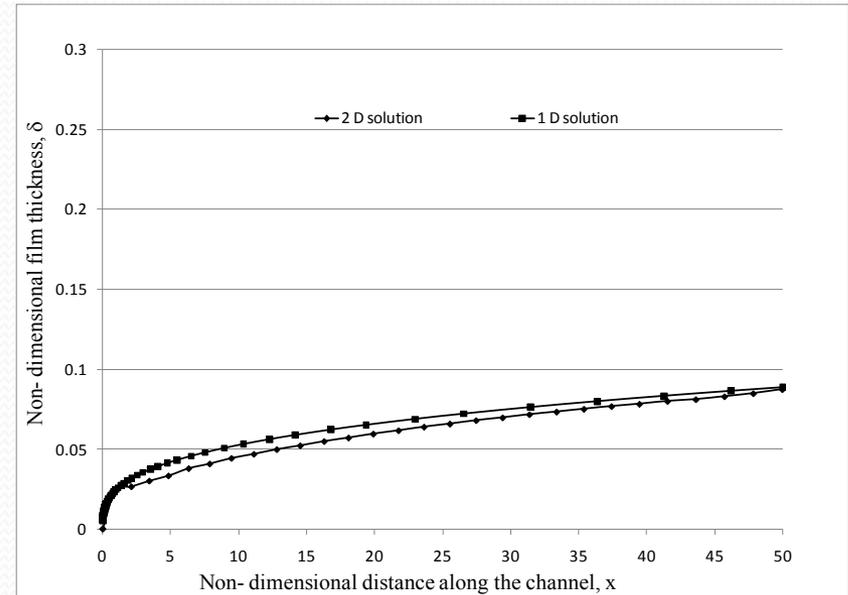


Comparison of Results Obtained by 1-D and 2-D Solution Techniques for Annular/Stratified Flows

Gravity Driven Flow
in mm Scale Vertical Ducts



Shear Driven Flow
in 0g, Horizontal, and μ m Scale Ducts



The 2-D and 1-D prediction for other flow variables (interfacial velocity, pressure, etc.) exhibit similar good agreements for different flow conditions and tube geometries as well. Within their own regimes, they also agree with experiments.

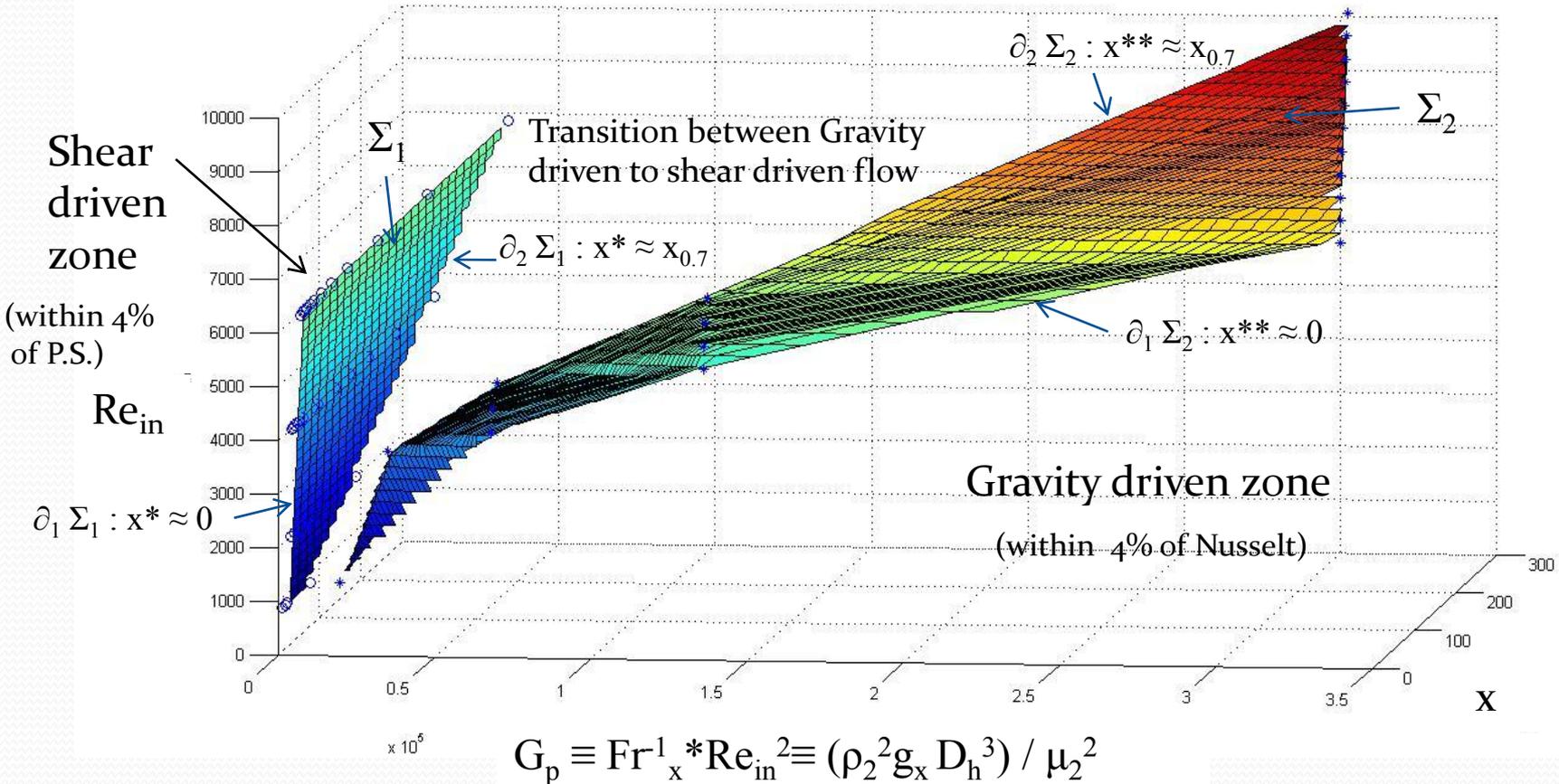
Both 1g and 0g flows are stable. Note: (i) gravity driven smooth flows become wavy for $Re_{\delta} > 30$, but they remain annular/stratified. (ii) Shear driven & 0g flows – though stable (as shown) are not always experimentally realized – except under “controlled” conditions.

COMPUTATIONAL RESULTS
ON
COMPARISONS BETWEEN
GRAVITY DRIVEN FLOWS AND SHEAR DRIVEN FLOWS

Transition Between Gravity Driven and Shear Driven Flows

Parameters affecting the flows: $\{x, Re_{in}, G_p \equiv Fr_x^{-1} * Re_{in}^2, Fr_y^{-1} = 0, Ja/Pr_1, \rho_2/\rho_1, \mu_2/\mu_1\}$

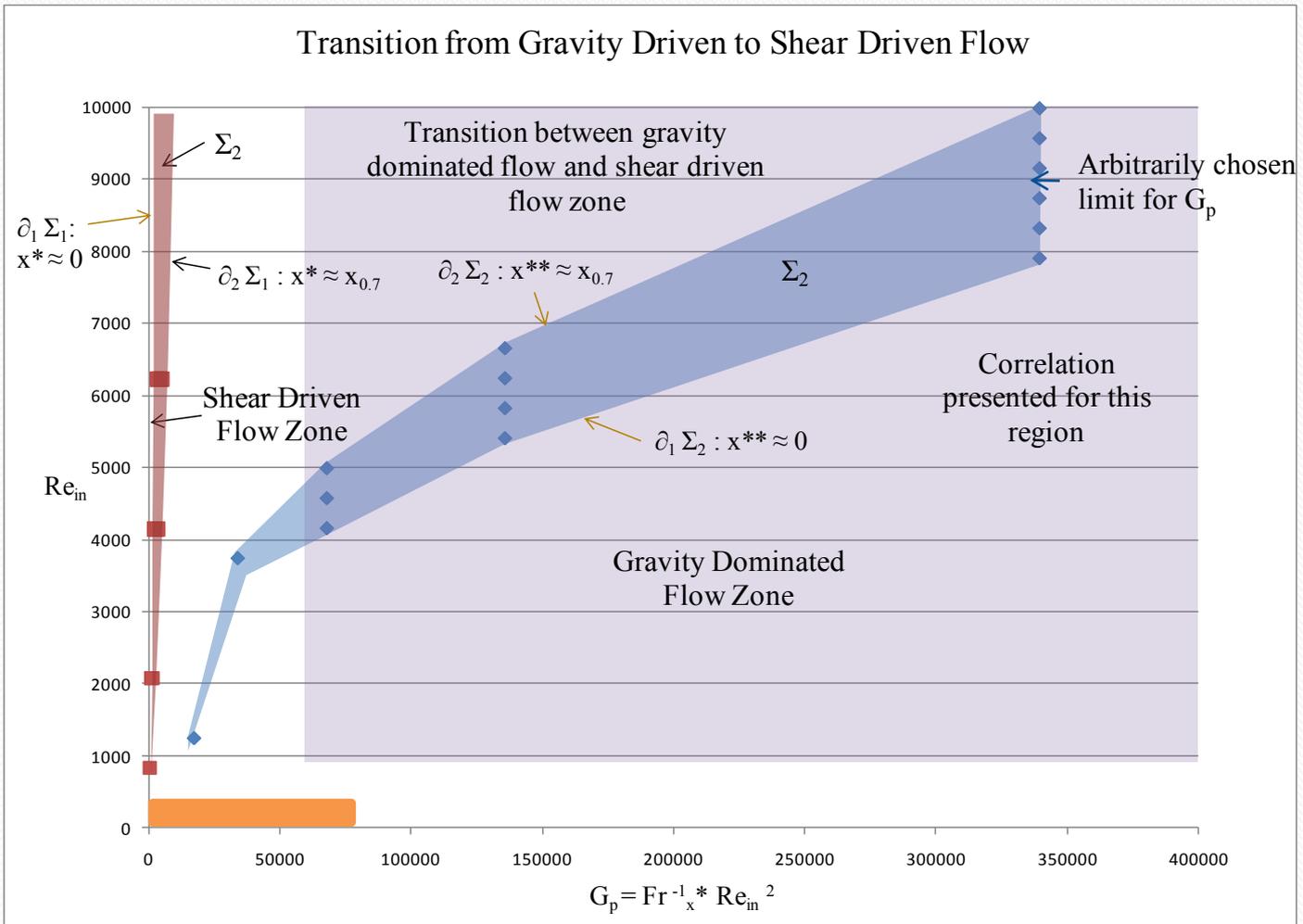
Method of Cooling: $T_w(x) = \text{Constant}$



Transition map in $\{x, Re_{in}, Fr_x^{-1}\}$ space for chosen $\{Ja/Pr_1, \rho_2/\rho_1, \mu_2/\mu_1\} = \{0.004, 0.0148, 0.0241\}$

Transition Between Gravity Driven and Shear Driven Flows

In the Re_{in} and G_p plane for a constant Ja/Pr_1 , ρ_2/ρ_1 , μ_2/μ_1



Projection of the Transition Map in Re_{in} - G_p Plane and Correlations for Gravity Driven and Shear Driven Flows

For 0g flows,

$$\delta_{ps}(x) = \frac{0.7487 * x^{0.35} * (Ja_1 / Pr_1)^{0.3611} * (\rho_2 / \rho_1)^{0.2380}}{Re_{in}^{0.3529} * (\mu_2 / \mu_1)^{0.5947}}$$

$$x_{0.75} = \frac{2.69 * Re_{in}^{0.1826} * (\rho_2 / \rho_1)^{1.1695} * (\mu_2 / \mu_1)^{0.1085}}{(Ja_1 / Pr_1)^{0.9911} * (Fr_x^{-1})^{0.5334}}$$

For gravity driven flows,

$$\delta_{Nu}(x) = \frac{1}{Y_c} \left[\frac{4 \cdot k_1 \cdot \mu_1 \cdot \Delta T \cdot x}{g \cdot \rho_1 \cdot (\rho_1 - \rho_2) \cdot h_{fg}} \right]^{1/4}$$

$$= [4 \cdot (Ja / Pr_1) \cdot (x / G_p)]^{1/4}$$

0g and other correlations (see paper) are for parameter space given by the following:

$$0 \leq x \leq x_A < x_{FC} \text{ or } 0 \leq x \leq x_{0.75}$$

$$900 \leq Re_{in} \leq 22000$$

$$0.0036 \leq Ja / Pr_1 \leq 0.0212$$

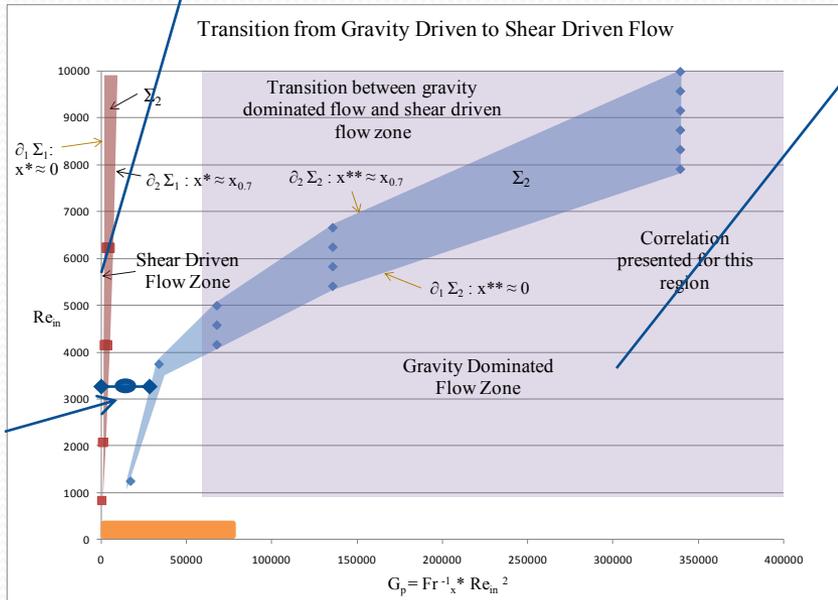
$$3.2E-4 \leq \rho_2 / \rho_1 \leq 0.03$$

$$0.0113 \leq \mu_2 / \mu_1 \leq 0.06$$

$$0.007 \leq Fr_x^{-1} \leq 0.01$$

$$Nu_x = (h_x * L_c) / k_1 = 1 / \delta$$

$$q''(x) = h_x * \Delta T$$



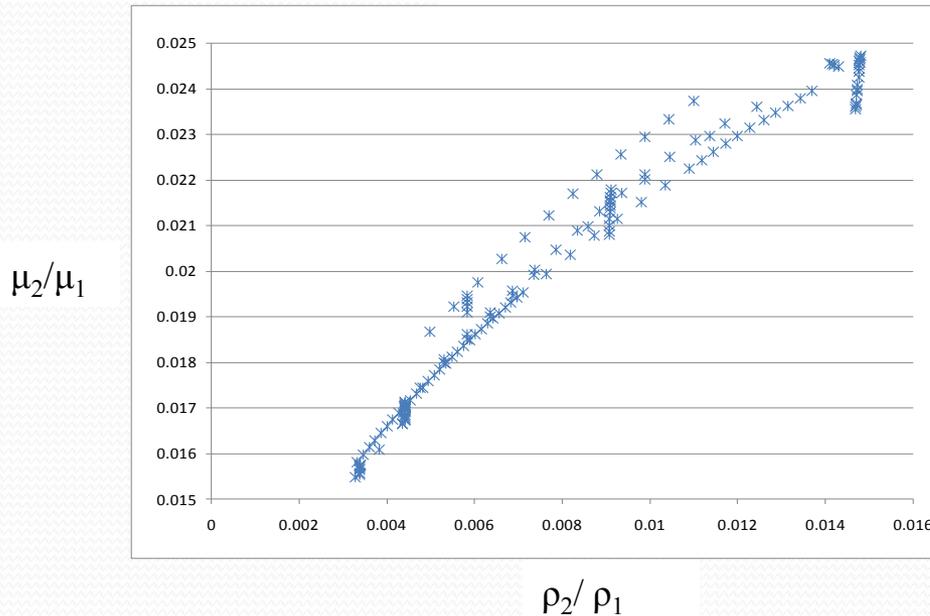
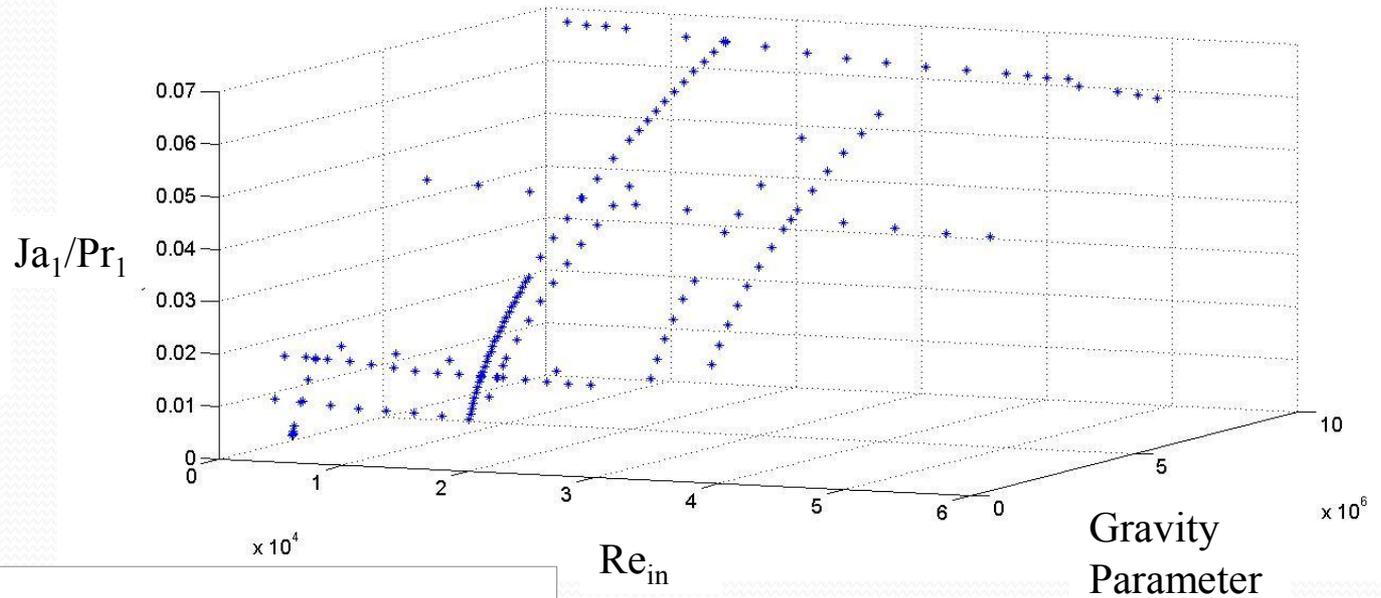
Error bar

$$G_p \equiv Fr_x^{-1} * Re_{in}^2 \equiv (\rho_2^2 g_x D_h^3) / \mu_2^2$$

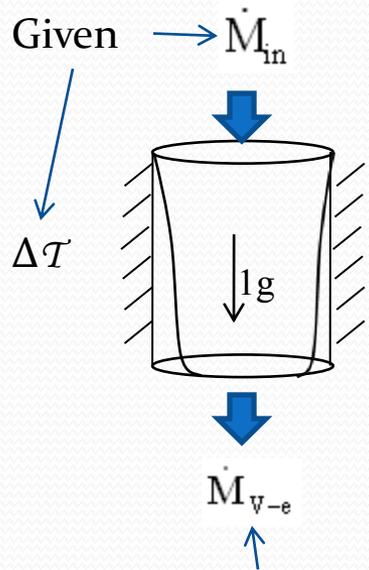
EXPERIMENTAL VERIFICATIONS FOR
GRAVITY DRIVEN FLOWS

Experimental Data Obtained for Fully Condensing Flows

Range of operating conditions and properties for the experimental data



Comparisons Between Theory and Experiments for Partially Condensing Flows (Annular/Stratified Regime)



is predicted and measured

where: $Z_e = \dot{M}_{v-e} / \dot{M}_{in}$

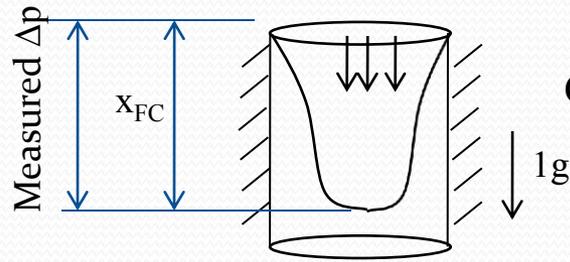
Run No.	\dot{M}_{in}	\dot{M}_v	Z_e	Z_e	Z_e	\bar{T}_w	T_{sat}	ΔT
	(g/s)	(g/s)	exp	comp 2-D	comp 1-D	(K)	(K)	(K)
	± 0.05	± 0.04	± 0.04			± 1	± 0.15	± 1
1	1.44	0.48	0.33	0.33	0.34	320	331.49	11
2	1.76	1.08	0.62	0.57	0.57	317	325.23	8
3	1.54	0.69	0.44	0.36	0.35	323	335.55	12
4	1.7	0.83	0.51	0.52	0.52	324	332.55	9
5	1.31	0.49	0.37	0.37	0.33	321	330.85	10
6*	1.93	1.39	0.72	0.72	0.76	322	325.55	4
7	1.59	1.11	0.69	0.63	0.62	328	334.25	6
8	2.12	1.37	0.64	0.64	0.64	320	327.85	8
9	1.3	0.45	0.35	0.38	0.42	321	329.29	8

Percentage agreement within $\pm 2\%$

Percentage agreement within $\pm 3\%$

[Annular Flow Regime Verification Video](#)

Comparisons Between Theory and Experiments for Fully Condensing Flows (Annular/Stratified Regime)



Given : \dot{M}_{in} and ΔT ➔ x_{FC} is predicted and measured
 Δp is predicted and measured

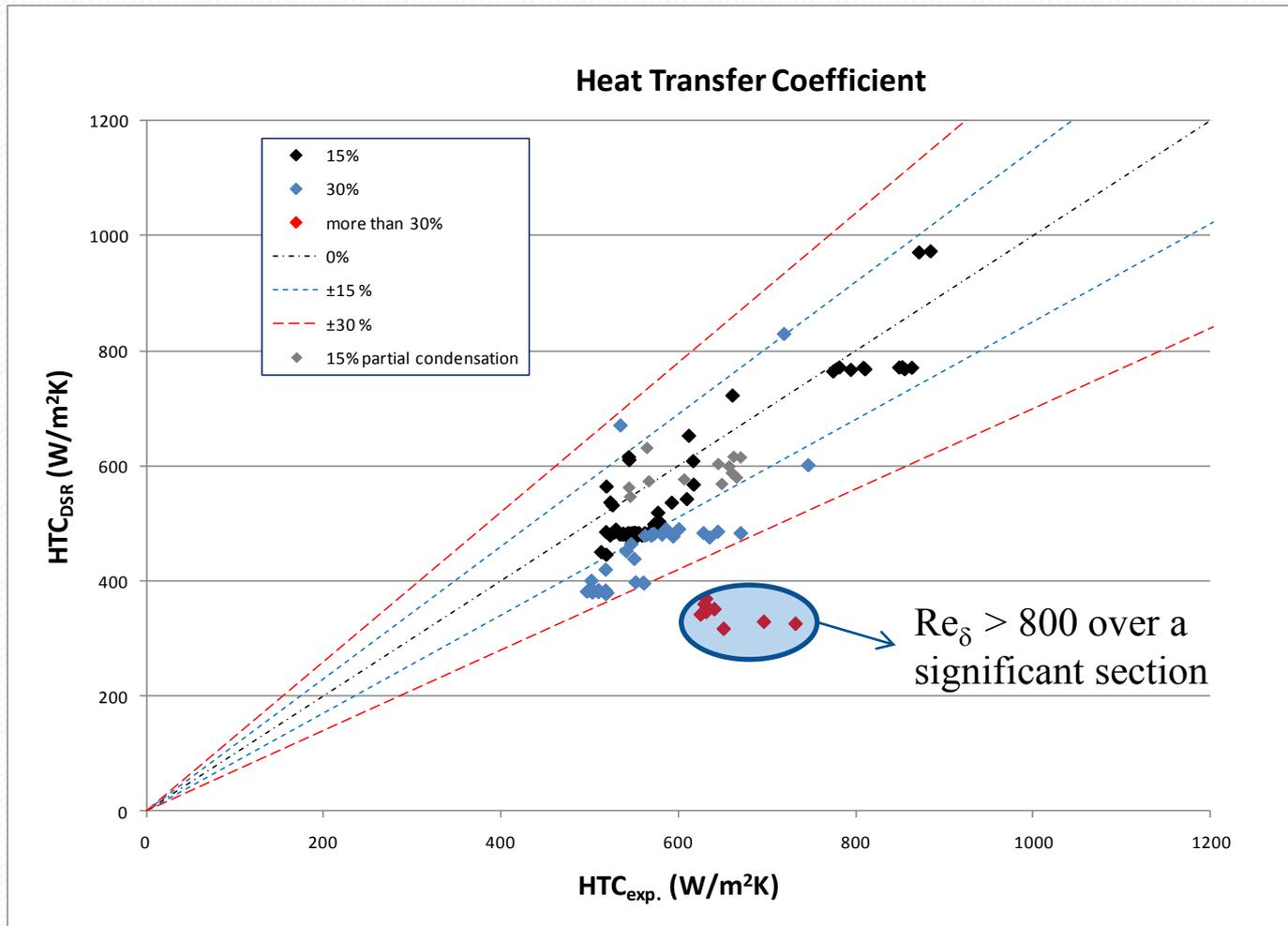
There is a good agreement between $\Delta p \equiv p_{in} - p_{exit}$ obtained both from experiments and predicted by quasi 1-D computational theory

Run No.	\dot{M}_{in} (g/s)	\bar{T}_w (°C)	T_{sat} (°C)	ΔT (°C)	p_{in} (kPa)	p_{XP-3} (kPa)	p_{XP-6} (kPa)	p_{exit} (kPa)	Δp (kPa)	Δp_{comp} (kPa)
	± 0.05	± 1	± 0.15	± 1	± 0.03 or ± 0.2	± 0.03	± 0.03	± 0.03	± 0.04	
1	0.86	31	71.27	40	162.52	162.72	164.08	172.37	-9.85	-8.84
2	0.854	36	75.21	39	182.29	182.36	184.43	193	-10.71	-8.34
3	0.852	31	75.9	45	187.16	187.15	189.26	198.1	-10.94	-8.69
4	0.72	26	70.36	44	156.91	157.26	159.72	167.62	-10.71	-9.14
5	0.71	29	73.01	43.7	170.69	171.39	173.86	182.32	-11.62	-9.08
6	0.7	26	69.03	42.6	151.85	152.55	155.04	162.76	-10.91	-11.28
7	0.852	31	76.2	45.2	187.16	187.15	189.26	198.1	-10.94	-8.73
8	0.861	33	75.5	42.7	183.67	183.82	184.22	192.3	-8.62	-8.51

The agreement is within $\pm 12\%$

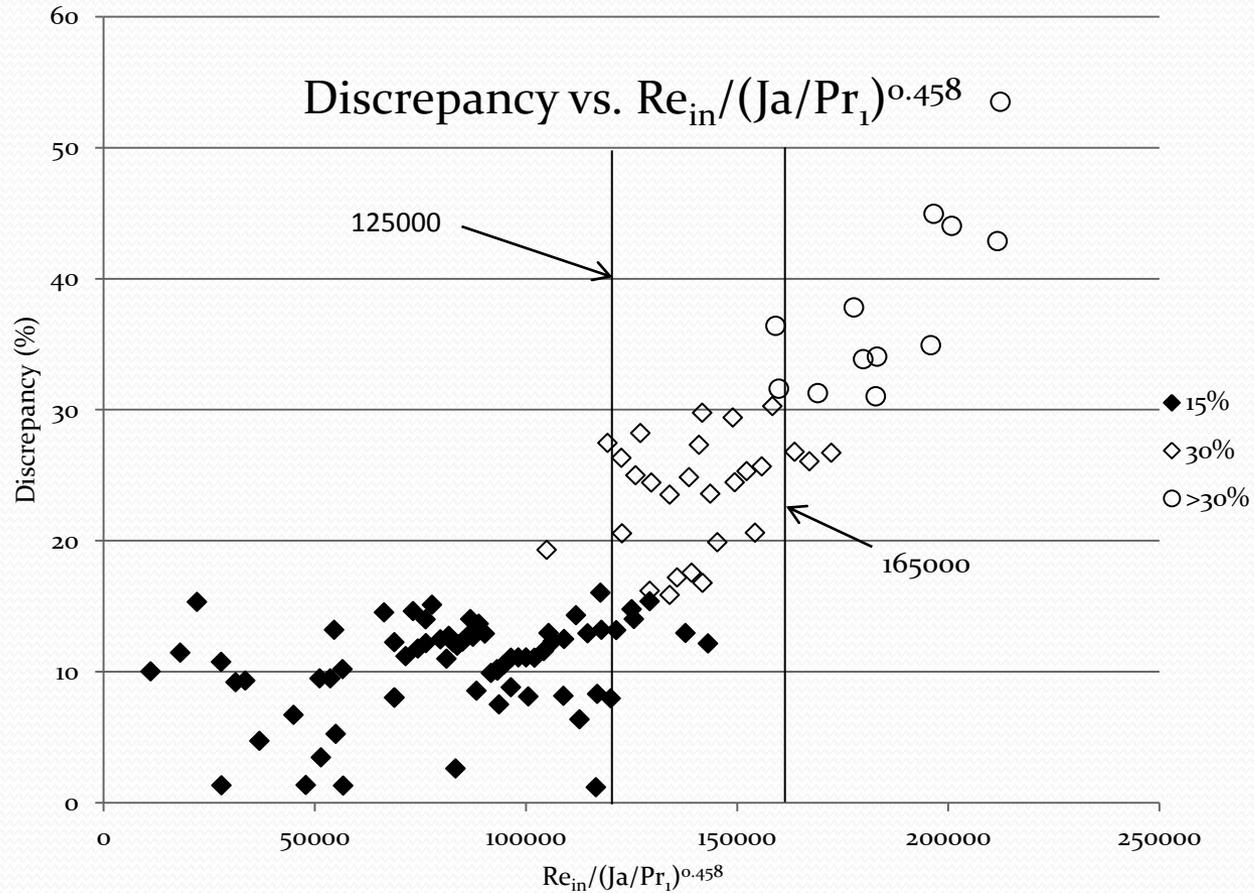
For shear driven cases, more detailed comparisons between theory and experiments is expected from a better instrumented horizontal rectangular test-section (forthcoming paper).

Comparisons Between Theory (1-D – No Waves) and Experiments for Fully and Partially Condensing Flows

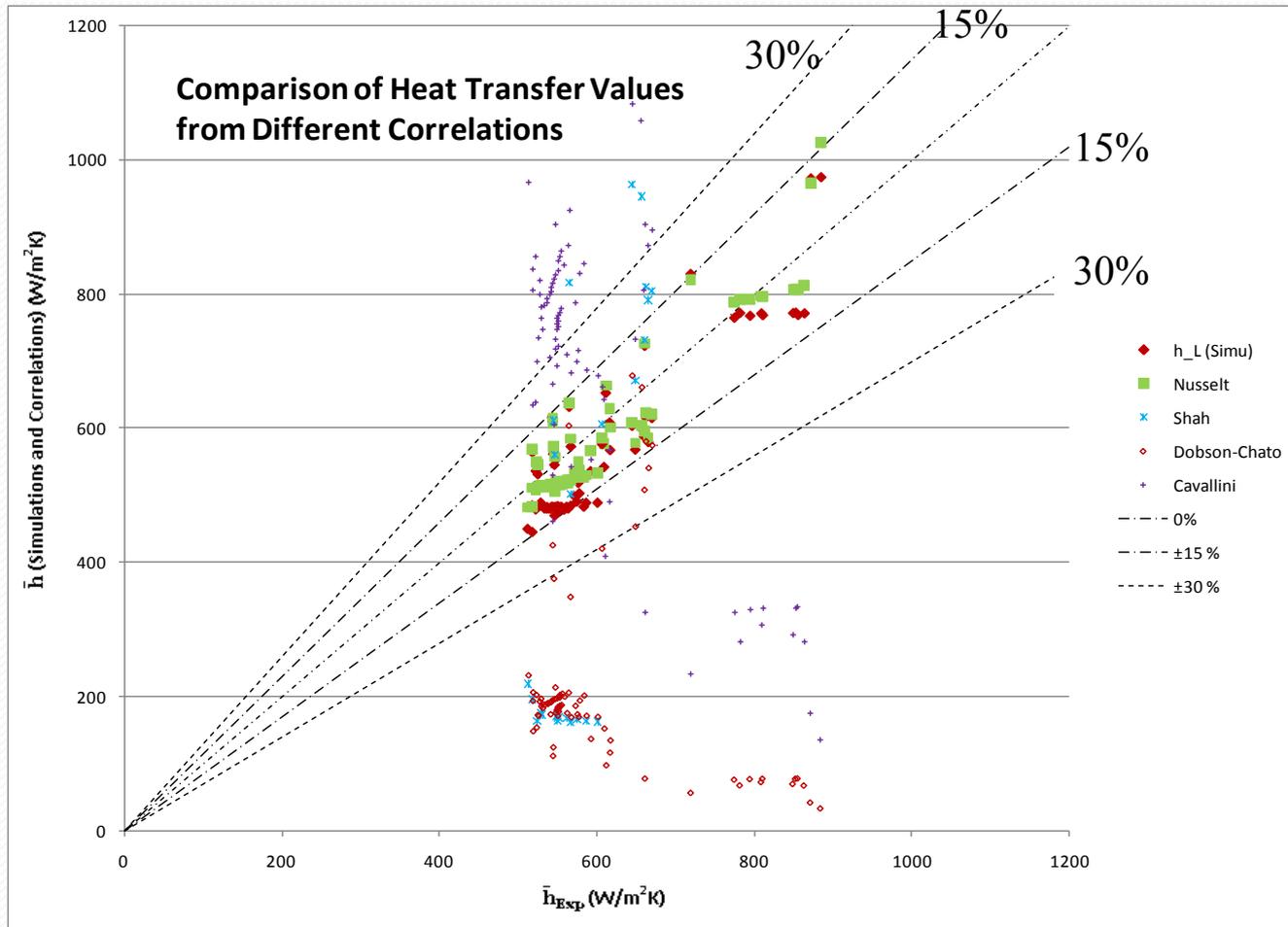


Better agreement with simulations with waves and turbulent effects are possible

Experimental Result Showing the Deviation from Laminar/Laminar Flow and Onset of Turbulence Near the Interface



Sample Comparisons of Experiments with Various Correlations for Partially Condensing Flows



Recommendation: Use Physics Based Sub-Categories

Parameters affecting the flows: $\{x, Re_{in}, G_p \equiv ((\rho_2^2 g_x D_h^3) / \mu_2^2), Ja/Pr_1, \rho_2 / \rho_1, \mu_2 / \mu_1\}$

Experimental correlations often replace: $\{x, Ja/Pr_1, Re_{in}\}$ by Re_δ and distance x by local value of vapor quality X or Z

Effectively, for common refrigerants, the parameters $(Re_{in}, G_p, Re_\delta)$ impose the following restrictions:

Re_{in} → Small: if $Re_{in} < Re_{cr}(x, G_p, Ja/Pr_1) \approx 50,000 \rightarrow$ Laminar Vapor model - OK
→ Large: if $Re_{in} > Re_{cr}(x, G_p, Ja/Pr_1) \approx 50,000 \rightarrow$ Vapor Turbulence becomes important

G_p → Small: if G_p is small (?) (μm -scale or $g_x = 0$) → Shear Driven Flows
→ Large: if G_p is large (?) (mm -scale or moderate g_x) → Gravity Driven Flows

Re_δ → Small: if $Re_\delta < Re_{\delta cr}(x, G_p, Ja/Pr_1) \approx 1,000 \rightarrow$ Laminar Condensate
→ Large: if $Re_\delta > Re_{\delta cr}(x, G_p, Ja/Pr_1) \approx 1,000 \rightarrow$ Turbulent Condensate

Annular Flow Correlations Practices

Method of Cooling: $T_w(x) = \text{Constant}$

Correlations	Low G_p	Moderate G_p	High G_p	Low Re_δ	High Re_δ	Low Re_{in}	High Re_{in}
Proposals based on this paper	■	■	■	■ ■ ■		■ ■ ■	
Cavallini [1974]		■		■		■	
Shah [1979]		■		■		■	
Dobson & Chato [1998]		■		■		■	
Azer et.al. [1971]		■		■		■	
Travis et.al. [1973]		■			■	■	
Soliman et.al. [1968]		■		■		■	

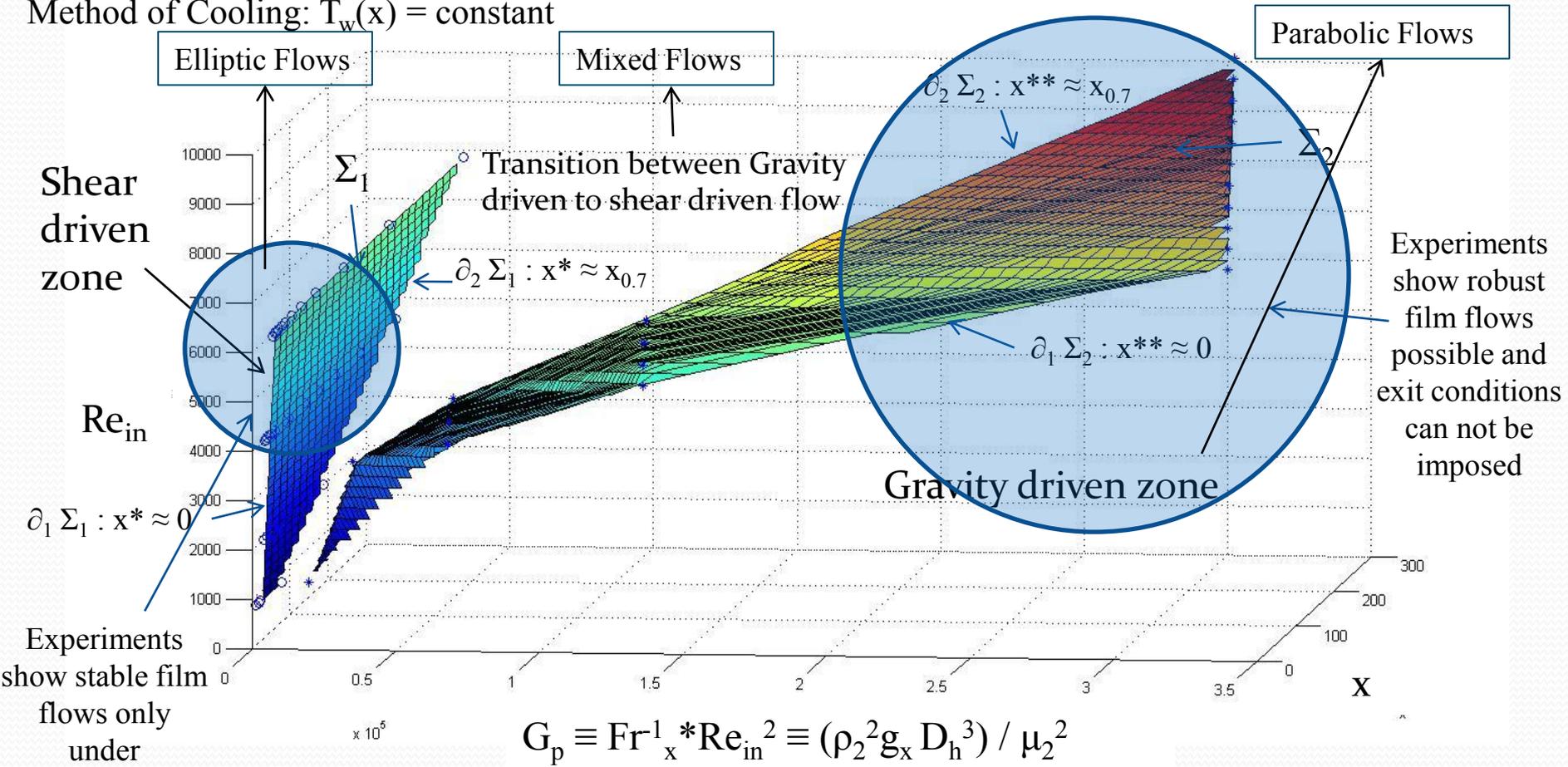
FUNDAMENTAL RESULTS ON EXIT-CONDITION SENSITIVITY AS A PART OF
BOUNDARY DATA , FLOW CONTROLLABILITY, AND FLOW REALIZABILITY

Assume Lam/Lam Flows & Look for Annular Flows

Transition Between Gravity Driven and Shear Driven Flows

Parameters affecting the flows: $\{x, Re_{in}, G_p \equiv ((\rho_2^2 g_x D_h^3) / \mu_2^2), Fr_y^1 = 0, Ja/Pr_1, \rho_2 / \rho_1, \mu_2 / \mu_1\}$

Method of Cooling: $T_w(x) = \text{constant}$

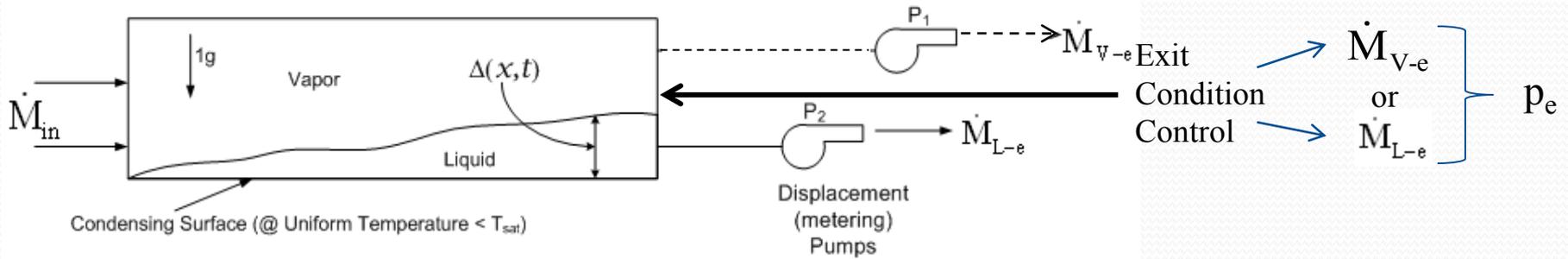


$$G_p \equiv Fr_x^{-1} Re_{in}^2 \equiv (\rho_2^2 g_x D_h^3) / \mu_2^2$$

Chosen $\{Ja/Pr_1, \rho_2 / \rho_1, \mu_2 / \mu_1\} = \{0.004, 0.0148, 0.0241\}$

The above maps takes the goals of Chen, Gerner, and Tien [1986] significantly forward.

Exit Condition Issue for Shear Driven Internal Condensing Flows (Consider Partially Condensing Annular/Stratified Flows)



In the above thought experiment, one asks whether the exit condensate flow rate (\dot{M}_{L-e}) (or equivalent exit pressure) can be used to “control” the flow and achieve multiple quasi-steady solutions (not necessarily annular/stratified). In other words: are these flows “elliptic” (i.e. do these flows listen to both upstream and downstream conditions) ?

- **Yes!**

Clearly, the above “control” is impossible for single-phase flows or adiabatic two-phase flows (with zero interfacial mass transfer) because, the information only travels downstream (i.e. they are parabolic flows).

Related Issues/Questions:

- What is the nature of the steady governing equations? Are they parabolic (as in single-phase or air-water flows)?
- Are there significant differences between gravity-driven and shear-driven flows?

Summary of Results

The basic result on “ellipticity” is:

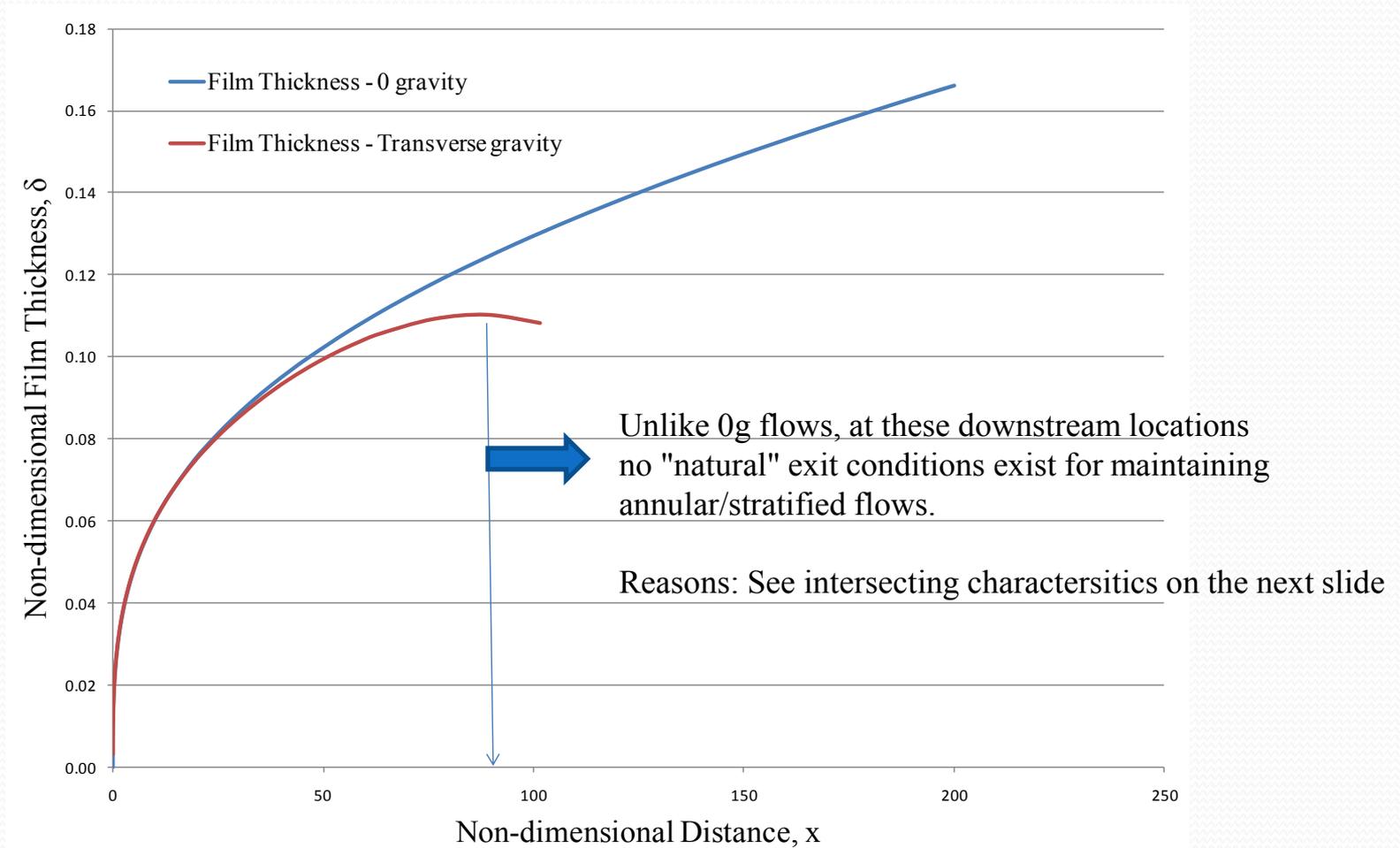
- Requires “exit” boundary conditions in general and responds to them.
- But, in the absence of external constraints, “parabolic” boundary conditions (i.e. inlet and wall boundary conditions) suffice for determining the “natural” unconstrained steady solution – not just the annular/stratified type but inclusive of other regimes (plug/slug, bubbly, etc.)

Experimental proof for stable and repeatable “natural” partially condensing shear driven flows

Experimental proof for stable and repeatable “natural” fully condensing shear driven flows

- Imposition of exit conditions- allowed for shear driven flows –changes the liquid/vapor morphology or interface locations and hence significantly changes heat transfer coefficient (or thermal resistance $R_{\text{condensation}}$ for condensing flows). This fact is being experimentally proven.

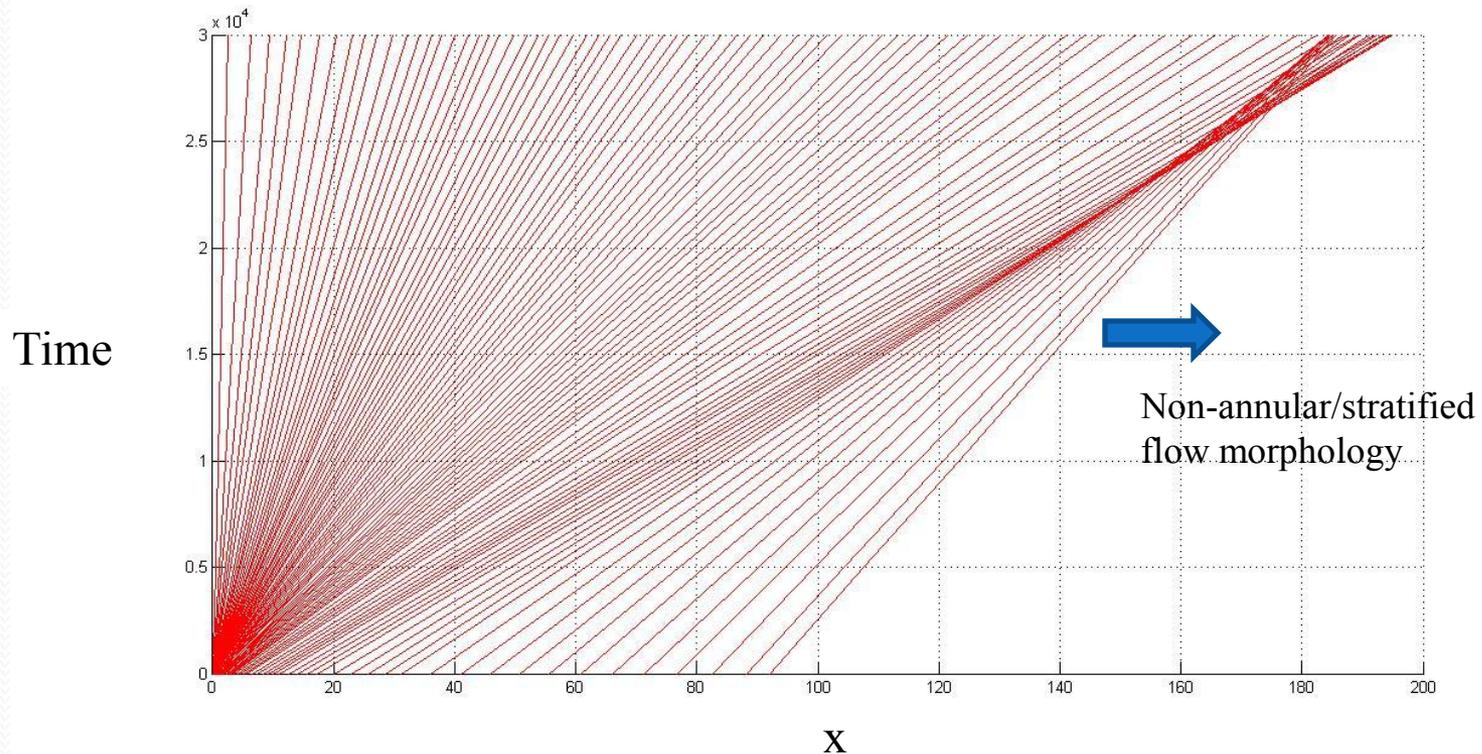
Differences between Shear Driven Flows in 0g Channel and Horizontal Channel



Annular/Stratified flow is not possible after $x > x^*$ (Ranjeeth et. al, 2010)

Shear Driven Flow in 0g Channel vs. horizontal Channel

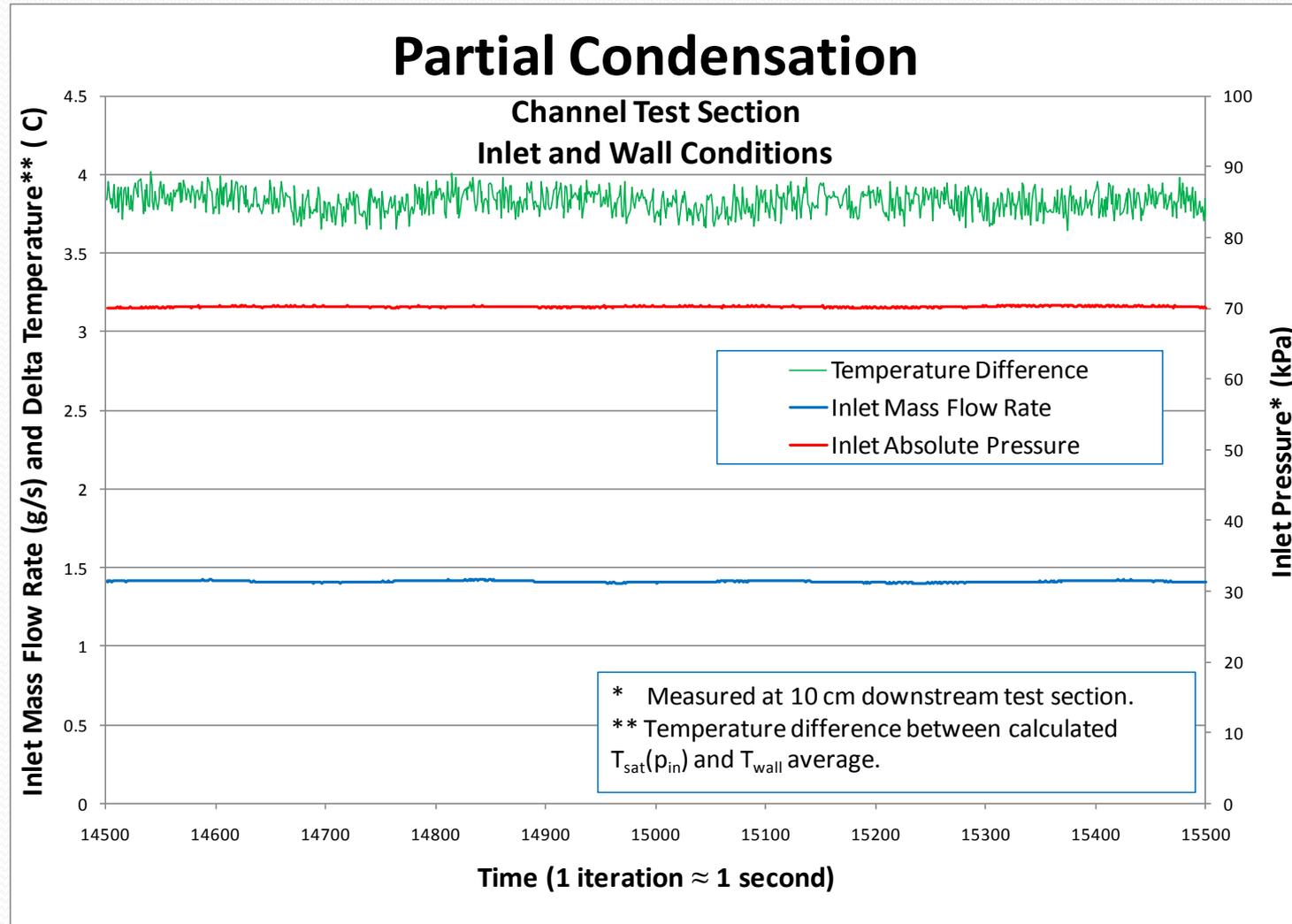
Study of Characteristics for flow in a 0g and horizontal channel



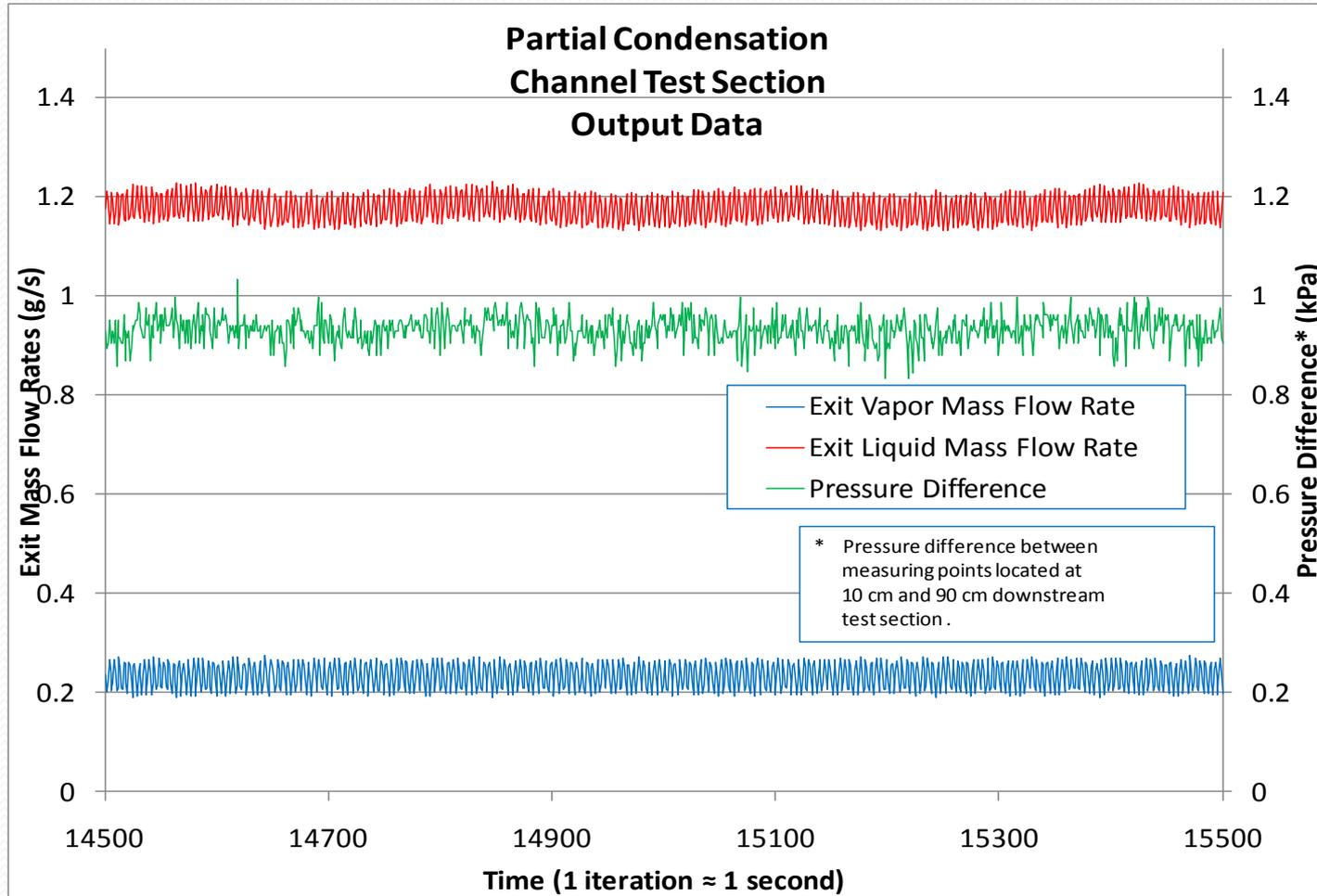
Annular/Stratified flow is not possible after $x > x^*$ (Ranjeeth et. al, 2010)

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Shear Driven Flows in a Horizontal Channel



Shear Driven Flows in a Horizontal Channel



[Morphology
Video](#)

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Comparisons Between Theory and Experiments for Fully Condensing Flows (Annular/Stratified Regime)

For a fully condensing flow (with $x_{FC} < L$), $\Delta p \equiv p_{in} - p_{exit}$ is obtained both from experiments and quasi 1-D computational theory



Run No.	\dot{M}_{in} (g/s)	\bar{T}_w (°C)	T_{sat} (°C)	ΔT (°C)	p_{in} (kPa)	p_{xP-3} (kPa)	p_{xP-6} (kPa)	p_{exit} (kPa)	Δp (kPa)	Δp_{comp} (kPa)
					± 0.03	± 0.03				
					or					
	± 0.05	± 1	± 0.15	± 1	± 0.2		± 0.03	± 0.03	± 0.04	
1	0.86	31	71.27	40	162.52	162.72	164.08	172.37	-9.85	-8.84
2	0.854	36	75.21	39	182.29	182.36	184.43	193	-10.71	-8.34
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The agreement is within $\pm 12\%$

More detailed comparisons between theory and experiments is expected from a better instrumented horizontal rectangular test-section (forthcoming).

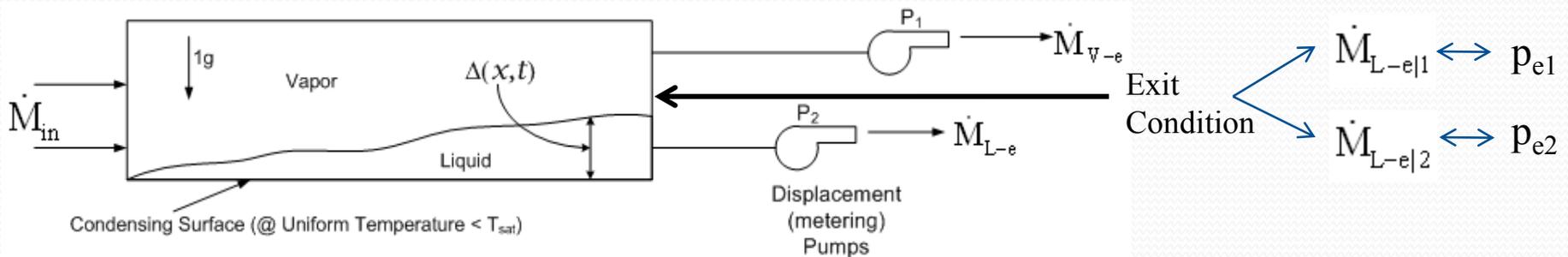
Conclusions

1. The novel proposed “transition maps” for annular/stratified flows show a proper subdivision of the parameter space into gravity, shear, and mixed flow zones.
2. For mm-scale range, the results – for both gravity and shear driven flows – as obtained from the 1-D solution technique were validated by successful comparisons with 2-D results as well as relevant experimental results.
3. The unique annular/stratified steady solutions define an exit condition which is termed as “natural.” For shear driven flows, unless “natural” exit condition is specified or is accessible, there could be other quasi-steady/unsteady realization of the governing unsteady equations because of inherent exit condition sensitivity. This leads to more complex non-annular flow morphologies.

Generalized Summary

Steady Governing Equations: Are They Parabolic or Elliptic?

Thought Experiment:

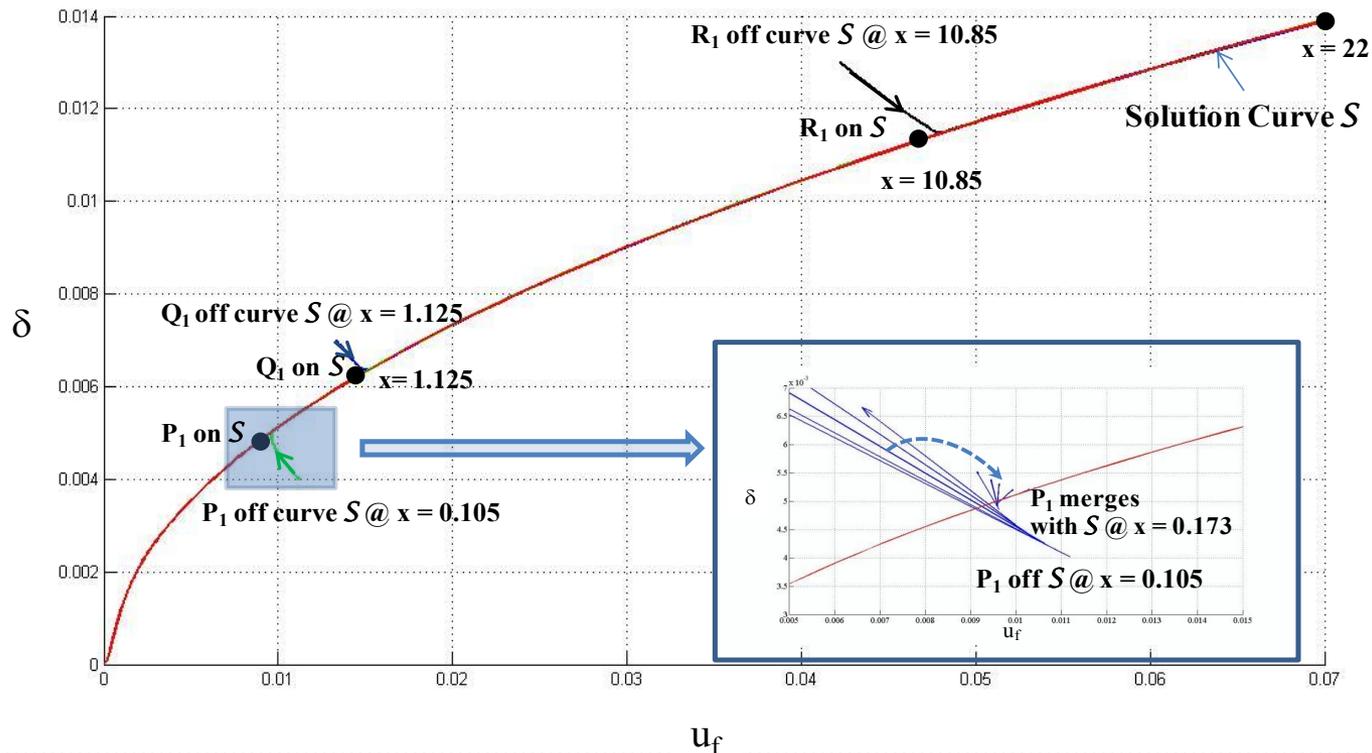


The Steady Governing Equations are Neither Elliptic Nor Parabolic

The quasi 1-D/ full 2-D code results indicate that the steady gravity driven flows behave (in most situations) almost like a parabolic flow as it has a strong attractor even in the absence of exit condition specification.

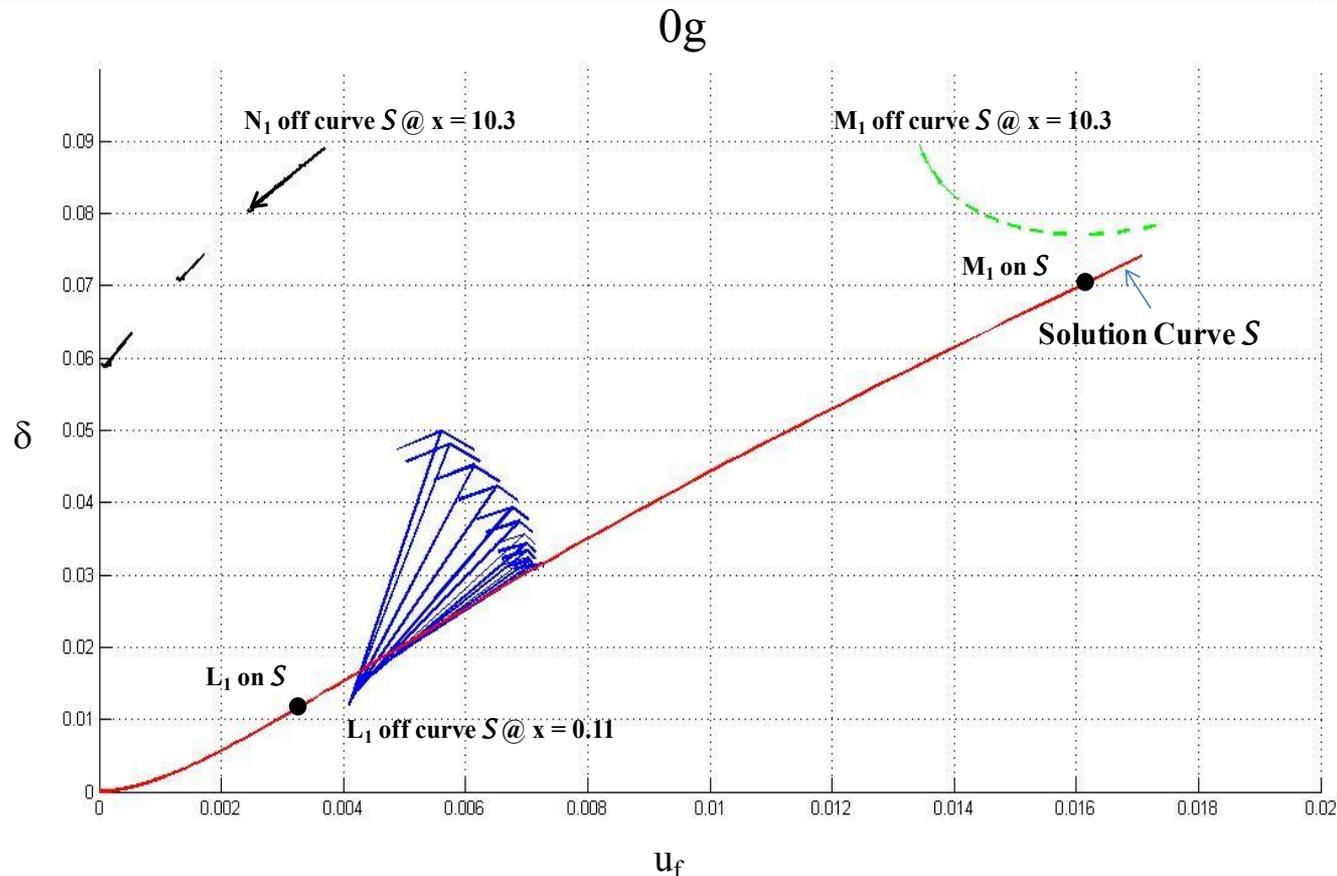
Nature of Steady Solutions and Phase Portrait Diagram

1g



However shear driven (0g or horizontal) internal condensing steady flows behave somewhat like “elliptic” problems as the steady solutions have weak attractors and can be controlled by imposition of exit conditions.

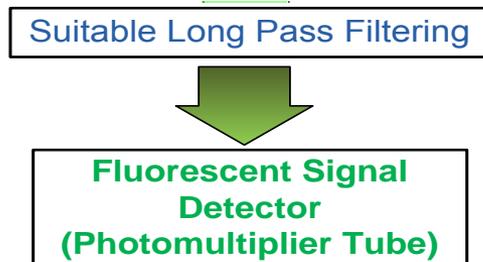
Nature of Steady Solutions and Phase Portrait Diagram Obtained from Quasi 1-D Approach



Sensor Principle

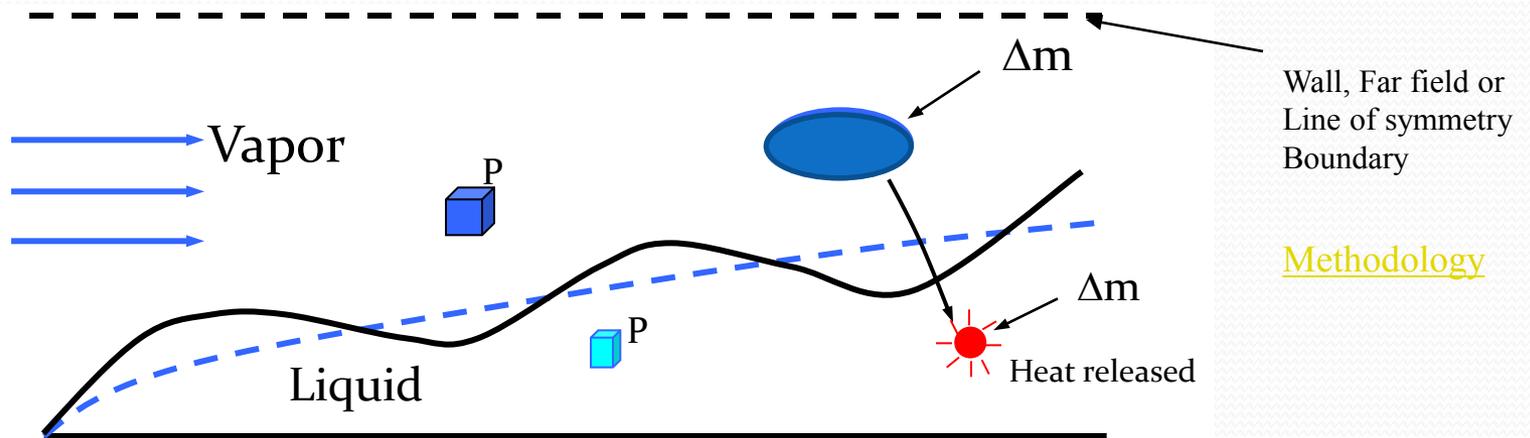
An identifiable part of the amount of “green” fluorescent light collected from the fluorescent dopant depends only on instantaneous thickness “ δ ” for a given concentration of the dopant.

Suitable filtering of
light



First Principles Underlying Flow Physics and Computational Problem

- Continuum governing equations (Mass, momentum, and energy for each differential element in the interior of the two phases)
- Interface conditions (on the unknown interface these are restrictions imposed by: kinematics, mass transfer, momentum transfer, energy transfer, and thermodynamics)



Other conditions

- Wall conditions
- Conditions at infinity (if any)
- Initial conditions ($t = 0$)
- Inlet conditions
- Exit conditions (need ?)

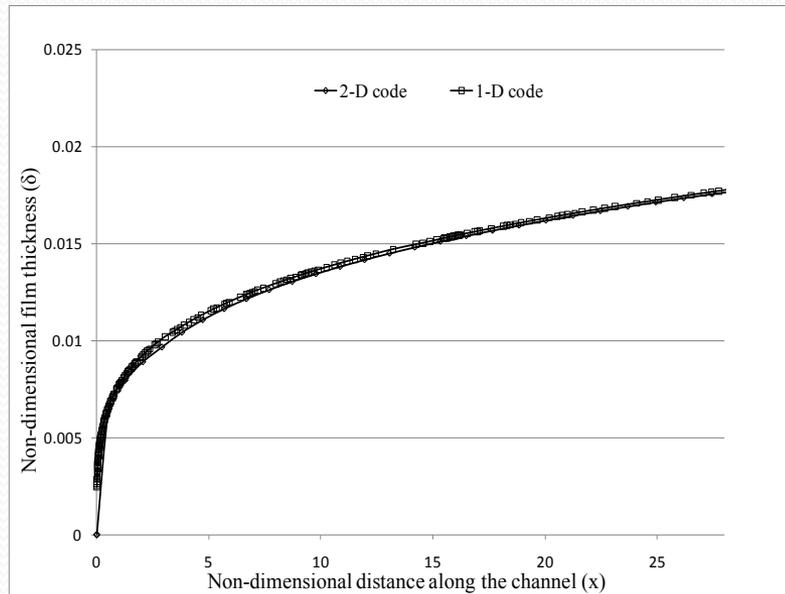
Special features

- Sharp interface
- Single-phase solutions interact through interface conditions
- Interface condition is used for interface tracking
 - Height function with adaptive grid (current)
 - Level-set function (planned)

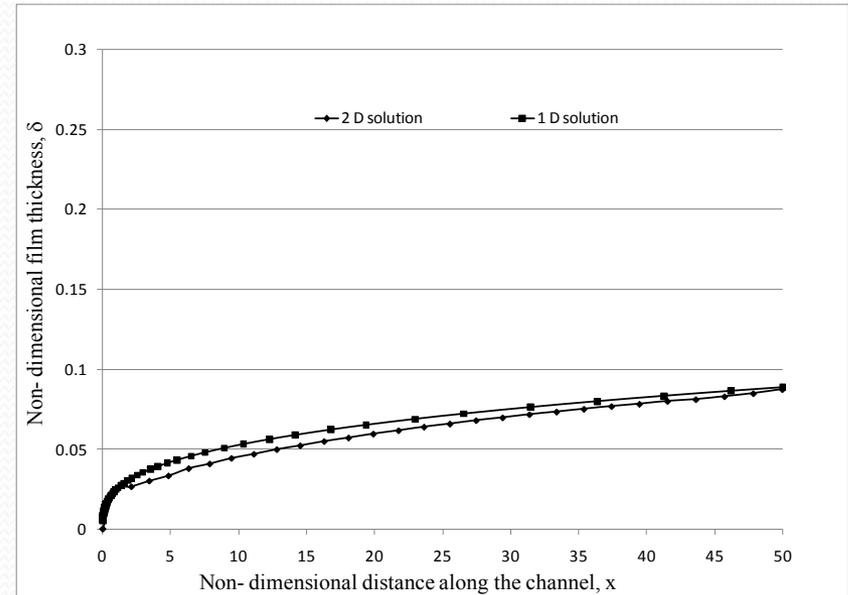
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Comparison of Results Obtained by 1-D and 2-D Solution Techniques for Annular/Stratified Flows

Gravity Driven Flow
in mm Scale Vertical Ducts



Shear Driven Flow
in 0g, Horizontal, and μ m Scale Ducts



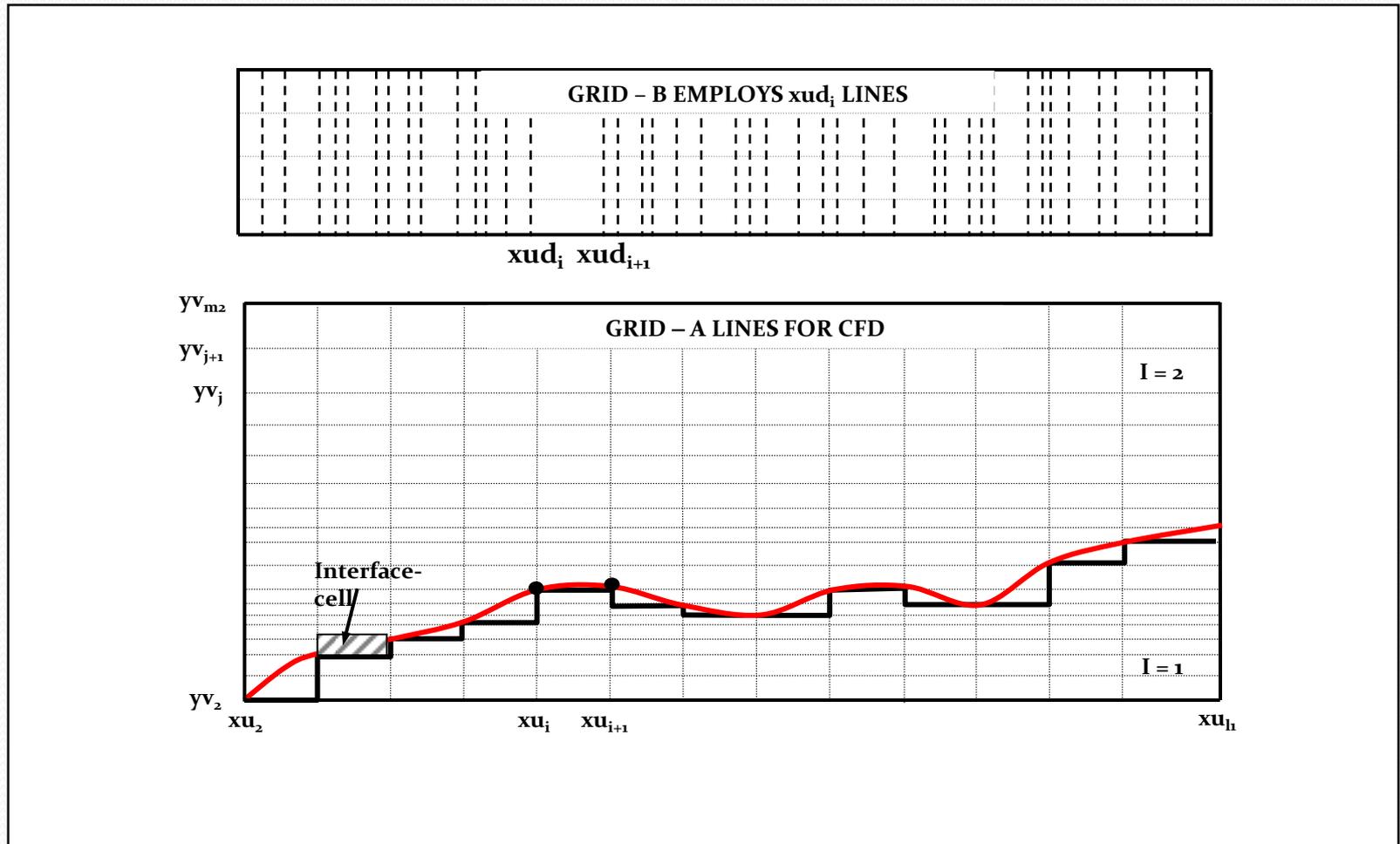
The 2-D and 1-D prediction for other flow variables (interfacial velocity, pressure, etc.) exhibit similar good agreements for different flow conditions and tube geometries as well. Within their own regimes, they also agree with experiments.

Both 1g and 0g flows are stable. Note: (i) gravity driven smooth flows become wavy for $Re_\delta > 30$, but they remain annular/stratified. (ii) Shear driven & 0g flows – though stable (as shown) are not always experimentally realized – except under “controlled” conditions.

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Computational Approach

Adaptive computational grids



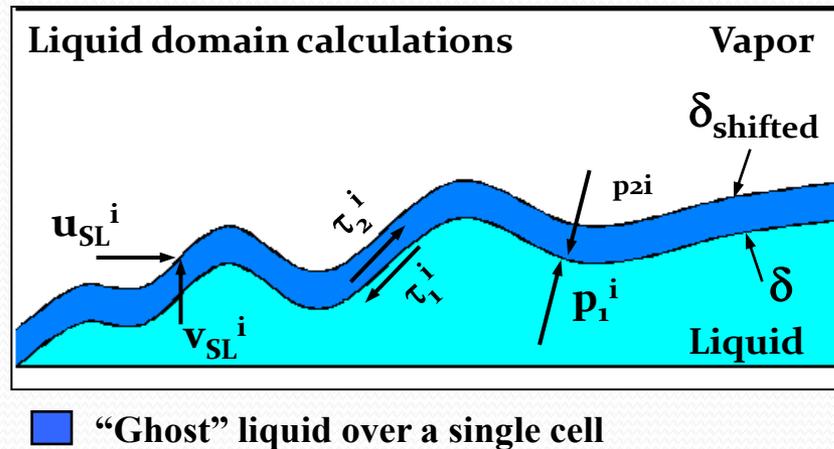
Computational Approach

Iterative solution strategy

At discrete number of spatial locations, guess $\{\delta, u_{SL}^i, v_{SL}^i, \theta_{SL}^i, u_V^i, v_V^i, \theta_V^i\}$ for the steady problem at $t = 0$ and, for the unsteady problem (incompressible vapor and unspecified exit condition) at $t > 0$, for the). Adjust these **seven** guess functions: $\{\delta, u_{SL}^i, v_{SL}^i, \theta_{SL}^i, u_V^i, v_V^i, \theta_V^i\}$ with the help of **seven** interface conditions. The following steps implement this philosophy by separate single-phase (liquid and vapor domain) calculations with a “sharp interface.”

Computational Approach

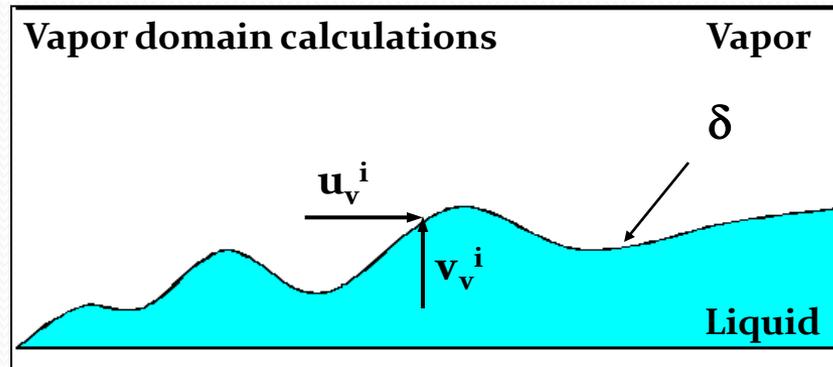
Iterative solution strategy (contd.)



After fixing $\{u_{\text{SL}}^i, v_{\text{SL}}^i, \theta_{\text{SL}}^i\}$ on shifted interface (δ_{shifted}), solve liquid domain under shifted interface by a *finite-volume* (SIMPLER) or a *finite-element* method. The $\{u_{\text{SL}}^i, v_{\text{SL}}^i, \theta_{\text{SL}}^i\}$ are adjusted to satisfy tangential stress (shear), normal stress (pressure), and saturation temperature conditions at the interface.

Computational Approach

Iterative solution strategy (contd.)



- After fixing $\{u_v^i, v_v^i, \theta_v^i\}$ on interface δ , solve vapor domain *above* interface by the same *finite-volume* method (SIMPLER). UPDATE the guesses for u_v^i , v_v^i , and θ_v^i with the help of: continuity of tangential velocity, interfacial mass flux equality $\dot{m}_{VK} = \dot{m}_{Energy}$, and saturation temperature conditions at the interface.

Computational Approach

However Popular Level-Set Methods Use

$$\dot{m}_{LK} = \dot{m}_{Energy} \quad \longrightarrow \quad \frac{\partial \phi}{\partial t} + \bar{\mathbf{V}} \cdot \nabla \phi \cong 0$$

where, $\phi(x,t) = 0$ locates the interface with

$$\bar{\mathbf{V}} \equiv \mathbf{v}_I - (\mathbf{k}_1 \cdot \nabla \mathcal{T}_1|^{extended} - \mathbf{k}_2 \cdot \nabla \mathcal{T}_2|^{extended}) \cdot (1/\rho_1) \cdot (1/h_{fg})$$

with subscript $I = 1$ is for liquid and $I = 2$ is for vapor

In the new COMSOL/MATLAB based approach, we propose to retain our current approach in principle but use the above level-set equation for locating the interface through $\phi = 0$. This will allow investigation of flow regime transitions from annular/stratified flows to plug/slug flows.

Computational Approach

Iterative solution strategy (contd.)

Our Current Practice is to Update δ (by tracking the interface) on an adaptive Eulerian Grid which remains fixed over a time interval $[t, t+\Delta t]$ of interest.

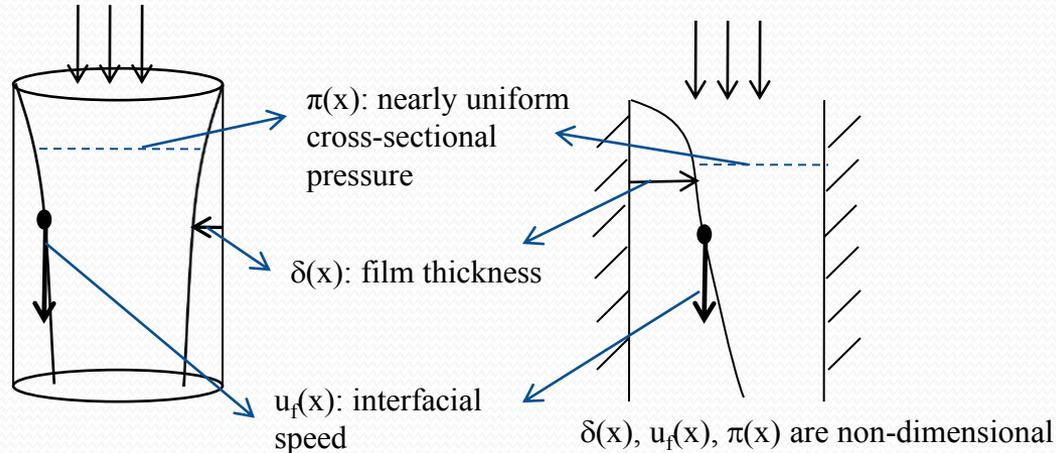
Current method uses $\phi = y - \Delta(x, t) = 0$ and “tracks” the interface through the reduced form of $\dot{m}_{LK} = \dot{m}_{Energy}$ given as:

$$\frac{\partial \delta}{\partial t} + \bar{u}(x, t) \frac{\partial \delta}{\partial x} = \bar{v}(x, t)$$
$$\delta(0, t) = 0$$

$$\delta(x, 0) = \delta_{steady}(x) \text{ or other prescriptions}$$

Alternative Theory/Computational Results from a Quasi 1-D Semi-Analytical Approach

- The method uses exact analytical solutions of the underlying 2-D governing equations under “thin film” approximation. Only the vapor phase momentum and mass balances employ one-dimensional governing equations with an assumed vapor profile. Hence this method is called “Quasi 1-D.”



For the unknown, $\mathbf{y}(x) = [\delta(x), u_f(x), \pi(x), d\pi/dx(x) \equiv \zeta(x)]^T$, the governing equation

$$d\mathbf{y}/dx = \mathbf{g}(\mathbf{y})$$

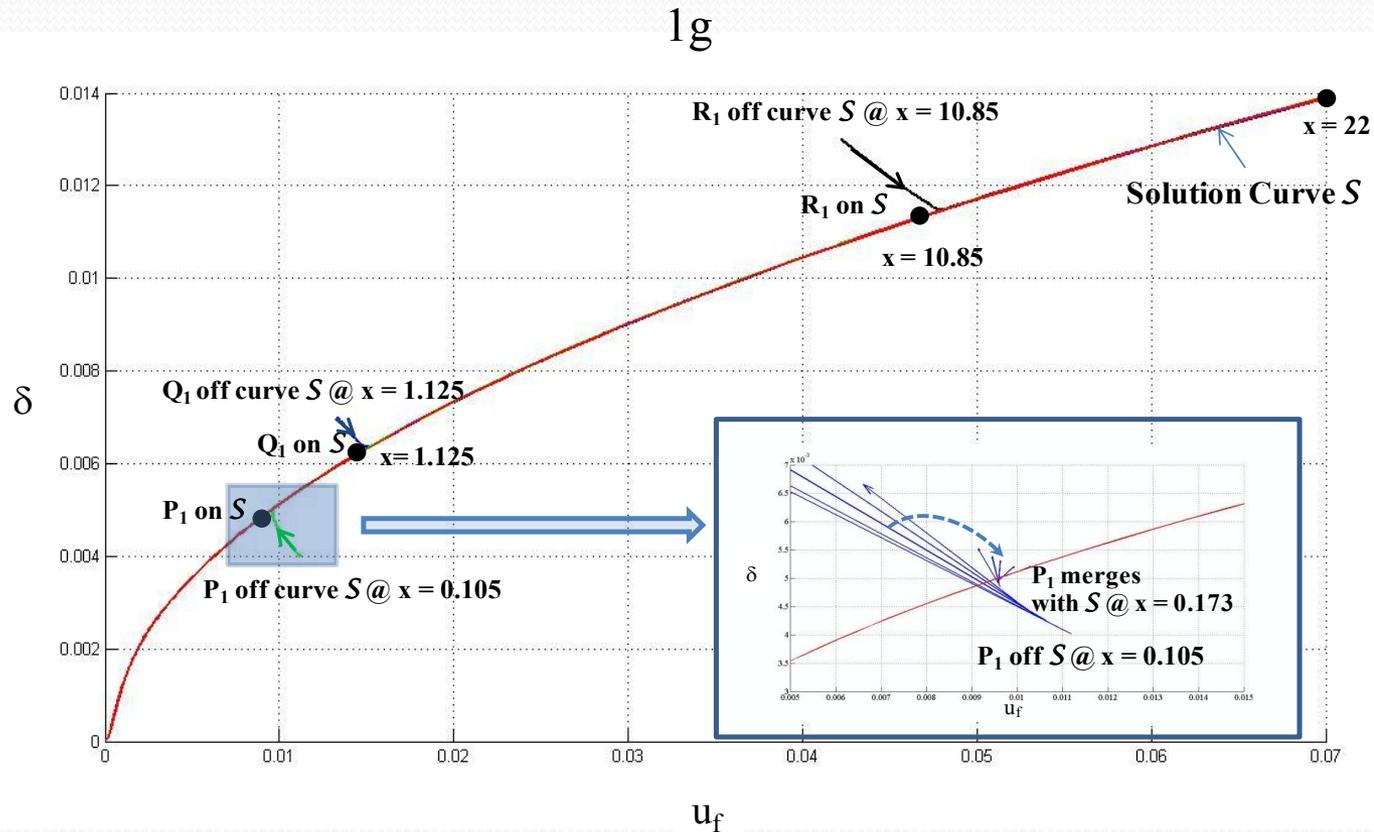
is to be solved, subject to the condition

$$\mathbf{y}(0) = [\delta(0), u_f(0), \pi(0), \zeta(0)]^T \text{ or } \mathbf{y}(\varepsilon) = [\delta(\varepsilon), u_f(\varepsilon), \pi(\varepsilon), \zeta(\varepsilon)]^T \text{ for } x > \varepsilon$$

Salient Features:

- The problem is singular
- Problem is neither parabolic (because of the presence of $\zeta(0^+)$ in the $\mathbf{y}(x)$) – nor clearly elliptic (since explicitly defined values of $\zeta(0^+)$ is not admissible.)

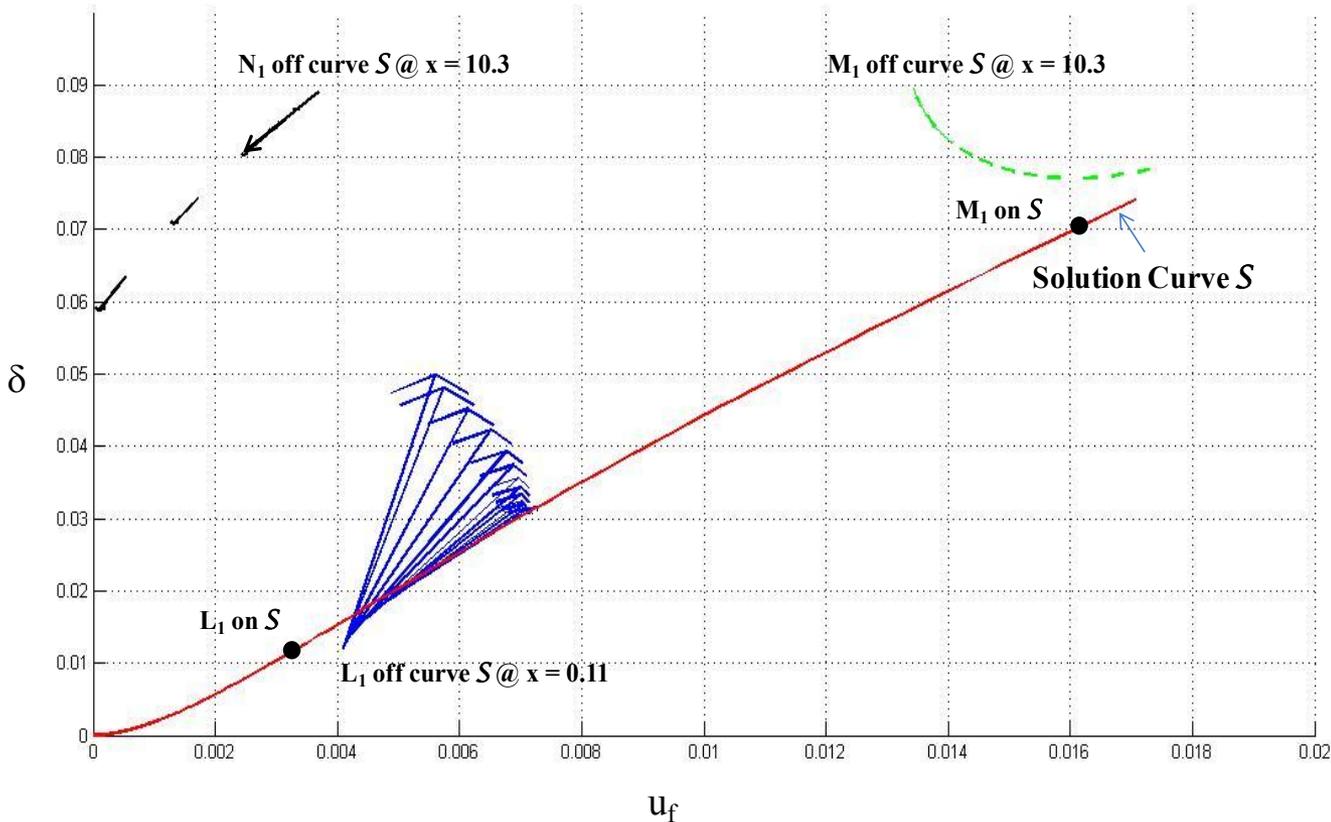
Nature of Steady Solutions and Phase Portrait Diagram



Strictly steady solution in 1g behaves like a “parabolic” solution as it does not need an exit condition specification.

Nature of Steady Solutions and Phase Portrait Diagram

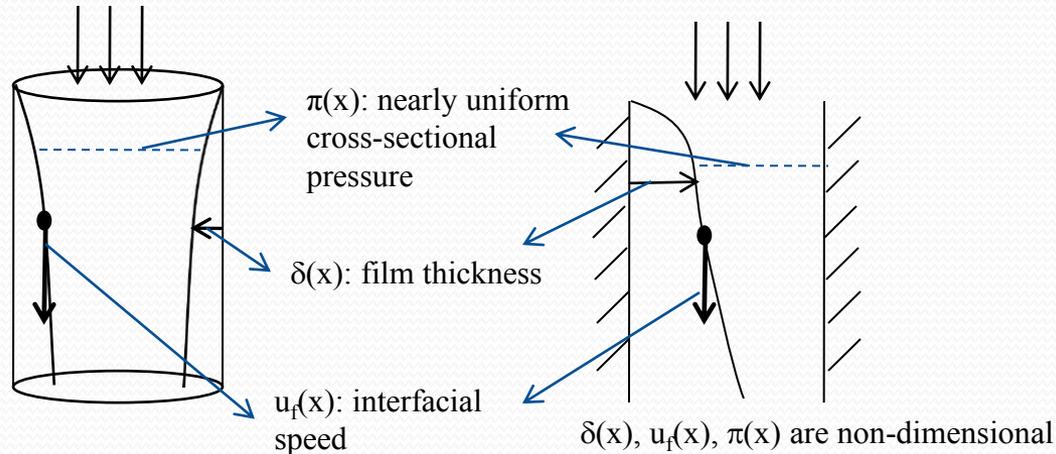
0g



Strictly steady solution in 0g behaves like an “elliptic” problem with “neutral” to “unstable” steady solution that can take different exit conditions.

Alternative Theory/Computational Results from a Quasi 1-D Semi-Analytical Approach

- The method uses exact analytical solutions of the underlying 2-D governing equations under “thin film” approximation. Only the vapor phase momentum and mass balances employ one-dimensional governing equations with an assumed vapor profile. Hence this method is called “Quasi 1-D.”



For the unknown, $\mathbf{y}(x) = [\delta(x), u_f(x), \pi(x), d\pi/dx(x) \equiv \zeta(x)]^T$, the governing equation

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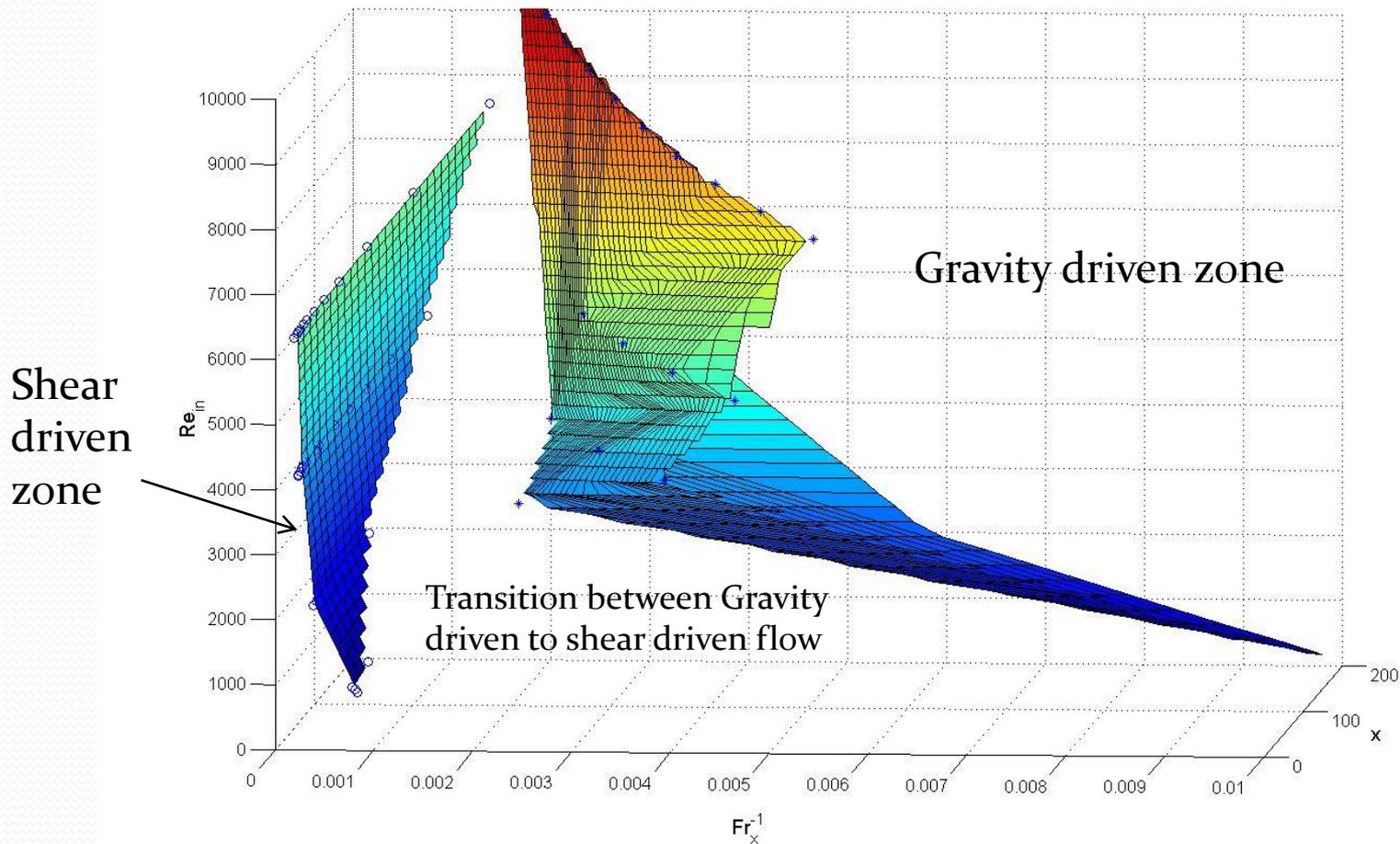
Salient Features:

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[Back](#)

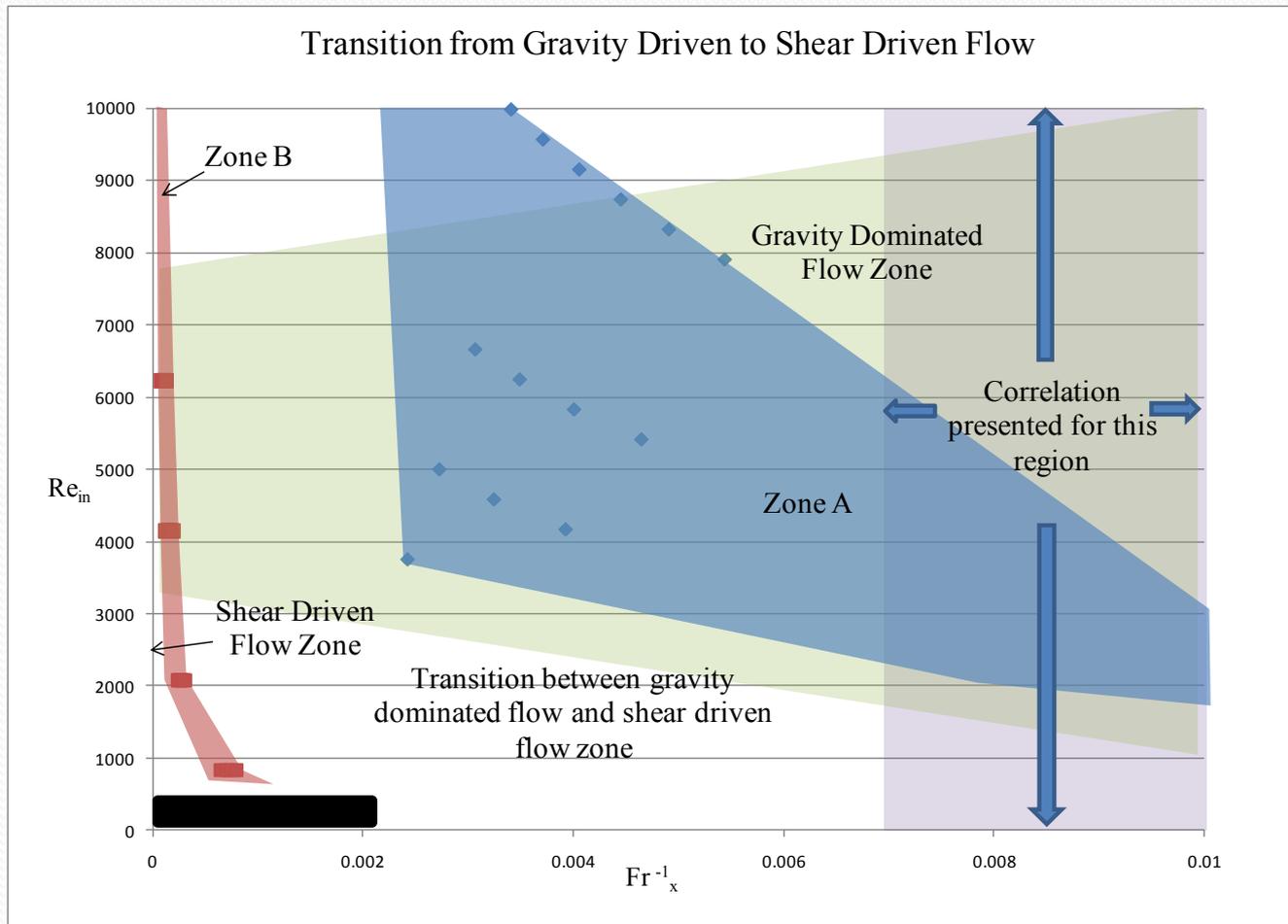
Transition Between Gravity Driven and Shear Driven Flows

Parameters affecting the flows: $\{x, Re_{in}, Fr_x^{-1}, Fr_y^{-1} = 0, Ja/Pr_1, \rho_2/\rho_1, \mu_2/\mu_1\}$



Transition Between Gravity Driven and Shear Driven Flows

In the Re_{in} and Fr_x^{-1} for a constant Ja/Pr_1 , ρ_2/ρ_1 , μ_2/μ_1



Transition Between Gravity Driven and Shear Driven Flows

For 0g flows,

$$\delta_{ps}(x) = \frac{0.7487 * x^{0.35} * (Ja_1 / Pr_1)^{0.3611} * (\rho_2 / \rho_1)^{0.2380}}{Re_{in}^{0.3529} * (\mu_2 / \mu_1)^{0.5947}}$$

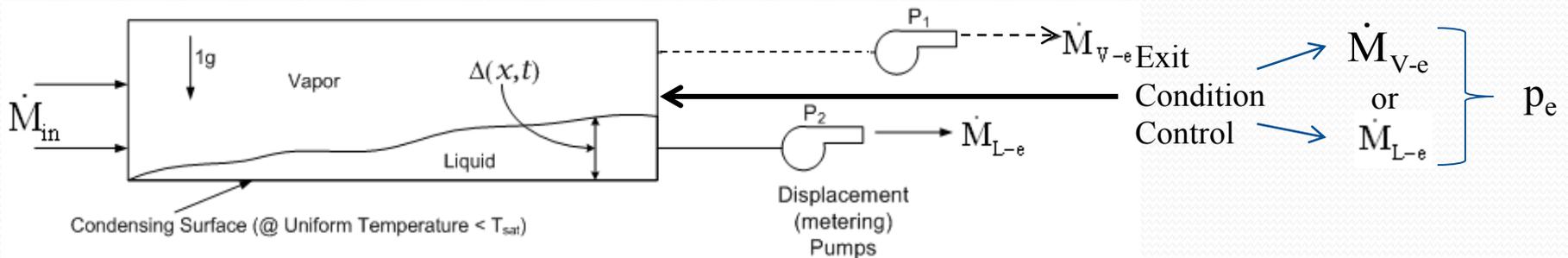
$$0.75x_{FC} = \frac{0.0447 * Re_{in} * (\rho_2 / \rho_1)^{0.43} * (\mu_2 / \mu_1)^{0.49}}{(Ja_1 / Pr_1)^{0.9}}$$

For Gravity driven and mixed flows (shaded purple in the flow regime map)

$$\delta(x) = \frac{15.93 * x^{0.26} * (Ja_1 / Pr_1)^{0.2684} * (\rho_2 / \rho_1)^{0.8065}}{Re_{in}^{0.8056} * (\mu_2 / \mu_1)^{0.8426} * (Fr_x^{-1})^{0.3891}}$$

$$0.75x_{FC} = \frac{2.69 * Re_{in}^{0.1826} * (\rho_2 / \rho_1)^{1.1695} * (\mu_2 / \mu_1)^{0.1085}}{(Ja_1 / Pr_1)^{0.9911} * (Fr_x^{-1})^{0.5334}}$$

Exit Condition Issue for Internal Condensing Flows (Consider Partially Condensing Annular/Stratified Flows)



In the above thought experiment, one asks whether the exit condensate flow rate (\dot{M}_{L-e}) (or equivalent exit pressure) can be used to “control” the flow and achieve multiple quasi-steady solutions (not necessarily annular/stratified). In other words: are these flows “elliptic” (i.e. do these flows listen to both upstream and downstream conditions) ?

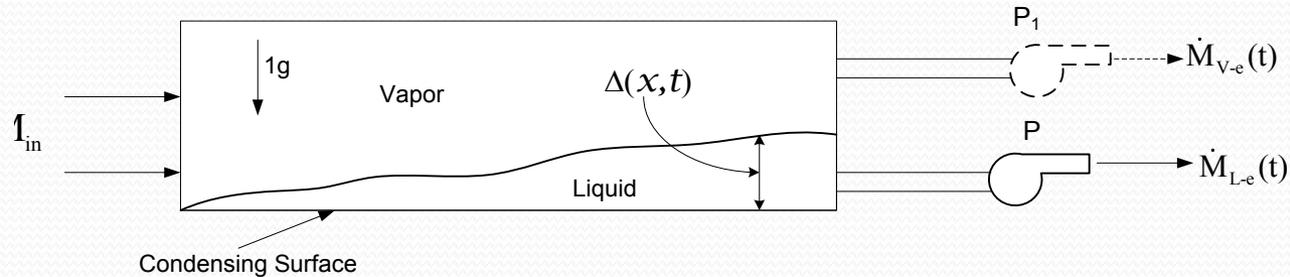
- **Yes!**

Clearly, the above “control” is impossible for single-phase flows or adiabatic two-phase flows (with zero interfacial mass transfer) because, the information only travels downstream (i.e. they are parabolic flows).

Related Issues/Questions:

- What is the nature of the steady governing equations? Are they parabolic (as in single-phase or air-water flows)?
- Are there significant differences between gravity-driven and shear-driven flows?

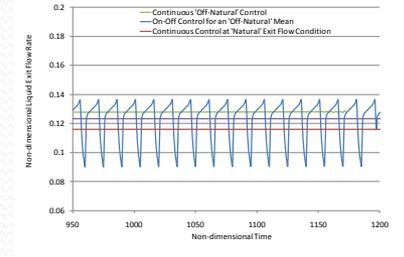
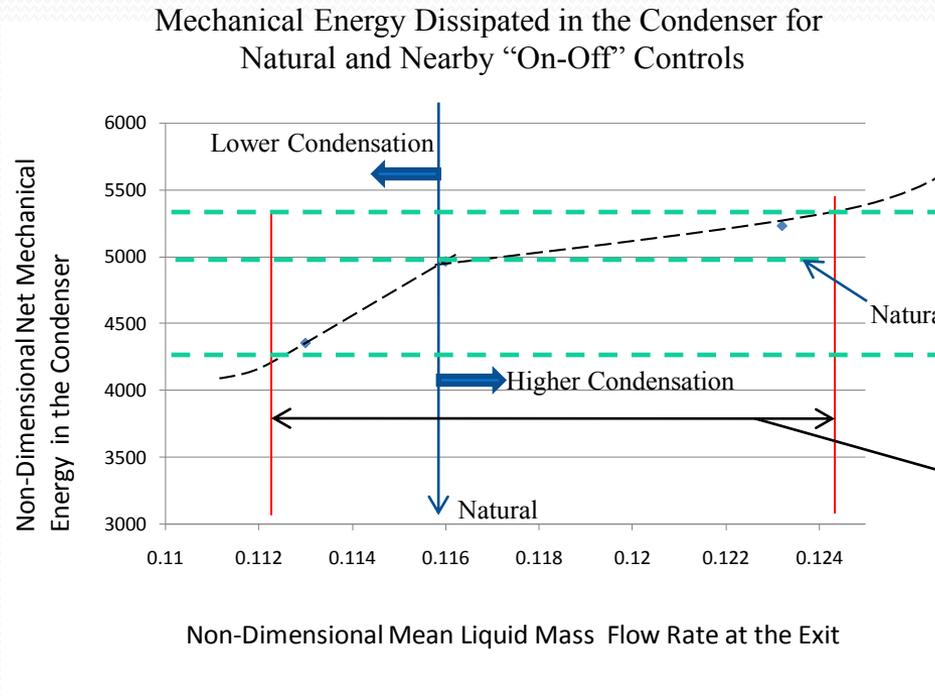
Result 2: Basic Results on Flow Controllability



- For an internal condensing flow, there is a unique steady “natural” annular/stratified (or “film” condensation) solution which can be realized in the absence of any “active” imposition of exit condition– i.e. when the set up allows the flow to seek its own exit condition.
- However one can “actively” impose different steady or quasi-steady exit conditions other than the “natural” one. This typically leads to other time dependent or quasi-steady solutions which may cause the flow regime to shift from annular stratified to non-annular (plug, slug, etc.) flows. This shows that the unsteady equations for these flows are “elliptic” – i.e. exit conditions matter. The impact is significant for shear driven flows and insignificant for gravity driven flows.
- For partial condensation, exit condition can be imposed either through control of the liquid exit mass flow rate or vapor exit mass flow rate – achieved by active pumping with the help of displacement pump P or P₁ shown in the figure above.
- The response of the flow to this controllability depends on:
 - Nature of the exit flow rate control function
 - Type of the annular/stratified flow - i.e. gravity driven or shear driven

Result 2 (contd.): Energy Dissipation in the Condenser

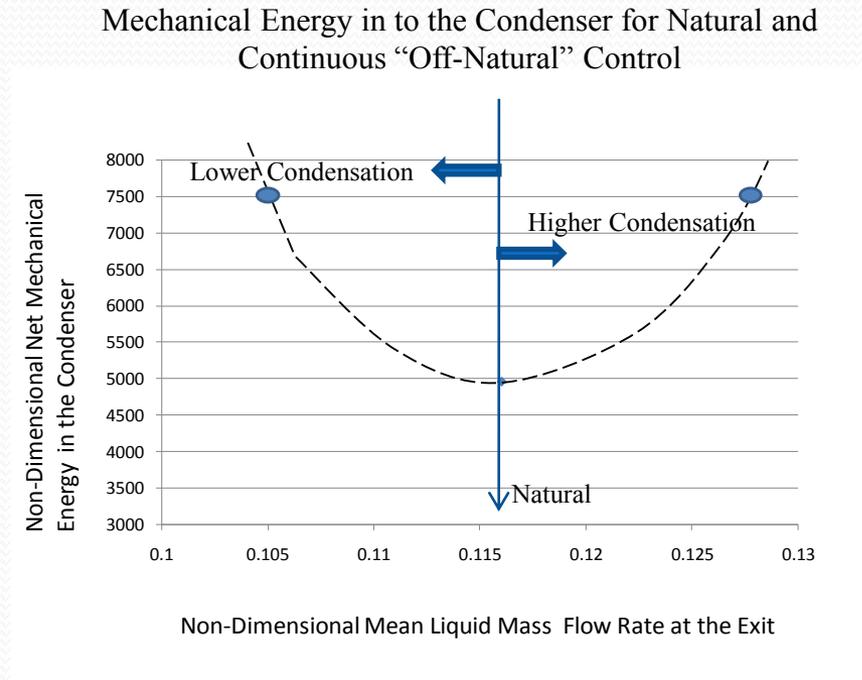
“On-Off” control with a mean that is near “natural”:
Results obtained by the computational tool



Annular flows realized through “on-off” control in this range correspond to the limited steady energy band associated with this control.

For “on-off” controls in the vicinity of steady “natural” energy consumption indicated above—nearby steady solutions exist. This makes PID control of exit flow rate possible – because the mean of the “on-off” control does not have to be exactly at the “natural.”

Result 2 (contd.): Energy Dissipation in the Condenser



Continuous “Off-Natural” Control: Long time ($t \rightarrow \infty$) non-annular quasi-steady flows mean that dissipative energy results can only be conjectured. The conjectured result is:

Key Experimental Results for Partially Condensing Internal Condensing Flows

- Gravity driven flows were found to be “parabolic” and no exit conditions could be experimentally imposed.
- For shear driven flows, repeatable annular stratified “natural” cases were achieved for unspecified exit conditions.
- For shear driven flows, theoretical results for flow controllability through exit conditions are being currently experimentally investigated and the results are expected soon.

Key Experimental Results for Fully Condensing Internal Condensing Flows

- Gravity driven flows were found to be “parabolic” and no exit conditions could be experimentally imposed.
- For shear driven fully condensing flows, repeatable complex morphology flows were experimentally achieved.
- For shear driven flows, theoretical results for flow controllability through exit conditions are being currently experimentally investigated and the results are expected soon.